Accuracy Assessment of Similarity Measures in Collaborative Recommendations Using CF4J Framework

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Abstract—There are various libraries that facilitate the design and development of recommender systems (RSs) research in both the academia and industry. Different libraries provide a different set of functionalities based on their foundational design principles. When new algorithms are proposed, researchers need to compare these against prior algorithms considering many challenges such as reproducibility of results, evaluation metrics, test harnesses, etc. Although many open source RS libraries exist to carry out research experiments and provide a varying degree of features such as extensibility, performance, scalability, flexibility, etc. To that end, this paper describes a recently introduced open-source RS library, Collaborative Filtering for Java (CF4J), which is specially designed for collaborative recommendations. Firstly, the brief internals of the CF4J framework are explained and it has been compared with other related libraries such as LibRec, LensKit, and Apache Mahout based on the recommendation approaches and evaluation tools. Secondly, we have summarized all the state-of-art similarity measures provided by the CF4J library. Finally, in order to determine the accuracy of these similarity measures, several experiments have been conducted using standardized benchmark datasets such as MovieLens-1M, MovieLens-10M, and MovieLens-20M. Empirically obtained results demonstrate that the Jaccard-Mean Squared Difference (JMSD) similarity measure provides better recommendation accuracy among all similarity measures.

Index Terms—Recommender Systems, Collaborative Filtering, Similarity Measures, CF4J Framework.

I. INTRODUCTION

The amount of information on the World Wide Web (or simply Web) is huge and wide. The explosive growth of information on the web frequently overwhelmed Internet users. Recommender Systems (RSs) help individuals who are not able to make decisions from the potentially overwhelming number of alternatives available on the web [1, 2]. Nowadays, most web users interact with RSs in one way or another which provides useful suggestions that may be relevant to users. Since recommendations are usually personalized, therefore, each user receives different suggestions from others. Traditionally, RSs are classified into following broad categories based on the filtering algorithm.

- Content-based: The system recommends items that are similar to the ones that user liked in the past [3, 4].
- Collaborative Filtering-based: The system recommends items that other users with similar tastes linked in the past [5, 6].
- Hybrid: These systems combine content-based and collaborative techniques [7, 8].

Among various recommendation approaches, collaborative filtering-based recommender systems (CFRS) are the most popular (due to their simplicity & efficiency) and are traditional approaches for recommendations [9, 10, 11]. CFRSs may further be classified into two classes: memory-based and model-based approaches [12]. Memory-based algorithms use the entire collection of rating data for providing recommendations in a heuristic manner [13, 14]. Model-based algorithms [15, 16, 17, 18, 19] learn a model from the rating data before providing any recommendations to users [20]. The memory-based methods also called as neighborhood-based approaches can further be categorized into two classes: user-based collaborative filtering (UBCF) and item-based collaborative filtering (IBCF). Fig. 1 shows a broad classification of collaborative filtering-based recommender systems.
Researchers have proposed a wide variety of algorithms for decades and new approaches are rapidly emerging in the RS literature. There is always a concern for comparing different approaches along with reproducible results. In order to accomplish these goals, there exist various libraries which support the development and experimentation with recommender systems. Different libraries provide a diverse set of functionalities based on their design foundations and some of them are commercial while others are open source. In this research, we have focused on open source RS libraries, particularly written in java language. Among these RS libraries, few libraries are not under active development but are available for use such as Duine[21], CoFi[22], Easyrec[23], and PREA[24]. Based on the general bibliography, following libraries are widely used for RS experimentation and are under active development: LibRec[25], Apache Mahout[26], [27], LensKit[28], and CF4J[29]. It is always beneficial to utilize RS libraries that facilitate researchers to design and implement new recommendation methods. A researcher or developer may choose an appropriate library for RS experimentation based on various constraints such as performance, efficiency, extensibility, etc.

This paper describes a recently introduced RS library, Collaborative Filtering For Java (CF4J)[29], which is specifically designed for collaborative filtering-based recommendations. The CF4J library facilitates: a) dataset loading, b) splitting the dataset into test and training data, c) complete and effortless access to intermediate or final result values, d) parallel execution framework specially designed for collaborative filtering, and e) evaluation of quality through various metrics. The CF4J framework also provides an implementation of state-of-the-art similarity measures proposed by various researchers. The contribution of this paper is as follows:

- Provides the internals and design details of the CF4J framework.
- Compares and contrasts the CF4J library with other related libraries based on recommendation methodologies and evaluation metrics.
- Summarizes all the similarity measures provided by the CF4J framework and explains how to introduce a new similarity measure using this framework.
- Evaluation of the similarity measures based on predictive accuracy measures (such as MAE/RMSE) and classification-based accuracy measures (such as precision) using standardized benchmark datasets (in movie domain).

II. PRELIMINARIES

In order to define the recommendation problem formally, we used the following notations as shown in Table 1. Primarily, there are two most important ways in which the recommendation problem can be specified systematically: the best item and top-N recommendation problem. The first formulation is to find a new item, for a particular user, which is most relevant to the user. The second formulation is to determine the top-N items, for a particular user. Basically, in order to provide the recommendation for a user, there is no need to find the actual rating values of the items which are to be recommended.

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Meaning</th>
</tr>
</thead>
<tbody>
<tr>
<td>U</td>
<td>The set of users in the system</td>
</tr>
<tr>
<td>I</td>
<td>The set of items in the system</td>
</tr>
<tr>
<td>R</td>
<td>The set of all ratings stored in the system</td>
</tr>
<tr>
<td>S</td>
<td>The set of possible values for ratings e.g., S = {1,2,3,4,5}</td>
</tr>
<tr>
<td>( r_{ui} )</td>
<td>The rating given by a user u ∈ U to a particular item i</td>
</tr>
<tr>
<td>( I_u )</td>
<td>The subset of items that have been rated by a user u</td>
</tr>
<tr>
<td>( U_i )</td>
<td>The subset of users that have rated item i</td>
</tr>
<tr>
<td>( I_v )</td>
<td>The subset of items that have been rated by two users u and v (I_u(∩)I_v)</td>
</tr>
<tr>
<td>( U_{ij} )</td>
<td>The subset of users that have rated both items i and j</td>
</tr>
</tbody>
</table>

Collaborative filtering-based (CF) approaches are the most significant and traditional algorithms for recommendations [30]. These algorithms are easy to implement and provide effective recommendations, therefore, are the most popular and widely used among research communities. The fundamental idea behind these approaches is that the information related to the past behaviors or interests of users are exploited and then utilized for suggesting items to the users. The CF techniques consider the basic assumptions that if users had shown the same interests in the past then they will have similar interests in the future too and user’s preferences remain constant and consistent with respect to the time.

Usually, the process of the neighborhood-based collaborative recommendation consists of the following steps [31], i.e. for an active user(u), for whom we want to predict the rating(\( r_{ui} \)) for a new item(i):

1. Calculate the similarity of all users with the active user u.
2. Select a subset of users most similar to the active user (k nearest neighbors).
3) Compute the prediction, \( r_{ui} \), by using the ratings of the \( k \) nearest neighbors.

Based on the application domain, the above steps may overlap or their order may be different [32]. It is noteworthy to understand that measuring similarities between users or items is the core component of the neighborhood-based collaborative recommendations. Therefore, this paper examines and evaluates the accuracy of the various similarity measures using standardized benchmark datasets.

A. Uncovering CF4J Framework

CF4J stands for Collaborative Filtering for Java. It is a java library specially designed to perform experiments in recommender system research or particularly in collaborative filtering-based recommendations. CF4J has been designed with a motive “a library developed from researchers to researchers” i.e. it is especially suited for the experimentation and research trials of new recommendation algorithms. The library is available from well-known java repositories such as Maven, Gradle, and SBT. Furthermore, the proper documentation of the library makes its usage smooth.

A1. Design of CF4J

Based on the various steps involved in a collaborative recommender system, the CF4J library has been designed according to the package structure shown in Fig. 2. It provides all the functionalities which are required by CF researchers such as data loading, train/test data splitting, etc. Table 2 summarizes the core functionalities provided by each package/subpackage.

A2. Core APIs

The most fundamental classes are User, Item, Kernel, and Processor. Kernel class handles all the data associated with the recommendation process i.e. it loads the rating data and builds a data model for manipulating rating values. Processor class enables to execute an intermediate step of the collaborative recommendation process to be parallelized. User class provides an abstraction to represent a user and accommodates information related to the user of the recommender system. Similarly, Item class abstracts an item and contains the information associated with the item. Fig. 3 represents the functionalities provided by (a) User class (b) Item class.

![Fig.2. The package structure of the CF4J library.](image)

Table 2. The core functionalities provided by CF4J library

<table>
<thead>
<tr>
<th>Package/sub package Name</th>
<th>Core functionalities</th>
</tr>
</thead>
<tbody>
<tr>
<td>cf4j</td>
<td>It consists of the indispensable classes of the library.</td>
</tr>
<tr>
<td>cf4j.knn</td>
<td>It contains the implementation of the various components of the k-nearest neighbor methods such as similarity measures, aggregation approaches, etc.</td>
</tr>
<tr>
<td>cf4j.model</td>
<td>It includes a matrix factorization-based collaborative filtering technique.</td>
</tr>
<tr>
<td>cf4j.qualityMeasures</td>
<td>It includes the implementation of various quality measures.</td>
</tr>
<tr>
<td>cf4j.utils</td>
<td>It contains various utilities used by the library.</td>
</tr>
</tbody>
</table>

For illustration purpose, the basic steps involved in a typical user-based collaborative filtering (UBCF) are shown in Fig. 4 where the similarity between users is calculated using the traditional Pearson Correlation Coefficient, neighbors’ ratings are aggregated using deviation from the mean approach, and the recommendation quality is evaluated using the mean absolute error (MAE) metric.
III. RELATED FRAMEWORKS

There are many possible ways in which one can compare different programming libraries which are developed to accomplish the same or similar tasks. Different researchers prioritize different goals based on the requirements such as ease of use, popularity, support and documentation, performance, extensibility, etc. Here, we have discussed only those RS libraries that are developed using Java technology and are popularly used in the RS literature. Furthermore, there are few libraries that are under active development nowadays while others are outdated but still available for experimentation and usage. Table 3 lists the RS libraries that are not under active development presently but may be utilized for various RS research tasks specific to them.

Based on the general bibliography in the RS research, the following libraries are widely used for the RS experimentation and are under active development:

(a) Duine [33]
(b) Cofi [22]
(c) Easyrec [34]
(d) PREA [24]

Table 3. The recommendation toolkits that are not under active development currently

<table>
<thead>
<tr>
<th>Baseline Approaches</th>
<th>Duine [33]</th>
<th>Cofi [22]</th>
<th>Easyrec [34]</th>
<th>PREA [24]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Memory-based CF</td>
<td>Constant</td>
<td>Memory-based CF</td>
<td>Memory-based CF</td>
<td>Memory-based CF</td>
</tr>
<tr>
<td>User-based CF</td>
<td>User Average</td>
<td>User-based CF</td>
<td>User-based CF</td>
<td>User-based CF</td>
</tr>
<tr>
<td>Item-based CF</td>
<td>Constant</td>
<td>Item-based CF</td>
<td>Item-based CF</td>
<td>Item-based CF</td>
</tr>
<tr>
<td>Model-based</td>
<td></td>
<td>Model-based</td>
<td>Model-based</td>
<td>Model-based</td>
</tr>
<tr>
<td>nil</td>
<td></td>
<td>nil</td>
<td>SVD</td>
<td>SVD</td>
</tr>
<tr>
<td>Other Methods</td>
<td>Case-based reasoning</td>
<td>Simple content-based</td>
<td>-</td>
<td>Rank-based CF</td>
</tr>
<tr>
<td>Evaluation Metrics</td>
<td>MAE</td>
<td>MAE</td>
<td>On-line evaluation</td>
<td>MAE, RMSE</td>
</tr>
<tr>
<td>Other Features</td>
<td>Explanation APIs</td>
<td>Provides wrappers for other languages</td>
<td>Easy to integrate and easy usage.</td>
<td>Provides wrappers for other languages</td>
</tr>
</tbody>
</table>
Except for the LibRec framework, the remaining frameworks primarily focus only on the collaborative filtering-based recommendation approaches while the LibRec framework provides support for various different RS approaches. Table 4 summarizes the various recommendation approaches and evaluation metrics provided by these libraries. Since this article evaluates the accuracy of various similarity measures available in the CF4J framework, therefore, we have listed the similarity measures provided by each framework in Table 5.

IV. SIMILARITY MEASURES

Neighborhood-based collaborative filtering employs various measures of similarity for discovering the neighborhood of an active user or item. This section briefly summarizes all the similarity measures which are provided by the CF4J framework. Here, we have used the same notations as explained in the earlier section.

A. Pearson Correlation Coefficient (PCC)

It displays the linear relationship between the rating vectors and demonstrates the degree to which two rating vectors are linearly related. Its value lies between -1 to +1; where the value +1 shows complete +ve linear correlation, 0 shows no linear correlation and -1 is complete -ve linear correlation [37,38].

\[
PCC(u,v) = \frac{\sum_{i \in I_u} (r_{ui} - \bar{r}_u)(r_{vi} - \bar{r}_v)}{\sqrt{\sum_{i \in I_u} (r_{ui} - \bar{r}_u)^2 \sum_{i \in I_v} (r_{vi} - \bar{r}_v)^2}}
\]  

(1)

B. Constrained Pearson Correlation Coefficient (CPCC)

It modifies the traditional PCC by using the median value (of the rating scale) in place of average rating. This variant keeps in mind the positivity and negativity of the ratings [6].

\[
CPCC(u,v) = \frac{\sum_{i \in I_u} (r_{ui} - \bar{r}_{med})(r_{vi} - \bar{r}_{med})}{\sqrt{\sum_{i \in I_u} (r_{ui} - \bar{r}_{med})^2 \sum_{i \in I_v} (r_{vi} - \bar{r}_{med})^2}}
\]

(2)

where r_{med} is the median value of the rating scale.

C. Cosine Similarity (COS)

It measures the cosine of the angle between the rating vectors, smaller angle means greater similarity [12].

\[
COS(u,v) = \frac{\sum_{i \in I_u} (r_{ui})(r_{vi})}{\sqrt{\sum_{i \in I_u} (r_{ui})^2 \sum_{i \in I_v} (r_{vi})^2}}
\]

(3)

D. Adjusted Cosine Similarity (ACOS)

It modifies the traditional PCC measure for computing similarities between items so that the differences between individual users can be taken into account. This measure used to calculate the similarity between items but can be analogously used for measuring the similarities between users.

\[
PCC(i,j) = \frac{\sum_{u \in U_{ij}} (r_{ui} - \bar{r}_i)(r_{uj} - \bar{r}_j)}{\sqrt{\sum_{u \in U_{ij}} (r_{ui} - \bar{r}_i)^2 \sum_{u \in U_{ij}} (r_{uj} - \bar{r}_j)^2}}
\]

(4)

Equation (4) measure the traditional PCC between two items i and j, where U_{ij} represents the set of users who have rated both the items i and j. The Adjusted Cosine Similarity (ACOS) [39] modifies (4) to incorporate the individual differences between users, therefore, can be defined by (5) as given below:
of rank correlation. Spearman’s correlation assesses monotonic relationships between the two observations. It returns value from -1 to 1; where 1 shows a perfect +ve correlation between ranks, 0 shows no correlation and -1 is perfect -ve correlation between the ranks [46]. It is also called Spearman’s rho and denoted by the Greek letter ρ (rho) or r_s.

\[
ACOS(i, j) = \frac{\sum_{u \in U} (r_{ui} - \bar{r}_u)(r_{uj} - \bar{r}_u)}{\sqrt{\sum_{u \in U} (r_{ui} - \bar{r}_u)^2 \sum_{u \in U} (r_{uj} - \bar{r}_u)^2}}
\] (5)

### E. Spearman’s Rank Correlation Coefficient (SRCC)

It adopts the traditional PCC over the rank values of the two variables, therefore, is a nonparametric measure.
If all the ranks are distinct, then it can be measured using (6) as given below:

\[ \rho = 1 - \frac{6 \sum d_i^2}{n(n^2-1)} \]  

(6)

Where \( n \) is the number of observations and \( d_i \) is the difference between the two ranks of the \( i \)-th observation. In the RS scenario, (6) may be rewritten as follow:

\[ SRCC(u,v) = 1 - \frac{6 \sum (r_{ui} - r_{vi})^2}{|I_u| \times (|I_u|^2 - 1)} \]  

(7)

F. Jaccard Index (J)

It is the ratio of the size of intersection divided by the size of the union. Likewise, the similarity between any two users, \( u \) and \( v \), may be defined as the proportion of the commonly rated items to the total items rated by two users [40].

\[ J(u,v) = \frac{|I_u \cap I_v|}{|I_u \cup I_v|} \]  

(8)

G. Mean Squared Difference (MSD)

It is the arithmetic mean of the squares of differences between corresponding values of the two rating vectors. For example, consider two vectors, \( x \) and \( y \) each of size \( n \), MSD(x,y) will be equal to \( \frac{1}{n} \sum_{i=1}^{n} (x_i - y_i)^2 \) [6]. The similarity based on MSD can be defined as \( \{1 - MSD(x,y) \} \) since the MSD measures the differences between the two vectors. Therefore, the similarity between any two users, \( u \) and \( v \), may be defined as follows:

\[ MSD(u,v) = 1 - \frac{\sum_{i \in I_u} (r_{ui} - r_{vi})^2}{|I_u|} \]  

(9)

H. Jaccard Mean Squared Difference (JMSD)

This measure combines the Jaccard similarity with MSD similarity to define a new hybrid similarity measure known as JMSD [41].

\[ JMSD(u,v) = jaccard(u,v) \times MSD(u,v) \]  

(10)

I. Coverage-Jaccard-Mean Squared Difference (CJMSD)

This measure modifies the JMSD measure by adding a term corresponding to the coverage that a user \( u \) can provide to another user \( v \), i.e. Coverage \( u \rightarrow v = \frac{|I_u - I_v|}{|I|} \).

Clearly, this similarity measure is asymmetric as Coverage \( u \rightarrow v \neq \text{Coverage} \( v \rightarrow u \) and hence the similarity between two users, \( u \) and \( v \), CJMSD(u,v) \( \neq \text{CJMSD}(v,u) \) [42].

\[ CJMSD(u,v) = \frac{|I_u - I_v|}{|I|} \times jaccard(u,v) \times MSD(u,v) \]  

(11)

J. Singularity-based similarity (SING)

To calculate the similarity between two users, the commonly rated items are divided into three subgroups:

- Items rated relevant by both the users
- Items rated non-relevant by both the users
- Items rated as relevant by one user and non-relevant by the other user

For each commonly rated item, singularity concerned with the relevant and non-relevant vote is calculated using all the users in the database. Finally, a traditional similarity measure is modulated by the value of the singularity over three subsets of the commonly rated items. Here, the authors utilize MSD as a traditional numerical similarity measure [43].

K. Proximity-Impact-Popularity measure (PIP)

It considers the three factors of similarity, Proximity, Impact, and Popularity for defining the overall similarity (SIM) between two users \( u \) and \( v \) [44].

\[ PIP(u,v) = \sum_{i \in I_u} PIP(r_{ui}, r_{vi}) \]  

(12)

where, PIP \( (r_{ui}, r_{vi}) \) is the PIP score for the two rating values. Further, the PIP score for any two ratings \( r_1 \) and \( r_2 \) is defined as follows:

\[ PIP(r_1, r_2) = \text{Proximity}(r_1, r_2) \times \text{Impact}(r_1, r_2) \times \text{Popularity}(r_1, r_2) \]  

(13)

where Proximity denotes the simple arithmetic difference between two ratings, Impact measures the strength by which an item is liked or disliked by the users, and Popularity denotes the degree to which two users’ ratings are common.

In all the equations from (1) to (13), all the formulae are written for calculating the similarity between users while analogous formulae can be easily written for calculating similarities between items.

L. Illustrative Example

Here, we will demonstrate a representative procedure for introducing a new similarity measure using a toy example in CF4J framework. CF4J contains several abstract classes and interfaces to provide excellent extensibility. For implementing new similarity measures, researchers may use the abstract classes, UsersSimilarities & ItemsSimilarities. Let’s define an imaginary similarity between two users as the absolute difference of their ratings’ averages, then we will encode as shown in Fig. 5.
public class ToySimilarity extends UserSimilarities {

@Override
public double similarity(User activeUser, User targetUser) {
    double a = activeUser.getRatingAverage();
    double t = targetUser.getRatingAverage();
    return Math.abs(a - t);
}
}

Fig 5. Illustrative example code for implementing a new dummy similarity measure between two users.

V. EXPERIMENTS

The offline experiments are the easiest to conduct as they require no interaction with real users. Therefore, offline experiments are the most popular and accepted way to evaluate the candidate recommendation approaches in comparison to user studies or online experiments [48].

We have performed offline experiments to evaluate the accuracy of various similarity measures available in the CF4J library. All the experiments are performed using standardized benchmark rating datasets (MovieLens-1M, 10M, and 20M), which is publicly available from GroupLens research [49]. Table 6 summarizes these datasets briefly, article [50] explains the detailed history and context of MovieLens datasets.

<table>
<thead>
<tr>
<th>Dataset</th>
<th>Brief Detail</th>
<th>Sparsity Level</th>
</tr>
</thead>
<tbody>
<tr>
<td>MovieLens-1M</td>
<td>• 1000,209 ratings from 6040 users on 3900 movies</td>
<td>1 - 1000,209</td>
</tr>
<tr>
<td></td>
<td>• Each user has rated at least 20 movies.</td>
<td>6040 * 3900</td>
</tr>
<tr>
<td>MovieLens-10M</td>
<td>• 10,000,054 ratings from 71567 users on 10681 movies</td>
<td>1 - 10000054</td>
</tr>
<tr>
<td></td>
<td>• Each user has rated at least 20 movies.</td>
<td>71567 * 10681</td>
</tr>
<tr>
<td>MovieLens-20M</td>
<td>• 20,000,263 ratings from 7138493 users on 27278 movies</td>
<td>1 - 20000263</td>
</tr>
<tr>
<td></td>
<td>• Each user has rated at least 20 movies.</td>
<td>138493 * 27278</td>
</tr>
</tbody>
</table>

Table 6. Brief description MovieLens datasets

A. Experimental Design

To evaluate the performance of various similarity measures, we have employed the user-based collaborative filtering (UBCF) with the k-nearest-neighbors (kNN) technique. The neighbors’ ratings are aggregated using deviation from the mean strategy. All the experiments are performed using the system/software configurations as specified in Table 7.

<table>
<thead>
<tr>
<th>High Performance Computing System</th>
<th>Intel(R) Xenon(R) Gold 6132(Skylake) 14 cores <a href="mailto:CPU@2.6GHz">CPU@2.6GHz</a> with 96GB RAM</th>
</tr>
</thead>
<tbody>
<tr>
<td>Operating System</td>
<td>Windows 10 pro</td>
</tr>
<tr>
<td>Eclipse IDE for Java EE</td>
<td>4.7.2 or higher</td>
</tr>
<tr>
<td>Java Runtime Environment (JRE)</td>
<td>Java 1.8</td>
</tr>
<tr>
<td>CF4J library version</td>
<td>1.1.1 or higher</td>
</tr>
</tbody>
</table>

Table 7. The details of the software and system used for experiments

B. Evaluation Metrics

One of the most crucial measure for evaluating the recommender systems is accuracy i.e. their capability to predict users’ choice accurately [51]. In the RS literature, accuracy is the most examined goal for designing a recommender system. The fundamental hypothesis is that if an RS predicts users’ preferences accurately then it will be preferred by users. Furthermore, the accuracy measure is not dependent on the user interface of the recommender system, therefore offline experiments are well suited for measuring the accuracy of an RS approaches with datasets from multiple domains. Here, we evaluated the following two types of accuracy measures:

- the accuracy of rating predictions
- the accuracy of usage predictions

B.1. Measuring the accuracy of rating predictions

Let R be the set of all ratings stored in the system i.e. rating matrix, and it is known that a user u has rated an item i with the rating value $r_{ui}$, also a recommendation algorithm predicts this rating as $\hat{r}_{ui}$. Therefore, we can calculate the error of estimation for this particular rating as $e_{ui} = \hat{r}_{ui} - r_{ui}$. There are various ways to compute the overall error for a system for a given test set T of user-item pairs (u, i) such as Mean Absolute Error(MAE), Root Mean Squared Error(RMSE), Normalized MAE (NMAE), Normalized RMSE (NRMSE), Average MAE and Average RMSE. Again, the following two metrics are the most popular among the research community for evaluating the accuracy of the rating prediction:

\[
RMSE = \sqrt{\frac{1}{|T|} \sum_{(u,i) \in T} (\hat{r}_{ui} - r_{ui})^2} \tag{14}
\]
\[ MAE = \sqrt{\frac{1}{|T|} \sum_{(u,i) \in T} |(\hat{r}_{ui} - r_{ui})|} \]  

(15)

B.2. Measuring the accuracy of usage predictions

Many recommender systems do not estimate the actual ratings of items rather try to suggest a set of items (top-N) that may be useful for the users. In order to calculate the accuracy of usage predictions in the offline experiments, we hide some of the items selected by a test user (i.e. purchased or browsed items via implicit feedback) and then predict a set of items that the user will select. The following four cases arise [52], as shown in Table 8.

Table 8. All four possible outcomes of the recommendation process.

<table>
<thead>
<tr>
<th></th>
<th>Recommended</th>
<th>Not recommended</th>
</tr>
</thead>
<tbody>
<tr>
<td>Preferred</td>
<td>True-Positive(tp)</td>
<td>False-Negative(fn)</td>
</tr>
<tr>
<td>Not preferred</td>
<td>False-Positive(tp)</td>
<td>True-Negative(tn)</td>
</tr>
</tbody>
</table>

Based on the above four cases, the overall quality of a recommender system may be estimated using various quantities such as precision, recall, false positive rate, etc.

\[ \text{Precision} = \frac{\#tp}{\#tp + \#fp} \]  

(16)

\[ \text{Recall(True Positive Rate)} = \frac{\#tp}{\#tp + \#fn} \]  

(17)

\[ \text{False Positive Rate} = \frac{\#fp}{\#fp + \#tn} \]  

(18)

In our experiments, we have evaluated Precision at N, where N is the number of recommendations i.e. size of the recommendation list, and varying it with various values of N such as 10, 15, 20, etc. Alternatively, the precision of an RS may also be simulated as the ratio of the relevant recommended items with respect to the number of recommended items, along with defining the meaning of relevance items, for example with items with predicted rating ≥ 4 (on a scale of 1 to 5) may be considered as relevant items.

VI. RESULTS AND DISCUSSION

Table 9 lists all the similarity measures along with the corresponding API class name in the CF4J framework. For assessing the predictive accuracy, 80% of the rating data is used as training data while the remaining 20% is used as test data. Furthermore, for each test user, 20% of ratings are used for validation purpose. We have calculated the values of MAE and RMSE for all similarity measures by varying the number of neighbors. MAE and RMSE values are compared for all the similarity measures in Fig. 6 and Fig. 7 respectively for different datasets (a) MovieLens-1M (b) MovieLens-10M (c) MovieLens-20M dataset.

Table 9. The similarity measures provided by CF4J library

<table>
<thead>
<tr>
<th>Similarity Measure</th>
<th>Ref.</th>
<th>API Class name</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pearson Correlation Coefficient (PCC)</td>
<td>[37]</td>
<td>MetricCorrelation</td>
</tr>
<tr>
<td>Constrained PCC (CPCC)</td>
<td>[6]</td>
<td>MetricCorrelationConstrained</td>
</tr>
<tr>
<td>Cosine Similarity (COS)</td>
<td>[12]</td>
<td>MetricCosine</td>
</tr>
<tr>
<td>Adjusted Cosine Similarity (ACOS)</td>
<td>[39]</td>
<td>MetricAdjustedCosine</td>
</tr>
<tr>
<td>SRCC</td>
<td></td>
<td>MetricSpearmanRank</td>
</tr>
<tr>
<td>Jaccard Index (JI)</td>
<td>[40]</td>
<td>MetricJaccard</td>
</tr>
<tr>
<td>Mean Squared Difference (MSD)</td>
<td>[6]</td>
<td>MetricMSD</td>
</tr>
<tr>
<td>Jaccard Mean Squared Difference (JMSD)</td>
<td>[41]</td>
<td>MetricJMSD</td>
</tr>
<tr>
<td>Coverage-JMSD (CJMSD)</td>
<td>[42]</td>
<td>MetricCJMSD</td>
</tr>
<tr>
<td>Singularity-based similarity (SING)</td>
<td>[43]</td>
<td>MetricSingularities</td>
</tr>
<tr>
<td>Proximity-Impact-Popularity (PIP)</td>
<td>[44]</td>
<td>MetricPIP</td>
</tr>
</tbody>
</table>
The empirical results of MAE values, as shown in Fig. 6 (a)-(c), demonstrate that the JMSD measure provides better predictive accuracy than other similarity measures. It should be noted that both JMSD and PIP provide almost comparable results but for small neighborhood size, PIP measure results in better values than the JMSD measure.

Similarly, the empirically obtained values of RMSE, shown in Fig. 7(a)-(c), demonstrate that the JMSD measure provides the best results among all measures. Based on the application domain, either MAE or RMSE may be selected for evaluating the predictive accuracy[53]. One important observation, from the empirical values of MAE and RMSE, is that some of the similarity measures monotonically decrease MAE/RMSE values against the number of neighbors while other similarity measures do not display any significant changes in MAE/RMSE values after some point of the neighborhood size. Based on this observation, all the available similarity measures may be divided into two clusters, \{PCC, CPCC, COS, ACOS, MSD\} & \{SRCC, JI, JMSD, CJMSD, SING, PIP\}.

In order to assess classification-based accuracy, we have evaluated precision values by varying the size of the recommended list i.e. Precision@N and N= 5, 10, 15… etc. The metrics that are taken from the information retrieval domain such as precision, describe users’ involvement nicely in comparison to predictive accuracy measures such as MAE/RMSE[52]. Table 10 summarizes the different parameter values used for measuring precision values. Fig. 8 compares the precision values for different size of the recommended list for all three datasets (a) MovieLens-1M (b) MovieLens-10M (c) MovieLens-20M.

As shown in Fig. 8 (a)-(c), the empirically obtained values of precision demonstrate that both JMSD and PIP measures provide almost comparable results. Here again, for the small size of recommendation list (e.g. top-5 and top-10), the PIP measure results in slightly better precision values than the JMSD measure. Based on the empirical results, we believe that if online e-commerce portal demands both types of accuracy (predictive and classification-based) simultaneously then JMSD measure may result in better recommendations than other similarity measures.
Table 10. Different parameters involved in experimenting with classification-based accuracy.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>ML-1M</th>
<th>ML-10M</th>
<th>ML-20M</th>
</tr>
</thead>
<tbody>
<tr>
<td>Test-Users %</td>
<td>20%</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Test-Items %</td>
<td>20%</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Rating Threshold (β)</td>
<td>4</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Recommendation size</td>
<td>[5, 10, 15, 20]</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Neighborhood-Size</td>
<td>180</td>
<td>320</td>
<td>400</td>
</tr>
</tbody>
</table>

Fig. 8. The Precision values for (a) MovieLens-1M (b) MovieLens-10M (c) MovieLens-20M datasets

VII. CONCLUSIONS

This paper describes a recently introduced open-source java library, Collaborative Filtering for Java (CF4J), for performing RS research experiments. The brief internals of the CF4J framework are explained so that it can be utilized to carry out the implementation of new recommendation tasks such as similarity measure, evaluation metric, etc. Furthermore, the CF4J framework is also compared with the other related libraries such as LibRec, LensKit, and Apache Mahout. It also provides the implementations of the state-of-art similarity measures for collaborative recommendations. In this research, several experiments have been conducted for evaluating the accuracy of these similarity measures using standardized benchmark datasets (MovieLens-1M, 10M, and 20M). From the empirically obtained results, it is concluded that the JMSD measure provides better recommendation accuracy among all the available similarity measures.

As a summary, the CF4J framework provides a simple way to conduct RS experiments with a unique parallel execution framework specially designed for collaborative recommendations. It provides excellent flexibility for accessing any intermediate value and is expendable for new implementations proposed by researchers. For the future work, this framework can be expanded into multiple dimensions such as implementing new recommendation approaches, evaluation methods, new similarity measures, etc.
REFERENCES


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