ACO Algorithm Applied to Multi-Objectives Optimization of Capacity Expansion in Next Generation Wireless Network

Dac-Nhuong Le\textsuperscript{a,*}, Son Hong Ngo\textsuperscript{b}, and Vinh Trong Le\textsuperscript{c}

\textsuperscript{a}Faculty of Information Technology, Haiphong University, Haiphong, Vietnam
\textsuperscript{b}Hanoi University of Science and Technology, Hanoi, Vietnam
\textsuperscript{c}Hanoi University of Science, Vietnam National University, Vietnam

Abstract

The optimal capacity expansion of base station subsystems in Next Generation Wireless Network (NGWN) problem with respect to multi-demand type and system capacity constraints is known to be NP-complete. In this paper, we propose a novel ant colony optimization algorithm to solve a network topology has two levels in which mobile users are sources and both base stations and base station controllers are concentrators. There are two important aspects of upgrading to NGWN. The first importance of backward compatibility with pre-existing networks, and the second is the cost and operational benefit of gradually enhancing networks, by replacing, upgrading and installing new wireless network infrastructure elements that can accommodate both voice and data demand. Our objective function is the sources to concentrators connectivity costs as well as the cost of the installation, connection, replacement, and capacity upgrade of infrastructure equipment. We evaluate the performance of our algorithm with a set of real world and data randomly generated. Numerical results show that our algorithm is a promising approach to solve this problem.

Index Terms: Next Generation Wireless Network, Multi-Objectives, Capacity Expansion, Base Station Subsystems, Ant Colony Optimization.

1. Introduction

The Next Generation Wireless Networks (NGWNs) are expected to provide high data rate and optimized quality of service to multimedia and real-time applications over the Internet Protocol (IP) networks to anybody, anywhere, and anytime. The wireless network infrastructure consists of equipment required by mobile network operators to enable mobile telephony calls or to connect fix subscribers by radio technology. The interacting layers architecture of next generation wireless network is shown in fig.1.
The architectural building blocks enabling mobile telephony are:

\(\begin{align*}
\text{i) The core network:} & \text{ comprised of the mobile switching centers (MSC), the packet data serving nodes (PDSN), and home agents (HA), and} \\
\text{ii) The base station subsystem (BSS) also known as the radio access network, consisting of base station controllers (BSC), base transceiver stations (BS), and mobile stations (MS).}
\end{align*}\)

Each BS is typically assigned a group of radio channels to support a number of mobile stations in its cell. BS’s at adjacent cells are assigned different sets of frequencies. The antennas of a BS are designed to achieve coverage only within the particular cell. By limiting coverage of a BS to its cell area, the set of frequencies assigned to this BS can be reused at other BS’s that are distant enough to keep co-channel interference within acceptable limits. The MSC is a modified central office switch, with extensions for mobile subscriber databases and intelligent network links, which enable the MSC to decide where to route an incoming call. If the requested subscriber for example is registered to be located in the MSC’s area, the call will be routed to the respective BSC. The BSC is part of the link between the BS and the MSC and is responsible for allocating and releasing radio channels to the MSs by way of the BS. In addition to managing channels on a radio interface, the BSC is also responsible for managing MS handovers to other radio channels. Other BSC functions include routing calls to the MSC, handling call control processes, and maintaining a database of subscribers and records of calls for billing [2]. The BSC is directly connected to the MSC and the PDSN. The PDSN is the point of entry into the wireless packet data network for mobile subscribers. The PDSN performs two basic functions [1], which are (1) exchanging packets with the mobile station over the radio network and (2) exchanging packets with other IP networks. The PDSN is generally coupled with HA, which is a router on a mobile node’s home network that maintains information about the device’s current location, as identified in its care-of address [3]. Corresponding to the architectural building blocks of a wireless network, are three types of interconnects [4]. These are (1) mobile device to BS interconnect, which includes both forward and reverse radio links, (2) the BS to BSC interconnect, which is called the backhaul, and (3) BSC to MSC interconnect.

In the network design and capacity planning literature, conventional approaches to meeting demand growth include location and installation of additional network elements [5-6]. The more commonly known
ACO Algorithm Applied to Multi-Objectives Optimization of Capacity Expansion in Next Generation Wireless Network

hierarchical capacitated concentrator location problem, which is an extension of the concentrator location problem to multiple levels and a classical research issue in the telecommunications literature [7-10]. However, this approach ignores two important aspects of upgrading to NGWN. The first importance of backward compatibility with pre-existing networks, and the second is the cost and operational benefit of gradually enhancing networks, by replacing, upgrading and installing new wireless network infrastructure elements that can accommodate both voice and data demand. In [6], the author used a greedy heuristic algorithm to solve the maximal coverage location problem in cellular communication Systems. A Tabu search algorithm and genetic algorithm approach to cellular capacity expansion to maximizing the coverage area and minimizing the number of transmitters is presented in [11-12]. Yu et al in [13] proposed a set covering algorithm for given traffic and finding optimal solution configuration in a CDMA network. A greedy strategy to optimal positioning of base stations for cellular radio networks and capacity planning of UMTS networks studied in [14-15]. An alternate approach to capacity planning and expansion is introduced for 3G network system capacity without an increase in base stations using a cell splitting approach [16]. In [17], the authors studied the base station location and service assignment problem in a W-CDMA.

The recently research in [18-22], we have proposed a novel particle swarm optimization (PSO) and ant colony optimization (ACO) algorithms to optimal location of controllers in wireless networks and centralized wireless access network. In this paper, we focus on the Multi-Objectives Optimal of Capacity Expansion (MOOCE) in NGWN and propose a novel ACO algorithm to solve it. The rest of this paper is organized as follows: Section 2 presents the MOOCE problem formulation. Section 3 presents our new algorithm to solve it based on ACO algorithm. Section 4 presents our simulation and analysis results, and finally, section 5 concludes the paper.

2. Problem formulation

In this section, we assume the network topology of base station subsystems have mobile users, n base stations, and p base station controllers. We introduce the following notation:

<table>
<thead>
<tr>
<th>Notation</th>
<th>Meaning</th>
</tr>
</thead>
<tbody>
<tr>
<td>$M$</td>
<td>Index set of Mobile user locations: $M = {MS_i, \forall i = 1..m}$</td>
</tr>
<tr>
<td>$N$</td>
<td>Index set of all Base Station (BS): $N = N1 \cup N2 = {BS_j, \forall j = 1..n}$</td>
</tr>
<tr>
<td>$N1$</td>
<td>Index set of existing BS; $N2$: Index set of potential BS</td>
</tr>
<tr>
<td>$P$</td>
<td>Index set of Base Station Controllers (BSC): $P = P1 \cup P2 = {BSC_k, \forall k = 1..p}$</td>
</tr>
<tr>
<td>$T_j$</td>
<td>Set of types available for $BS_j$, $\forall j \in N$</td>
</tr>
<tr>
<td>$S$</td>
<td>Set of commodity types: $s = \begin{cases} 1 &amp; \text{if commodity type is voice} \ 2 &amp; \text{if commodity type is data} \end{cases}$</td>
</tr>
<tr>
<td>$N_t$</td>
<td>Index set of all BS of type $t$. $N_t = N1_\cup N2_t$</td>
</tr>
<tr>
<td>$D_t$</td>
<td>Demand of commodity type $s$ for mobile user $MS_i$, $\forall i \in M$</td>
</tr>
<tr>
<td>$MaxBS_{Cap_j}$</td>
<td>Maximum capacity of $BS_j$ type $t$, $\forall j \in N_t$</td>
</tr>
<tr>
<td>$MaxBSC_{Cap_k}$</td>
<td>Maximum capacity of $BSC_k$, $\forall k \in P$</td>
</tr>
<tr>
<td>$d_{hi}$</td>
<td>Distance of mobile user $MS_i$ from $BS_j$ of type $t$ $\forall i \in M, \forall j \in N_t$</td>
</tr>
</tbody>
</table>
ACO Algorithm Applied to Multi-Objectives Optimization of Capacity Expansion in Next Generation Wireless Network

<table>
<thead>
<tr>
<th>Notation</th>
<th>Meaning</th>
</tr>
</thead>
<tbody>
<tr>
<td>$MaxBS_Cov_{j}$</td>
<td>Maximum coverage range for $BS_j$ of type $t$</td>
</tr>
<tr>
<td>cost_connect$_{jk}$</td>
<td>Cost of connecting $BS_j$ of type $t$ to $BSC_k$</td>
</tr>
<tr>
<td>cost_install$_k$</td>
<td>Cost of installing $BSC_k, \forall k \in P2$</td>
</tr>
<tr>
<td>cost_upgrade$_j$</td>
<td>Per channel cost of upgrading $BS_j, \forall j \in N1$</td>
</tr>
<tr>
<td>cost_setup$_{jt}$</td>
<td>Cost of constructing and connecting $BS_j, \forall j \in N2$</td>
</tr>
</tbody>
</table>

The MOOCE in NGWN problem has two steps: the initial assignment of MSs to BS and the connection of BS to BSC and capacity expansion and traffic increase with constraint specifies that:

- Each mobile user $MS_i$ will be assigned to exactly one base station $BS_j$ of type $t$
- Mobile users are within that base stations’ maximum range $MaxBS\_Cov$
- At most one base station of type $t$ can exist at location $j$
- If a base station $BS_j$ is operated, it has to be connected to a $BSC_k$ and the BSC has to be active.
- The capacity constraints of the model, in which we argue that BSs must have the necessary capacity to accommodate traffic demand of all demand types $s$ for all MSs assigned to it and the BSC must have the necessary capacity to accommodate all BSs assigned to it.

In the first step, we use the indicator variables are:

- $\alpha_j = \begin{cases} 1 \text{ if } BS_j \text{ of type } t \text{ is operated} \\ 0 \text{ otherwise} \end{cases}$
- $\beta_{jk} = \begin{cases} 1 \text{ if } BS_j \text{ of type } t \text{ is connected to } BSC_k \\ 0 \text{ otherwise} \end{cases}$
- $\delta_k = \begin{cases} 1 \text{ if } BSC_k \text{ is operated in initial assignment} \\ 0 \text{ otherwise} \end{cases}$

Fig. 2. The Initial Assignment step with indicator variables

Fig. 2 show an example of an existing initial assignment that each mobile user can be assigned to only one BS, while each BS has to be connected to a single BSC.

In the second step, we use the decision variables are:
Fig. 3 illustrates an assignment after capacity expansion and traffic increase, and indicates the respective decision variables. New wireless BSS infrastructure equipment with BS and BSC in red shades. The objective of MOOCE is to minimize the total cost of expanding an initial wireless BSS to accommodate increased traffic demand. The MOOCE problem can be defined as follows:

\[ \text{Min} \sum_{j=1}^{\bar{n}} \sum_{i=1}^{\bar{m}} \left( \text{cost\_connect}_{ij} Y_{ijk} - \beta_{jk} \right) + \sum_{k=1}^{\bar{p}} \text{cost\_install}_k (W_k - \delta_k) + \sum_{j=1}^{\bar{n}} \text{cost\_upgrade}_j \left( \sum_{i=1}^{\bar{m}} \text{MaxBS \_cap}_i Z_{ij} - \alpha_{ij} \right) + \sum_{j=1}^{\bar{n}} \sum_{k=1}^{\bar{p}} \text{cost\_setup}_k Z_{kj} \]

Subject to:

\[ \sum_{j=1}^{\bar{n}} X_{ij} = 1, \quad \forall i = 1..m \]  \hspace{1cm} (2)

\[ d_x X_{ij} \leq \text{MaxCov}_j Z_{ij}, \quad \forall i = 1..m, j = 1..n, t \in T_j \]  \hspace{1cm} (3)

\[ \sum_{t \in T_j} Z_{ij} \leq 1, \quad \forall j = 1..n \]  \hspace{1cm} (4)

\[ Z_{ij} \leq \sum_{k=1}^{\bar{p}} Y_{ijk}, \quad \forall j = 1..n, t \in T_j \]  \hspace{1cm} (5)

\[ Y_{ijk} \leq W_k, \quad \forall k = 1..p, j = 1..n, t \in T_j \]  \hspace{1cm} (6)

\[ \sum_{j=1}^{\bar{n}} \sum_{i=1}^{\bar{m}} D_x X_{ij} \leq \text{MaxBS \_Cap}_j \times Z_{ij}, \quad \forall j = 1..n, \quad t \in T_j \]  \hspace{1cm} (7)
ACO Algorithm Applied to Multi-Objectives Optimization of Capacity Expansion in Next Generation Wireless Network

\[ \sum_{j=1}^{n} \sum_{t \in T_j} Y_{j,k} \leq \text{MaxBSC} \times \text{Cap}_k \times W_k, \quad \forall k = 1..p \]  

\[ X_{ij} \in \{0,1\}, \quad Y_{j,k} \in \{0,1\}, \quad Z_{ji} \in \{0,1\}, \quad W_k \in \{0,1\} \]

\[ \forall i = 1..m, \quad j = 1..n, \quad k = 1..p, \quad t \in T_j \]

3. ACO based Algorithm for The MOOCE

3.1. Ant Colony Optimization

The ACO algorithm is originated from ant behavior in the food searching. When an ant travels through paths, from nest food location, it drops pheromone. According to the pheromone concentration the other ants choose appropriate path. The paths with the greatest pheromone concentration are the shortest ways to the food. The optimization algorithm can be developed from such ant behavior. The first ACO algorithm was the Ant System [23], and after then, other implementations of the algorithm have been developed [24].

3.2. Solving the MOOCE based on ACO

In this section, we present application of ACO technique with the dynamic local heuristic information for the MOOCE problem. Our new algorithm is described as follows:

In the first step, we construct a transport network \( G1 = (V1, E1) \), where \( V1 = M \cup N1 \cup P1 \) in which \( M = \{1,2,...,m\} \) is the set of MSs, \( N1 = \{1,2,...,n1\} \) is the set of existing BSs, \( P1 = \{1,2,...,p1\} \) is the set of existing BSCs and \( E1 \) is the set of edge connections between \( MS_i \) to existing BS and existing BS to existing BSC\( _k \) satisfy constraints. We find the maximum flow of the transport network \( G1 \) by adding two vertices \( S \) (Source) and \( D \) (Destination) is shown in Fig.4 to defines indicator variables.

In Fig.4, nodes has white color is set of existing MS, BS, BSC. The weight of the edges on the graph \( G1 \) is defined as follows:

- The edges from vertex \( S \) to \( MS_i \) is demand of commodity type \( s \) for mobile user, denoted as \( c(S,MS_j) = D^s_i, (i=1..m) \).
• The edges from MS<sub>i</sub> to BS<sub>j</sub> is capacity of MS<sub>i</sub> if MS<sub>i</sub> is connected to BS<sub>j</sub>, denoted as \( c(i,j) = D^i_j \), \((i=1..m, j=1..n1)\).

• The edges from BS<sub>j</sub> to BSC<sub>k</sub> is total capacity of MS<sub>i</sub> is connected to BS<sub>j</sub>, denoted as

\[
c(j,k) = \sum_{i, \text{MS connected BS}_{j}} D^i_j \text{, (j = 1..n1, k = 1..p1)} \tag{10}\]

• The edges from BSC<sub>k</sub> to vertex D is total capacity of BS<sub>j</sub> connected to BSC<sub>k</sub>, denoted as

\[
c(k,D) = \sum_{j, \text{BS connected BSC}_{k}} c(i,j) \text{, (j = 1..n1, k = 1..p1).} \tag{11}\]

In the second step, we construct a transport network \( G_2 = (V_2, E_2) \), where \( V_2 = M \cup N \cup P \) in which \( M = \{1,2,..,m\} \) is the set of MSs, \( N = \{1,2,..,n\} \) is the set of BSs, \( P = \{1,2,..,p\} \) is the set of BSCs and \( E_2 \) is the set of all edge connections between MS<sub>i</sub> to BS<sub>j</sub> and BS<sub>j</sub> to BSC<sub>k</sub>.

![Fig. 5. The FullGraph G2 determine the decision variables](image)

Fig. 5 show all edge connections possible satisfy the constraints (2)-(9). In which, red nodes are set of potential BSs, and blue nodes are set of potential BSCs.

A colony of artificial ants is created to find solutions. Optimization problems solutions can be expressed in terms of feasible paths on the graph \( G_2 \). The encoding of the ant \( Ant_k \) configuration is by means of binary string \( Ant_k = \{x_1,x_2,..,x_{m+n+p}\} \), where

\[
x_i = \begin{cases} 
1 & \text{if } i \in [1..m] \text{ then MS}_i \text{ is operated} \\
1 & \text{if } i \in [m+1..m+n] \text{ then BS}_j \text{ is operated (} j = i - m \text{)} \\
1 & \text{if } i \in [m+n+1..m+n+p] \text{ then BSC}_k \text{ is operated (} k = i - m - n \text{)} \\
0 & \text{otherwise} 
\end{cases} \tag{12}\]
In our case, we use real encoding to express an element of the pheromone matrix is generated by graph $G_2$ that represent a location for ant movement, and in the same time it is possible receiver location. A path by each $Ant_k$, pheromone intensities on links are evaporated with a pheromone update rule. Each edge $(i, j)$ of the graph $G_2$ is associated a total pheromone concentration $\tau_{ij}$. At each node, each $Ant_k$ executes a decision policy to determine the next node of the path. If $Ant_k$ is currently located at node $i$ and it selects the next node $j \in N_i^k$ according to the transition probability defined by:

$$p_{ij}^k = \frac{[\tau_{ij}]^\alpha [\eta_{ij}]^\beta}{\sum_{i \in N_i^k} [\tau_{ij}]^\alpha [\eta_{ij}]^\beta}$$

where, $\tau_{ij}$ is the pheromone content of the path from node $i$ to node $j$. $N_i^k$ is the neighborhood includes only locations that have not been visited by ant $k$ when it is at node $i$, $\eta_{ij}$ is the desirability of node $j$, and it is a problem-dependent function to be minimized given by:

$$\eta_{ij} = \frac{1}{d_{ij}}$$

where, $d_{ij}$ is the cost of connect from $MS_i$ to $BS_j$ or $BS_i$ to $BSC_j$.

The influence of the pheromone concentration to the probability value is presented by the constant $\alpha$, while constant $\beta$ do the same for the desirability. The ants deposit pheromone on the locations they visited according to the relation.

$$\tau_{ij}^{new} = \tau_{ij}^{current} + \Delta \tau_{ij}^k$$

where $\Delta \tau_{ij}^k$ is the amount of pheromone that $Ant_k$ exudes to the node $j$ when it is going from node $i$ to node $j$.

This additional amount of pheromone is defined by:

$$\Delta \tau_{ij}^k = \frac{1}{(cost_{connect_{ij}} + cost_{install_{ij}} + cost_{upgrade_{ij}} + cost_{setup_{ij}})}$$

The cost function for the $Ant_k$ by the formula (1). This algorithm will terminate either when the maximum number of iterations is reached or an acceptable solution is found.

3.3. Our Algorithm

The pseudo-code of ACO algorithm to solving MOOCE as follows:

<table>
<thead>
<tr>
<th>ACO ALGORITHM</th>
</tr>
</thead>
<tbody>
<tr>
<td>INITIALIZATION:</td>
</tr>
<tr>
<td>Algorithm parameters: $\alpha, \beta$</td>
</tr>
<tr>
<td>Ant populationsize: $K$.</td>
</tr>
</tbody>
</table>
ACO Algorithm Applied to Multi-Objectives Optimization of Capacity Expansion in Next Generation Wireless Network

Maximum number of iteration: $N_{Max}$.

**GENERATION:**
- Generating the pheromone matrix for the Ant $k$.
- Update the pheromone values and set $x^* = k$;
- $i = 1$.

**REPEAT**
- FOR $k = 1$ TO $K$
  - Computing the cost function for the ant $k$ by the formula (1)
  - Computing probability move of ant individual by the formula (13)
  - IF $f(k) < f(x^*)$ THEN
    - Update the pheromone values by the formula (15)
    - Set $x^* = k$.
  ENDIF
- ENDFOR
- UNTIL $i > N_{Max}$

4. Experiments and Results

4.1. The problems tackled

In our experiments, we have tackled several MOOCE instances of different difficulty levels. There are 10 MOOCE instances with values for $M$, $N$ and $P$ shown in Table 2.

<table>
<thead>
<tr>
<th>Problem #</th>
<th>Mobile Users $(M)$</th>
<th>Base Stations</th>
<th>Base Stations Controllers</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>$N$</td>
<td>$N_1$</td>
</tr>
<tr>
<td>1.</td>
<td>10</td>
<td>4</td>
<td>3</td>
</tr>
<tr>
<td>2.</td>
<td>20</td>
<td>5</td>
<td>3</td>
</tr>
<tr>
<td>3.</td>
<td><strong>30</strong></td>
<td><strong>6</strong></td>
<td><strong>3</strong></td>
</tr>
<tr>
<td>4.</td>
<td>40</td>
<td>7</td>
<td>3</td>
</tr>
<tr>
<td>5.</td>
<td>50</td>
<td>10</td>
<td>6</td>
</tr>
<tr>
<td>6.</td>
<td>60</td>
<td>15</td>
<td>10</td>
</tr>
<tr>
<td>7.</td>
<td>70</td>
<td>15</td>
<td>8</td>
</tr>
<tr>
<td>8.</td>
<td>80</td>
<td>20</td>
<td>10</td>
</tr>
<tr>
<td>9.</td>
<td>90</td>
<td>25</td>
<td>15</td>
</tr>
<tr>
<td>10.</td>
<td>150</td>
<td>40</td>
<td>20</td>
</tr>
</tbody>
</table>

4.2. Parameters for the ACO algorithm

We have already defined parameters for the ACO algorithm shown in Table 3:

<table>
<thead>
<tr>
<th>Ant Population size</th>
<th>$K = 100$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Maximum number of interaction</td>
<td>$N_{Max} = 500$</td>
</tr>
<tr>
<td>Parameter</td>
<td>$\alpha=1$, $\beta=10$</td>
</tr>
</tbody>
</table>
4.3. Numerical Analysis

We evaluate the performance of our algorithms to optimize capacity expansion with multi-objectives. The experiment was conducted on Genuine Intel® CPU DuoCore 3.0 GHz, 2 GB of RAM machine. We ran the experiment ACO algorithm implemented using C language. The experimental results of our algorithm shown in Fig.6 and Fig.7.

![Fig.6](image1)

Fig.6. The results obtained in the MOOC instances tackle.

![Fig.7](image2)

Fig.7. Time processing MOOC instances tackle.

The results show that problems with the small number of $M$, $N$, $P$ such as problem #1, #2, #3, #4 and #5, algorithm has approximate optimal results fast with small interactions. However, when the problem size is large, the optimal results may be slower such as problem #6, #7, #8, #9 and #10. Convergence speed is not the same and depend on the distribution of parameters data.

Fig.8 show an existing initial assignment of problem #4. In which, BSC2, BSC4 are existing BSCs; BSC1, BSC3 are potential BSCs; BS3, BS4, BS6 are existing BSs; BS1, BS2, BS5 are potential BSs. MS6, MS29,
ACO Algorithm Applied to Multi-Objectives Optimization of Capacity Expansion in Next Generation Wireless Network

MS16, MS22 are not connected. Fig.9 show an optimal solution with BSC2 is replaced by BSC3, BS4 is replaced by BS2 and BS5. BS1 is added and connect to BSC4. Red edges are replace connections.

From this result, we confirmed that this is a promising approach to solve this problem.

5. Conclusions

In this paper, we propose a novel ant colony optimization algorithm to solve a network topology has two levels in which mobile users are sources and both base stations and base station controllers are concentrators.
Our objective function is the total cost of concentrator connectivity, installation, connection, replacement, and capacity upgrade of infrastructure equipment. Our experiment results show that our algorithm is a promising approach to solve this problem.

Reference


