

# Machine Learning Based on Kernel Function Controlled Gaussian Process Regression Method for In-depth Extrapolative Analysis of Covid-19 Daily Cases Drift Rates

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**Abstract:** Precise extrapolative mining and analysis of relevant dataset during or after any disease outbreak can assist the government, stake holders and relevant agencies in the health sector to make important decisions with respect to the disease outbreak control and management. While prior works has concentrated on non-stationary long term data, this work focuses on a short term non-stationary and relatively noisy data. Particularly, a distinctive nonparametric machine learning method based kernel-controlled probabilistic Gaussian process regression model has been proposed and employed to model and analyze Covid-19 pandemic data acquired over a period of approximately six weeks. To accomplish the aim, the MATLAB 2018a computational and machine learning environment was engaged to develop and perform the Gaussian process extrapolative analysis. The results displayed high scalability and optimal performance over the commonly used machine learning methods such as the Neural networks, Neural-Fuzzy networks, Random forest, Regression tree, Support Vector machines, K-nearest neighbor and Discriminant linear regression models. These results offer a solid foundation for conducting research on reliable prognostic estimations and analysis of contagious disease emergence intensity and spread.

**Index Terms:** Covid-19 pandemic, short term, Non-stationary data, kernel, Machine learning, Gaussian process regression

## 1. Introduction

In spite of unrelenting efforts to improve on the health care systems and processes globally, the outbreak and spreading of corona virus disease 19 epidemics, also popularly shortened as 'Covid-19' that is currently ravaging the whole human wellbeing remain a primary public health challenge.

In Nigeria, the first confirmed COVID-19 pandemic case was made known publicly on 27 February 2020. This happened when an Italian national who visited Lagos around the said date tested positive for the virus [1] [2]. Up till date, information of such confirmed COVID-19 pandemic cases are being reported daily globally, including the length and breathe of Africa, and well as our dear Country-Nigeria.

Nevertheless, realistic response to such quantum epidemics counts on propitious intervention, superlatively informed by available up-to-date data sources. Also, the visualization and predictive analysis of such epidemic data can play a vital role in exclusive decision making. Predictive analysis plays a decisive head the cast role in driving fruitful outcomes and scrutinizing pain points [3] [4]. Specifically, the provision of detail predictive analysis of such Covid-19 data can assist the government, stake holders and relevant agencies in the health sector and relevant agencies to make important decisions with respect future disease outbreak control and management. The results of the quantitative predictive analysis can as well help to reveal whether various efforts currently being put in place to manageably control or curtail the disease outbreak is effective or not.

## 2. Literature Review

There exist many linear or nonlinear disease extrapolative models and methods in literature and among they key ones are autoregressive integrated moving average (ARIMA) [5] [6], Neural Networks (NN) [7]-[20] and nonlinear autoregressive neural networks (NAR) [21]. However, ARIMA, NN and NAR models, including other similar ones usually performed poorly on non-stationary long-term data and noisy data sets [22-28].

In [14, 15, 23, 24], the authors explored the long short-term memory model (LSMM) to tackle the non-stationary long-term data with time series analysis. But the LSMM only predicts well when the data is large [25-28].

In this paper, a machine learning based on Gaussian process regression model that is capable of handling both simple and complex input-output data relationship, including the non-stationary data and noisy Covid-19 data sets is presented. The impact of different kernels (covariance functions), which usually impose some level of characteristics weights on the Gaussian process modelling are also investigated and reported.

## 3. Methodology

In this research work, nonparametric machine learning method based kernel-controlled probabilistic Gaussian process regression model has been proposed and employed to model and analyze Covid-19 pandemic data acquired over a period of approximately six weeks. To accomplish the aim, the MATLAB 2018a computational and machine learning environment was engaged to develop and perform the Gaussian process extrapolative analysis.

### 3.1. Gaussian Regression Process

Gaussian processes (GP) can be described as a finite assemblage of conjointly random variables with (stable) Gaussian distribution. In terms of regression problems, these random variables define and characterize the values of a function  $f(x)$  over an  $x$  input and  $y$  output space.

Given a  $k$  training set of data,  $\mathfrak{N}_1 = [(x_i, y_i)]_{i=1}^k$ , where  $x_i$  expresses the input vector and  $y_i$  the target, the desire is to efficiently learn a function  $f(x_i)$  such that the input vector  $x_i$  is transform into the target  $y_i$  as defined by:

$$y_i = f(x_i) + \varepsilon_i; i = 1, 2, \dots, t \tag{1}$$

where

$\varepsilon$  designate the Gaussian zero mean noise and  $\sigma_i^2$  the variance.

The observed target can equally be defined using the expression equation (2):

$$y_i \approx N(0, K(X, X) + \sigma_i^2 I); i = 1, 2, \dots, t \tag{2}$$

where

$K(X, X)$  expresses the covariance matrix.

Now, let  $\mathfrak{N}_2 = [(x_i^t, y_i^t)]_{i=1}^{k^*}$  is another set of unknown i.i.d. testing data samples like the  $\mathfrak{N}_1$ .

The combined distribution of the focused target data values and the expected desired predicted output over the input vector can be described by:

$$\begin{bmatrix} f \\ \bar{f}^* \end{bmatrix} \Big|_{X, X^*} \approx N \left( \bar{0}, \begin{bmatrix} K(X, X) + \sigma_i^2 I & K(X, X^*) \\ K(X^*, X) & K(X^*, X^*) \end{bmatrix} \right) \tag{3}$$

where

$$X = \begin{bmatrix} -(x_1)^T \\ -(x_2)^T \\ \vdots \\ -(x_k)^T \end{bmatrix} \in \mathbb{R}^{n \times m}, \quad \bar{y} = \begin{bmatrix} (y_1)^T \\ (y_2)^T \\ \vdots \\ (y_k)^T \end{bmatrix} \in \mathbb{R}^m \tag{4}$$

$$\bar{f} = \begin{bmatrix} f(x_1)^T \\ f(x_2)^T \\ \vdots \\ f(x_k)^T \end{bmatrix} \in \mathbb{R}^{m \times n}, \quad \varepsilon = \begin{bmatrix} (\varepsilon_1) \\ (\varepsilon_2) \\ \vdots \\ (\varepsilon_k) \end{bmatrix} \in \mathbb{R}^m \tag{5}$$

$$X^* = \begin{bmatrix} -(x_1)^T \\ -(x_2)^T \\ \vdots \\ -(x_k)^T \end{bmatrix} \in \mathbb{R}^{n \times m}, \quad \bar{y}^* = \begin{bmatrix} (y_1^*)^T \\ (y_2^*)^T \\ \vdots \\ (y_k^*)^T \end{bmatrix} \in \mathbb{R}^{m^*} \tag{6}$$

$$\bar{f}^* = \begin{bmatrix} f(x_1^*)^T \\ f(x_2^*)^T \\ \vdots \\ f(x_k^*)^T \end{bmatrix} \in \mathbb{R}^{m^* \times n}, \quad \epsilon = \begin{bmatrix} (\epsilon_1^*) \\ (\epsilon_2^*) \\ \vdots \\ (\epsilon_k^*) \end{bmatrix} \in \mathbb{R}^{m^*} \tag{7}$$

and

$$K(X, X) \in \mathbb{R}^{m \times n}, \quad K(X, X^*) \in \mathbb{R}^{m \times m^*}, \quad K(X^*, X) \in \mathbb{R}^{m^* \times n} \text{ and } K(X^*, X^*) \in \mathbb{R}^{m^* \times m^*}$$

### 3.2. Kernels

The kernel (or covariance function) plus the mean function completely delineates the Gaussian process modeling. There exist a number of kernels which can impose different characteristics weights on the Gaussian process modelling. The ones investigated in this work includes: ardexponential, squaredexponential, ardsquaredexponential, exponential, ardrationalquadratic, rationalquadratic, matern32, ardmatern32, matern52, and ardmatern52.

### 3.3 Six Alternative Regression Models for Comparison.

- (a) **A multilayer perceptron (MLP) Neural Network.** MLP is a special popular feedforward artificial neural network (ANN) model with at least three layered nodes. Its input-output prediction function can be expressed as [18, 20]:

$$y(x) = f_{log}(w_o + \bar{w}, \bar{x}) + b \tag{8}$$

where  $f_{log}$  denote the logistic function,  $w_o$  is the weight matrix,  $\bar{w}$  and  $\bar{x}$  are the  $k$ th neurons number and the input variable,  $b$  is the bias.

- (b) **Decision Regression Trees (DRT):** Regression trees are known distinctive nonlinear regression machine learning model for predictive analysis. Its input-output prediction function can be defined as:

$$y(x) = \frac{1}{z} \sum_{i=1}^z y_i \tag{9}$$

where  $z$  denote the available observation number at a specified cell.

- (c) **Support Vector Machine (SVM):** SVM regression is another nonlinear regression machine learning model used for predictive analysis. Its input-output prediction function for non-linear regression can defined as:

$$y(x) = \sum_{i=1}^c (\alpha_i - \alpha_i^*) . k(x_i, x) + b \tag{10}$$

where  $\alpha_i, \alpha_i^*$  designate the langrage multipliers,  $c$  is the bias term and  $k(.)$  is the kernel function.

- (d) **Neural-Fuzzy.** SVM is a special hybrid nonlinear supervised learning model which combines neural networks with that of fuzzy logic for robust data predictions. Its input-output ANFIS (adaptive neuro-fuzzy inference system) based prediction function can defined as:

$$y(o) = \sum_{i=1} \bar{w}_i f_i = \frac{\sum_{i=1} w_i f_i}{\sum_{i=1} w_i} \tag{11}$$

where  $\bar{w}$  is the output layer.  $f_1, f_2$  express the hybridized least square function and gradient descent function

- (e) **Random Forest:** Random forest is a predictor made up of randomized base regression trees collection of randomized base regression trees  $\{r_n(x, \theta_m, D_n) | m \geq 1\}$ . Its input-output function can be defined as:

$$r_n(x, D_n) = E_o \{r_n(x, \theta_m, D_n)\} \tag{12}$$

where  $\theta_m$  indicate the i.i.d. randomizing output variable.  $E_o$  denotes expectation in correspondence with the random parameter, and the data set  $D_n$ .

(f) **K-nearest Neighbors:** K-nearest Neighbors (KNN) is a nonparametric regression method which employs 'feature similarity' to estimate and predict new data points' values. Its input-output function can be defined as [29]:

$$f(x) = \frac{1}{K} \sum_{x_i \in N_o}^K y_i \tag{13}$$

where

K= nearest neighbor number

$x_o$ . = the prediction point

$N_o$ , = training observation number

(g) **Linear Discriminant analysis Regression:** Linear discriminant analysis employs number of prediction equations to estimate cluster membership from predictors set by means of independent variables. Its input-output function can be defined as:

$$D = a + b_1x_1 + b_2x_2 \dots + b_mx_m \tag{14}$$

where:

a, b= modelling parameters

x. = input variable

m, = training observation number

#### 4. Data Collection and Transformation Method

The six weeks Covid-19 datasets used in this work were obtained from Nigeria Center for Disease Control (NCDC) website database (<https://ncdc.gov.ng/>) [30]. The NDCDC is the Nigeria public health institute, established by the Government with the sole responsibility to control, prevent, detect, respond and manage public health emergencies and infectious disease outbreaks. Among other key responsibilities, the institute is also empowered to organize surveillance systems for data collection, synthesization and provision on different diseases of public health importance.

The data collected from the institute are of two main parts. The first part consist of only confirmed cases of Covid-19 disease infected persons across thirty states in Nigeria since 13<sup>th</sup> March, 2020. The second part consist confirmed cases of daily infected persons in admission, discharged person who recovered from Covid-19 disease after treatment, persons who died of Covid-19 disease during treatment.

Each portion of the obtained data where processed and standardized before passing it through it the different regression training processes. Their scripts coding and execution was achieved using Matlab 2018a software/user interface. Regression and some of their Key training parameters and algorithms are provided in table 1:

Table 1. Regressors and some of their Key training parameters/algorithms

| Regressor Name               | Some Key training parameters/algorithms   |
|------------------------------|---|
| MLP Neural Networks          | Training algorithm: trainlm, No. of layers/neurons: 2:20, NumEpochs = 50                    |
| Neural-Fuzzy Networks        | NumMfs = 20; MfType = gbellmf, NumEpochs = 100  |
| Support Vector               | Kernel function: Gaussian, KFold:5, KernelScale:auto, OptimizeHyperparameters; auto         |
| Linear Discriminant Analysis | DiscrimType: linear, Holdout:0.3, Optimizer: bayesopt                                       |
| Random Forest                | Method:Bag,NumLearningCycles:200  |
| Binary Decision tree         | MaxNumSplits:7, Optimizer: bayesopt   |
| K-nearest neighbor           | NumNeighbors:2,distfunctn:Euclidean   |
| Gaussian Process             | Kernel function: Squared exponential, FitMethod: sr, PredictMethod: fic Optimizer: bayesopt |

#### 5. Results and Analysis

Here, all the graphics and computations were achieved using Matlab 2018a software. First, we start by looking at the impact of different kernels (covariance functions), which usually impose high degree of characteristics weights on the Gaussian process modelling. Table 2 display the attained prediction performance impact of the ten different kernels on confirmed cases Covid-19 data using four evaluation metrics such as mean absolute error (MAE), standard deviation error (STD), coefficient of determination ( $R^2$ ) and root mean absolute error (RMSE). A lower MAE, STD AND RMSE

values indicate superior prediction accuracy.  $R^2$  value close or equal to 1 means the predicted out values correlate well with the focused target data. The results reveal that all kernels almost have the same predictive performance results. However, squaredexponential recorded the lowest MAE of 0.0010 compared to others. Therefore, Gaussian process regression with squaredexponential kernel is chosen and employed in the remaining parts of this work.

Table 2. Prediction Errors and R2 Values for 10 different Kernels investigated

| Kernel                | MAE    | STD    | RMSE   | R <sup>2</sup> |
|-----------------------|--------|--------|--------|----------------|
| ardexponential        | 0.0018 | 0.0438 | 0.0442 | 1.0000         |
| squaredexponential    | 0.0010 | 0.0020 | 0.0020 | 1.0000         |
| ardsquaredexponential | 0.0060 | 0.0076 | 0.0075 | 1.0000         |
| exponential           | 0.0409 | 0.0609 | 0.0409 | 1.0000         |
| ardrationalquadratic  | 0.0058 | 0.0075 | 0.0075 | 1.0000         |
| rationalquadratic     | 0.0020 | 0.0021 | 0.0021 | 1.0000         |
| matern32              | 0.0034 | 0.0047 | 0.0046 | 1.0000         |
| ardmatern32           | 0.0027 | 0.0038 | 0.0038 | 1.0000         |
| matern52              | 0.0011 | 0.0020 | 0.0020 | 1.0000         |
| ardmatern52           | 0.0062 | 0.0079 | 0.0079 | 1.0000         |

Figs. 1 to 8 display predictive analysis graphs of confirmed cases of Covid-19 data plotted using are the Gaussian process regression model with squaredexponential kernel and seven other models for the purpose of comparison. From the graphs and Table 3, the focus Gaussian process regression model display the best prediction performance with approximately 0.008 RMSE value when compared to Neural networks, Neural-Fuzzy networks, Neural-fuzzy model, Random forest, Regression tree, Support Vector Machines, K-nearest model and Discriminant regression model models that attained 28.87, 6.75, 38.84, 41.58, 40.19, 9.23 and 17.23 RMSE values.

The summarized results of table 4 shows the predictive performance of different regression model on confirmed cases data of daily infected persons in admission, data on discharged persons that recovered from Covid-19 disease after treatment, and lastly data on persons who died of Covid-19 disease since 13<sup>th</sup> March to 17<sup>th</sup> May, 2020. Though the Gaussian process regression model display a best prediction results on all Covid-19 data as usual, but we can also observed from the table that neural-fuzzy prediction accuracies are also very high, probably due to its hybrid nature. This results also implies that neural-fuzzy model can be used an alternative model. On the other hand, support vector machine and Random forest regression models performed the worst prediction result.

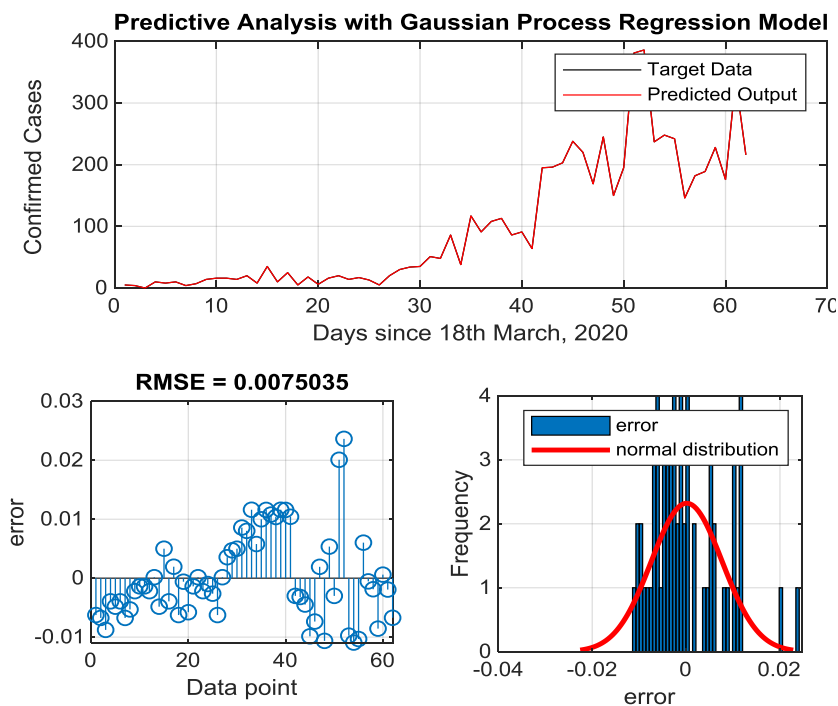


Fig. 1. Predictive analysis plot with Gaussian process regression

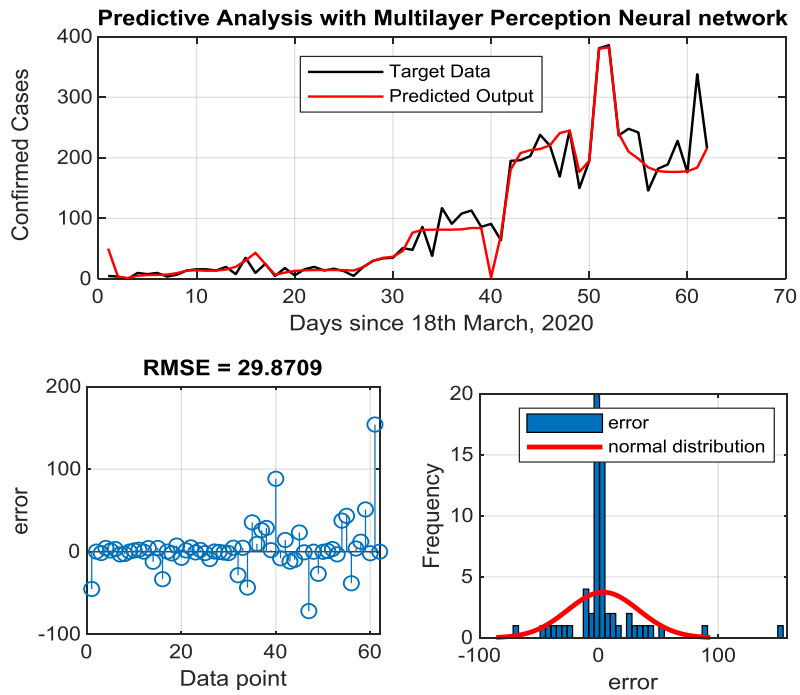


Fig. 2. Predictive analysis plot with Neural network Model

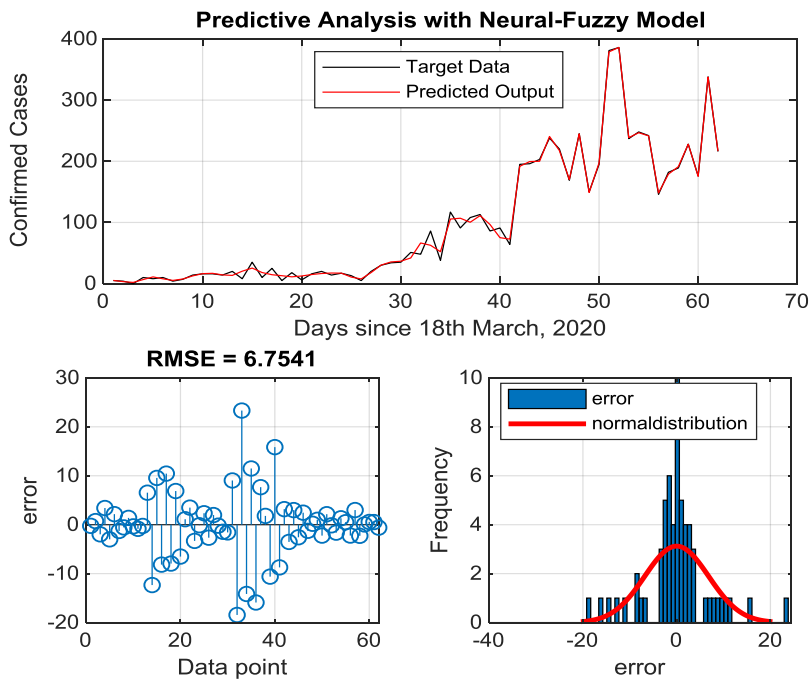


Fig.3. Predictive analysis plot with Neural-Fuzzy model

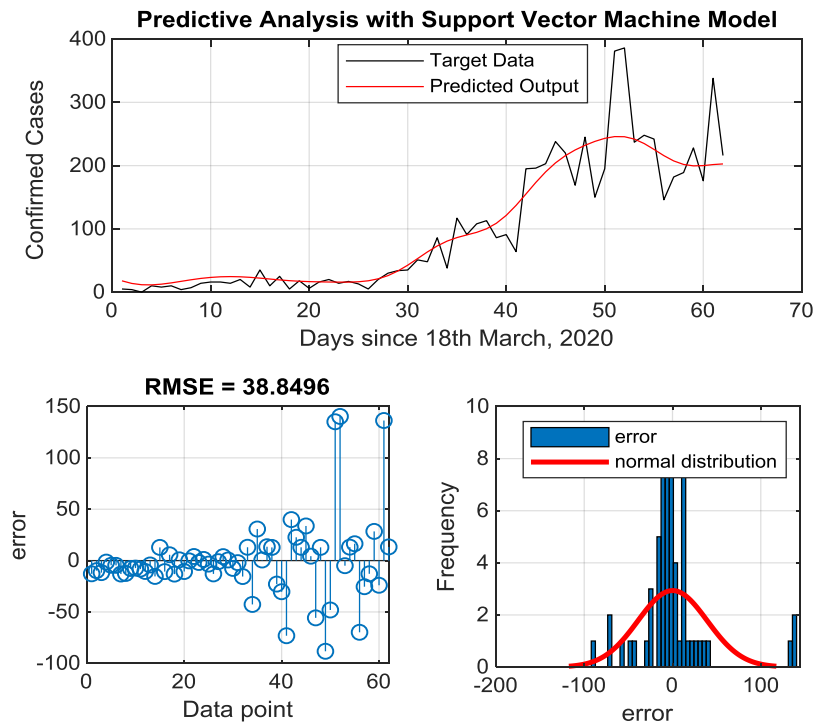


Fig. 4. Predictive analysis plot with Support Vector Machine model

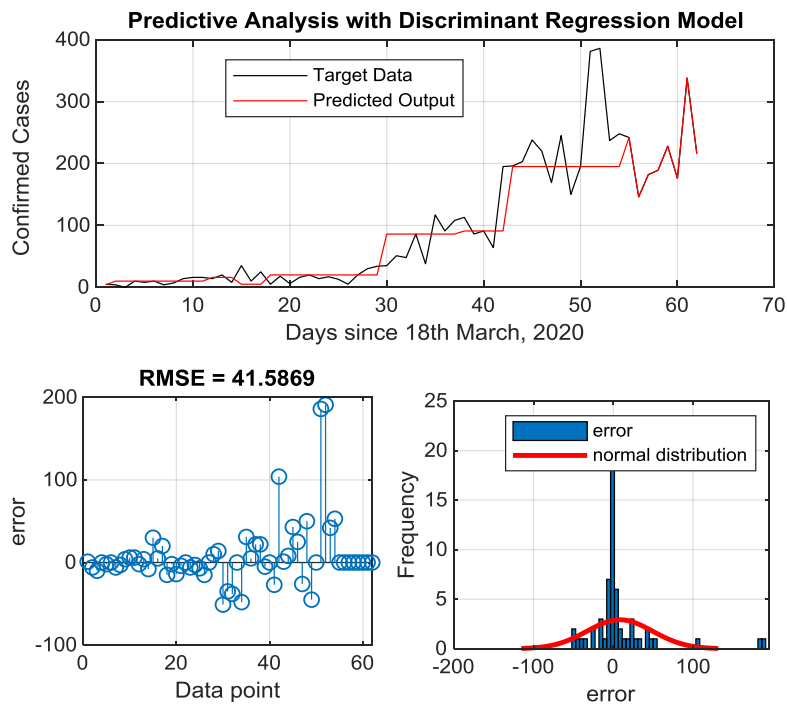


Fig. 5. Predictive analysis plot with Discriminant regression model

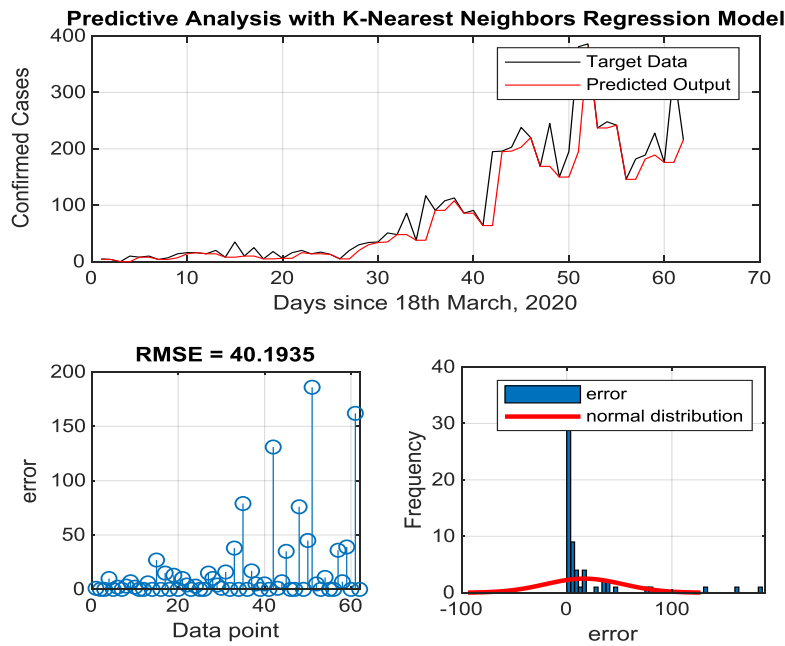


Fig. 6. Predictive analysis plot with K-Nearest Neighbor model

Table 3. Prediction Errors and R<sup>2</sup> Values for 8 different Regression Models investigated

| Regression Model       | MAE   | STD   | RMSE  | R <sup>2</sup> |
|------------------------|-------|-------|-------|----------------|
| MLP Neural Network     | 15.32 | 29.90 | 29.87 | 0.9563         |
| Neural-Fuzzy Network   | 4.420 | 274   | 6.81  | 0.9978         |
| Support Vector Machine | 22.75 | 1411  | 37.17 | 0.9260         |
| Discriminant           | 20.33 | 1261  | 41.11 | 0.9153         |
| K-nearest Neighbor     | 1668  | 1034  | 38.87 | 0.9208         |
| Decision Tree          | 6.59  | 407   | 9.81  | 0.9954         |
| Random Forest          | 25.25 | 1565  | 42.48 | 0.9126         |
| Gaussian Process       | 0.006 | 0.369 | 0.008 | 1.0000         |

Table 4. Prediction Errors and R<sup>2</sup> Values for 8 different Regression models investigated

|   | Regression Model       | MAE    | STD    | RMSE   | R <sup>2</sup> |
|---|------------------------|--------|--------|--------|----------------|
| Prediction results using Data on Confirmed cases of persons on admission                    | MLP Neural Network     | 11.75  | 23.53  | 25.72  | 0.9949         |
|   | Neural-Fuzzy Network   | 0.02   | 0.02   | 0.02   | 1.0000         |
|   | Support Vector Machine | 73.94  | 305.01 | 307.57 | 0.2654         |
|   | Discriminant Linear    | 8.91   | 19.71  | 20.97  | 0.9966         |
|   | K-nearest Neighbor     | 41.08  | 215.82 | 216.54 | 0.6959         |
|   | Decision Tree          | 11.88  | 27.47  | 27.04  | 0.9943         |
|   | Random Forest          | 88.11  | 300.24 | 276.59 | 0.3109         |
|   | Gaussian Process       | 0.008  | 0.01   | 0.01   | 1.0000         |
| Prediction results using Data on discharge cases of persons that recovered from the disease | MLP Neural Network     | 14.93  | 43.44  | 42.44  | 0.8285         |
|   | Neural-Fuzzy Network   | 0.05   | 0.020  | 0.010  | 1.000          |
|   | Support Vector Machine | 20.41  | 76.70  | 76.66  | 0.4547         |
|   | Discriminant           | 2.68   | 4.97   | 5.02   | 0.9977         |
|   | K-nearest Neighbor     | 17.62  | 75.16  | 75.96  | 0.4646         |
|   | Decision Tree          | 3.37   | 5.75   | 5.67   | 0.9970         |
|   | Random Forest          | 28.42  | 86.98  | 85.90  | 0.3153         |
|   | Gaussian Process       | 0.01   | 0.01   | 0.01   | 1.0000         |
| Prediction results using daily Data of those that died of the disease within the period     | MLP Neural Network     | 3.51   | 6.52   | 6.59   | 0.5859         |
|   | Neural-Fuzzy Network   | 0.002  | 0.002  | 0.002  | 1.0000         |
|   | Support Vector Machine | 3.26   | 7.28   | 7.58   | 0.4534         |
|   | Discriminant           | 2.57   | 6.50   | 6.44   | 0.6055         |
|   | K-nearest Neighbor     | 1.45   | 3.73   | 3.96   | 0.8590         |
|   | Decision Tree          | 0.88   | 2.00   | 1.97   | 0.9629         |
|   | Random Forest          | 3.81   | 7.00   | 6.93   | 0.5427         |
|   | Gaussian Process       | 0.0002 | 0.0004 | 0.0005 | 1.0000         |



## 6. Conclusion

In recent years, prognostic-based data mining by means of machine learning models have been gaining cute recognition and relevance in different research areas of science, medicine engineering and humanity.

In this work, a kernel-based probabilistic Gaussian process regression model, which is a distinctive nonparametric machine learning method has been proposed and employed to model and analysis the acquired data over a period of approximately six weeks. To accomplish the task, the MATLAB 2018a computational and machine learning environment was engaged to develop and perform the Gaussian process extrapolative analysis. By worth of some key evaluation metrics such as mean absolute error, standard deviation error, coefficient of determination and root mean absolute error, the extrapolative results of the adopted model reveal robust performance over the commonly used machine leaning types such as the Neural networks, Neural-Fuzzy networks, Neural-fuzzy model, Random forest, Regression tree, Support Vector Machines, K-nearest model and Discriminant regression model.

In future work, prognostic and prescriptive analysis of global datasets on Covid-19 pandemic with larger geographical areas would be the focus.

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