

A Concave Hull Based Algorithm for Object Shape Reconstruction

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Abstract-Hull algorithms are the most efficient and closest methods to be redesigned for connecting vertices for geometric shape reconstruction. The vertices are the input points representing the original object shape. Our objective is to reconstruct the shape and edges but with no information on any pattern, it is challenging to reconstruct the lines to resemble the original shape. By comparing our results to recent concave hull based algorithms, two performance measures were conducted to evaluate the accuracy and time complexity of the proposed method. Besides achieving the most acceptable accuracy which is 100%, the time complexity of the proposed algorithm is evaluated to be O(wn). All results have shown a competitive and more effective algorithm compared to the most efficient similar ones. The algorithm is shown to be able to solve the problems of vertices connection in an efficient way by devising a new approach.

Index Terms—Convex hull, concave hull, vertices, shape reconstruction.

I. INTRODUCTION

Many approaches are given to solve the problem of polygon computing to approximate geometric shapes based on a given point set in \mathbb{R}^2 . Various methods are designed specifically based on the nature of the output [1]. The objective of this research, is to connect the points or vertices from the identified object faces that contain disordered vertices of (x, y). One of the challenging tasks is to know which vertices to connect together as we have no connectivity information. Typically, a line is drawn from each vertex to every other remaining vertex to form a polygon such as the OpenGL_Line ready function. However, this does not allow the recognition of the real object as can be seen in Figure 1. The main objective of the proposed method in this paper is to imitate the source drawing and reconstruct the shape. Given a set of points

(vertices) from two faces representing the dominant shape of the object, the goal is to connect them "connect-thedots" by finding the correct path to produce a "meaningful' object. The most relevant studies that could address this issue are the ones done on hull computation. Numerous algorithms were developed and improved over the years to address the problem of hull computation and detection [2]–[5]. The algorithm starts with the convex hull computation and several works developed from this process are still considered as state of the art. The strategies to solve the problem in this paper are taken as a basis on how to handle convex and non-convex objects.



Fig.1. A connection on (a) a sample object of our dataset, (b) vertices of the object and (c), Line drawing between points in OpenGL.

The computations of convex and concave hulls on the set of points in two-dimensional planes are still a challenge in many different areas. They have been widely used in many fields such as computer graphics, image processing, GIS, wireless tracking, pattern recognition and artificial intelligence. It is important to understand that numerous algorithms are designed based on very different needs. The construction of hull from a given set of points is used to detect convexity or concavity as can be seen in Figure 2. The convex hull of a point-set is the smallest convex space that contains all the points belonging to that set. For a finite 2D point-set, the convex hull can be defined as the smallest convex polygon containing all the points. Meanwhile, concave hull is described when the hull around one set of group of objects is not required to have a convex shape. The shape defined allows any angle between the points. Convex hulls have several useful properties that can be suitable for a variation of recognition and representation tasks. A convex hull can also be defined when the shape that contains all the points does not have any angle that exceeds 180 degrees between two adjacent points.



Fig.2. Classification of convex and concave hull. Adapted from [6]

Graham's scan algorithm [4] for computing the convex hull is used as a basic idea for connecting set of points in a plane. The result of convex hull construction using Graham's Scan shows that the enumeration is to extract the extrapolation or the image boundary. The algorithm does not enumerate points with same x or y value and neglects the inner points. Figure 3 shows several results for using Graham's Scan Algorithm. As seen in the figure, the convex hull technique does not reflect the original shape which mostly has a dataset of concave objects. Thus, concave hull is a better choice and is more advanced to capture the concaveness of the shape of the object [7].



Fig.3. Graham's Scan based on convex hull rules of our datasets



Fig.4. The smoothness of concave hull determined by threshold [7]

Concave hull computation is an active field in computation geometry with different approaches to compute the boundaries from point sets of the arbitrary shape. There are many known algorithms for computing convex hull but very few for computing concave hulls. The techniques used to compute concave hulls are based on nearest neighbor, kernel functions, using a convex hull or Delaunay triangulation. A prominent algorithm for concave hull computation is to construct non-convex or simple polygons that characterize the shape from a set of points in the plane. It is based on the Delaunay triangulation of the points. The method first creates a convex Delaunay triangulation with the entire vertex connecting each other. Then, the algorithm removes the edges that are smaller than a certain threshold value, but still does not give any expected results. However, it is not applicable in our work because the algorithm still connects the most outer points. The smoothness of the shape is based on the 'digging method' and threshold value in order to produce the appropriate depth as shown in Figure 4. In conclusion, we abandoned the convex hull approach because it cannot preserve the original object shape.

The challenge in this work is of how to re-implement hull based algorithms to utilize the concavity to reconstruct an object shape. While any convex and concave hull approach ignores some points, our work inspects all points for a given object to be connected. By comparing and analyzing the time complexity of the previous algorithms we have realized the issue of high time complexity. In this study, a technique for object shape reconstruction is proposed by utilizing a 'splitting and recombination' approach to correctly connect the vertices which also affects the detection of the object shape. We have emphasized on a design to decrease the time complexity in comparison with the best options. Point and vertex is used interchangeably throughout this paper.

This paper is organized as follows: section 2 presents the related works. Section 3 describes the concave Hull based algorithm developed for object shape reconstruction. Section 4 introduces the implementation undertaken. Section 5 presents some examples of the obtained results, and discusses performance evaluation of the implemented algorithm. Section 6 concludes with some remarks and future work.

II. RELATED WORKS

Computing a set of points in a plane to represent a shape has arisen in the computer vision and computer graphics domain. It has been used to solve several problems in pattern recognition, control theory, machine learning, computational graphics, and structural health monitoring and also signal classification. A shape recognized from a set of points can easily be perceived by a human brain, but the recognition is difficult for a computer. Before related works are presented, it is important to define the ideas about terminologies and the difference of opinion. There are several hulls, however we reviewed the concave hull category due to their wide and various range of utilization.

Several methods are exploited to compute a shape or boundary from arbitrary set of points. The main idea behind the concave hull computation is based on the nearest neighbor techniques, kernel functions or convex hull, and its Delaunay triangulation [8]. A well-known concave hull algorithms proposed by Edelsbrunnern et al. [9] is defined as α – shapes obtained from Delaunay triangulation that represent a set S of n points in the plane parameterized by α . For a finite set of points, the α – hull approaches the generalization of convex hull. A related notion, \mathcal{A} –shape of the set of points P constructed from Voronoi diagrams is proposed by Melkemi & Djebali [10]. This algorithm is presented for only 2D and could be extended for 3D. By composing the Voronoi diagram for $\mathcal{A} \cup P$ where \mathcal{A} is an arbitrary finite points set, we also join pair points $p, q \in P$ and thus define the \mathcal{A} – shape of P. The pair points p, q would only be considered if in addition to these cells bordering each other, they also border some common Voronoi cells that contain a point of \mathcal{A} .

Galton & Duckham [1] proposed a non-convex hull algorithm to characterize the boundary of a finite input set in the plane based on Delaunay triangulation of the points. These boundaries are commonly derived using either polygon or hull-based methods or statistical techniques. Also called non-convex footprint is implemented in GIS for footprint delineating the area occupied by a set of points and is extended in the work of Moreira & Santos [11]. The algorithm requires $O(n^3)$ time to execute.

Moreira & Santos [11] proposed an algorithm based on Jarvis march to compute the boundary of points set in 2D. It employs a k – th nearest neighbor, and angles properties which are depending on the previous computed point. The algorithm can work with most of the scenario. However, in some cases it produces boundaries that do not contain all the samples in the dataset. Thus, preprocessing is needed to remove outliers in order to produce an accurate result.

Duckham et al. [12] proposed a technique called x - algorithm to generate a characteristic hull-based method. They applied this method for boundaries shaping the countries and also alphabet letters using datasets of known distribution. The x - shape algorithm is based on Delaunay triangle which receives dot patterns as input and produces a polygon as an output. A length parameter l is introduced between the shortest and longest boundary edges. No digging can occur when the l is longer than the longest boundary edge. The concavity degrees rise when the edge is shorter than the shortest boundary edge. This method is to delineate the polygonal regions as an alternative to a minimum convex polygon (MCP) and is considered as one of the time-efficient concave hull algorithms with a time complexity of $O(n \log n)$ [13].

Another approach for concave hull method is a method starting with convex hull followed by 'a digging' method which is presented by Park & Oh [7]. The algorithm first starts with the concave list from the concave point and the 'dig' process is based on the list in order to find the nearest point. This study also includes the evaluation criteria for convex and concave hull algorithms. It has a time complexity of $O(n \log n + n)$, where it takes n computations longer than the Duckham algorithm in all times. The algorithm also uses a threshold parameter p to determine an occurrence of the digging process that may result to convex or concave. The authors also suggested that the lower threshold value will result to a more concave hull, whereas a higher threshold value results to convex hull. However, their algorithm never entirely

captures the actual shapes of the datasets as the digging only occurs on the shorter edges. By digging at the long edges the algorithm would have a more close simulation of finding the desired shape but still it will not be able to. Methirumangalath et al. [14] proposed an unified algorithm to compute geometric shape by a given set of point S in \mathbb{R}^2 . The algorithm is based on Delaunay triangle and is capable to deal with many prominent features such as sharp corners, concavities and thin regions. However, the algorithm requires parameter tuning for boundary detection if the input point is very sparse. Additionally, it also suffers dealing with noise input like other approaches that use Delaunay triangle in their algorithm. Table 1 refers to different concave hull algorithms and their time complexity.

Table 1. A time complexity comparison of concave hull algorithms

Algorithms	Time complexity		
Galton & Duckham [1]	$O(n^3)$		
Moreira & Santos [11]	$O(n^3)$		
Duckham et al. [12]	$O(n \log n)$		
Park & Oh [7]	$O(n\log n + n)$		
Methirumangalath et al. [14]	$O(n \log n)$		

III. THE PROPOSED METHODS

The aim of the algorithm is to create edges or connect unorganized vertices in each face (f_1) and (f_2) and between the two faces in order to define the original shape. Figure 5 shows a set of vertices of an object comprising of two faces that provides no connection information. Each face is a representative of a side of a symmetric object.



Fig.5. Two-dimensional vertices represents an object: (a) object vertices, (b) vertices of face 1 (f_1) and (c) vertices of face 2 (f_2)

The proposed approach is based on the points or vertices which are elements of \mathbb{R}_2 in the plane. The first step is to determine the Seed Point SP as the connection determinant for the initial and subsequent vertices construction. The second step is region splitting which is to divide the faces into two parts based on the centroid of the face vertices. In the third step, the vertices in each region are connected and complete face connection is completed in the fourth step where the edges are added between faces. The procedure used in this algorithm is illustrated in the flow shown in Figure 6.



Fig.6. The procedure of the proposed method

A. Seed Point Identification

This is the first stage where certain elements are determined for accurate shape identification. Based on our method, each face must be divided into two regions which are referred as the upper region (r_1) and the lower region (r_2) based on the centroid of the face vertices. The Seed Point (SP) is a starting point for connecting vertices and needs to be declared beforehand. If a wrong seed point is selected, it may result in misconnecting and thus produce the wrong shape. To determine the SP, a minimum x value is initialized and is resided in the first index of the upper region (r_1) , meaning that the regions would change to include the seed point at the upper region (r_1) automatically. Later, the remaining vertices are computed for the region division. Figure 7 shows the seed point being dedicated to the upper region and the region classification represented in equation (1).

$$f(SP) = x_min(v_i) \Vdash r_1 \tag{1}$$



Fig.7. (a) The original location of seed point in (r_2) (b) Seed point (sp) being dedicated to the upper region (r_1)

B. Region Splitting

There are two sets: face f_1 and f_2 containing all the vertices $v_1, v_2, ..., v_n$ corresponding to the object which is also expressed in equation (2). The algorithm is to find the upper region (r_1) and lower region (r_2) based on the remaining vertices after seed point has been identified. Later these two regions are merged together in order to have complete connection in the object face.

$$v = \sum_{i=1}^{n} w_i v_i, \tag{2}$$

where
$$w_i \in \mathbb{R}, w_i \ge 0$$
 for each $i \in [n]$, and $\sum_{i=1}^n w_i = 1$

For every face, two regions are partitioned based on the centroid of y - axis or x - axis. In equation (3) we show that the remaining vertices which are less than \overline{Y} (also same for \overline{X}) are assigned to r_1 and the rest are kept in r_2 . The centroid of vertices in respect to \overline{Y} are accumulated in the second equation of (3). The y-values of the vertices, yi for $0 \le i < n$, are used to split the region into horizontal strips while x-values in vertical strips. Figure 8 illustrates the visualization of the object face with the division of two regions.

$$f(r) = \begin{cases} v_i + 1 \in r_1, & if(v_{i+1}(y) \le \bar{Y}) \\ v_i + 1 \in r_2, & else & if(v_{i+1}(y) > \bar{Y}) \end{cases}$$
(3)



Fig.8. (a) An imaginary lines shows the centroid of (b) f_1 and (c) f_2 that splitting the regions

C. Vertices Connection

The idea of traversal strategy between vertices in this phase is based on an incremental construction approach which is a method of computing the convex hull of a finite set of vertices. While convex hull method chooses the anchor point from the lowest y coordinate, the algorithm sets the least x coordinate as the starting point. To reduce the complexity of the disorganization, the connection is broken into two regions which are upper region (r_1) and lower region (r_2) as described in the previous section. The algorithm is operated by a "walking" procedure. It walks clockwise for upper regions while counterclockwise for lower regions.

For a formulated description of the procedure, let SP be the point in r_1 with the minimum x – coordinate or the leftmost vertex and let $(v_2, v_3, ..., v_n)$ be the remaining vertices in r₁. Starting from SP, the connection is made based on x⁺direction until the rightmost vertex. This is explained in equation (4) where we start from our seed point SP and by incrementally differentiating the x values. The same procedure is performed on the lower region but with the exception of the direction. In case the next two vertices to be connected have the same x value, the smallest angle of the vertex is chosen based on equation (5), where Atan2 is to find angle in radians between two points $(\delta y, \delta x)$. After each of these two regions is complete, they are concatenated into a complete face by connecting the corresponding first and last vertex in both regions.

$$(V_c) = SP + \sum_{i=2}^n (x_i - x_{i-1}) : SP = a, x \in (a, b], n \in \mathbb{Z}^+$$
(4)

$$\delta y = y2 - y1$$

$$\delta x = x2 - x1$$

$$angle = \left|Atan2(\delta y, \delta x) * \left(\frac{180}{Pl}\right)\right|$$
(5)

Figure 9 shows the process of creating a combination of faces as a result of the algorithm. In Figure 9 (a) two regions of f_1 are shown which will be unified to a single face in figure (b). The same is shown for the f_2 in figure (c) and figure (d). Figure (e) shows the combination of the faces together as the result of our algorithm for this stage.



Fig.9. (a) Two regions of face one (b) the unified single face one (c) two regions of the second face (d) the unified single face two (e) the connection of each face

D. Face Connection

In continuance of the previous step, every vertex of a face is connected to form the original shape. The results for now would be in a 2D form. To achieve the complete

object, these faces are connected. New edges are inserted to each corresponding vertex of each region and face as shown in Figure 10.



Fig.10. The two faces is concatenated for a complete geometric object

E. Overall Algorithm

Input: Face Vertices	//Two	faces	of	the		
object contain same number of vertices						
<i>Result</i> : Polygon/object connection //Set of edges form						
object shape						

/*1. List Initialization*/

The whole list is sorted (radix sort) as two arrays: x-array and y-array

/*2. Seed Point Identification*/

The minimum x value from the x-array is initialized as the Seed Point (*SP*)

The (SP) is resided as the first index in the x-array

/*3. Region Splitting*/

Get the centroid of y - axis of the vertices from y-array FOR all of the vertices iIF $Y(i) \le centroid$ $vertex \in r_1$ ELSE

 $vertex \in r_2$ end FOR

/*4. Vertices Connection*/

The walking procedure is based on the x^+ – *direction* and the smallest angle between two vertices (X(i), X(i + 1))//clockwise for r_1 and counter clockwise for r_2

We start from *SP* and go one by one through the *x*-array. **FOR** all of the *i* in the r_1 and r_2 of *x*-array

$$if X(i) < X(i + 1)$$
Insert new edge $(i, i + 1)$

$$if X(i) = X(i + 1)$$

$$if angle (X(i)) < angle (X(i + 1))$$
Insert new edge $(i, i + 1)$
end FOR

Connect the first index of r_1 to the first index of r_2 and Connect the last index of r_1 to the last index of r_2

/*5. Face Connection*/

```
The connection is based on the clockwise movement FOR all of the vertices i
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r_{1}(i))
Insert new edges (F1 \rightarrow r_{1}(i), F2 \rightarrow r_{2}(i), F2 \rightarrow r_{2}(i))
end FOR
Insert new edges (F1 \rightarrow r_{2}(i), F2 \rightarrow r_{2}(i))
```

Fig.11. The proposed pseudo code for object shape reconstruction

IV. IMPLEMENTATION

A Graphical User Interface (GUI) is designed to run the entire algorithm and to test the experiments for producing the results. The data structure and coded blocks were built based on each process indicated in the proposed methodology section. The implementation is to ensure that the overall algorithm is efficient enough to connect the vertices within the faces and to connect both faces accurately. Visual Basic 6.0 has been chosen as the development environment at this stage. Figure 12 shows the system GUI for object shape reconstruction process. The elements of each process have been segregated to show the progress in each stage for algorithm validation. In the top left corner it shows the visualized raw data as input and through the stages it reaches to the bottom right corner, visualizing the overall model as a result.



Fig.12. The system interface for object shape reconstruction algorithm for a sample object from our dataset

V. EXPERIMENTS, RESULTS AND DISCUSSION

The object shape reconstruction algorithm can successfully obtain its objective in constructing the final shape from two set of faces with disorganized vertices. As explained in the introduction of this chapter, there are several experiments which have attempted to solve the connection problem. A challenge for all of these studies is to find the connection as there is no clue about how the points should be connected. Generally, the connections between vertices are made through incremental construction based on the x axis and angle evaluation for each prior vertex to the next vertex. These connections between the set of points should preserve the original shape of the object. We name the technique as the splitting and recombination technique due to the reason that we first split the vertices and then recombine to create the shape. It is used to gratify the process of the connection. A sample of the experiment results are presented in Table 2.

Original input	Vertices and regions	<i>f</i> 1	f2	Both faces	Complete connection of each face	Complete object connection
R.	<u></u>	-2	-رید. - ب	-		Test -
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Table 2. Sample output of the vertices connection experiments

To evaluate and validate the proposed object shape reconstruction algorithm, experiments are conducted on a

computer with specifications of Windows 7 Professional, 8G-RAM and 3.2 GHz CPU. We have also gone through

a series of performance evaluations to make sure that the proposed algorithm is precise and correct. We evaluated the accuracy of the output and computational/time complexity by modeling the computation/time usage of the proposed algorithm. This would give us estimates to know how fast the algorithm could deliver the output if the numbers of vertices which are the inputs are considerable.

A. Performance Evaluation (Accuracy)

One of the metrics evaluated is the accuracy of the proposed algorithm. The performance of the proposed algorithm is evaluated against the well-known concave hull algorithm based on the precision metric. Precision can be defined as the exactness of measurement. Equation (6) is used to compute the precision:

$$Precision = \frac{TP}{TP + FP} \tag{6}$$

Let TP (True Positive) represent the correct shape detected. FP (False Positive) is when we are unable to detect the true or correct shape (falsely detect). Our algorithm does not include a method to detect false or incorrect shapes. The algorithm either detects a correct shape (TP) or does not detect (FP) by its inefficiency. Based on this description there is no recall to be estimated. We defined the accuracy which is the closeness of a measurement to the true value and could conclude the precision we reach as accuracy. The more precise the proposed algorithm detects the shapes, the more accurate it is.

The evaluation process starts by creating a set of ground truth images. By ground truth image we mean the original image that shows the shape of the object and which would later be used as a benchmark for the validation. For evaluation, the ground truth is compared with the proposed algorithm and also to the closest algorithm to this work which is concave hull by Park & Oh [7]. We use a modified version of the concave hull algorithm to suit the objective and performance of our algorithm. Comparing the original images, our results and the results of modified concave hull algorithm, we could reach a conclusion on how efficient, complete and accurate our algorithm is. A visual example of the ground truth, modified concave hull and the proposed algorithm compared together is shown in Figure 13. Using the entire image dataset, the accuracy of both methods has been demonstrated and evaluated. The results show that both algorithms achieved the same accuracy which is 100%. In other words, both algorithms accurately detect all the shapes of the ground truth. We must note that the concave hull is modified to be competitive with the nature of our work. If we compare with the unmodified concave algorithm we see a result of only 52% correct identified shapes. This points out the competitiveness of the proposed algorithm while it has taken a completely new approach. The resulted accuracy is not unusual in the context of shape identification. Though the same accuracy could be achieved by modifying the concave algorithm, we will later show that the proposed algorithm has complete benefits in its new approach in terms of time complexity and thus performance.



Fig.13. A sample visual comparison of the results between ground truth images, modified concave algorithm and the proposed algorithm

B. Performance Evaluation (Time Complexity)

The time complexity models the time taken by an algorithm as the input size rises considerably. It is usually expressed using the big O notation to classify algorithms by how they performed on input data size they are working on [15]. It is measured by estimating the number

of elementary operations performed by an algorithm; either in loops or other functions. Based on the evaluated model, the algorithm could be compared with other algorithms to determine the most efficient in terms of the time or computations needed to finish the entire process.

We have computed the time complexity of the Concave hull algorithm proposed by Park & Oh [7] for a

2-dimensional dataset. It utilizes a convex hull algorithm to generate a list. Convex hull has a O(nlogn) complexity. For the next three steps the algorithm digs through the concave list. The authors have mentioned that the overall complexity of their algorithm is O(nlogn). Referring to our algorithm in Figure (11), we show 5 distinct stages. We computed the complexity of each stage and conclude as follows:

T1: List initialization: Radix Sort has been used to sort the entire list due to its efficiency. Normally Radix Sort complexity is computed by: O(wn) where w is our word size. (For example 123 has a word size of 3 while 23 has a word size of 2 because of the number of digits composing the number). In our case, the vertices are not scattered in long distance and so our word size w might not even exceed 3.

T2: Seed point identification: Simple initialization, O(1)

T3: Region splitting: Goes through the whole list and assigns based on centroid O(n)

T4: Vertices connection (Walking): Walks through all the edges using the x-array, O(2n)

T5: Face connection: Goes once through all the vertices and inserts edges, O(n)

Therefore, the total estimated time complexity is O(wn) where w is estimated to be between 7 and log(n). In the worst case scenario where are vertices are scattered in very far apart distances the time complexity would reach O(nlogn) but it would still be smaller. This is far from possible based on the nature of our work. Based on mathematical evidence, O(wn) has less complexity in comparison with O(nlogn + n) by Park and Oh [7]. A graph shown in Figure 14 shows a visual comparison of the complexities of the two algorithms when many vertices are given as inputs. The y axis represents the number of computations which each computation is a unit of time. The x axis represents the number of vertices given as input to both algorithms.



Fig.14. A time complexity comparison of the proposed algorithm with [7]

VI. CONCLUSION

This proposed algorithm producing the correct shape on finite vertices of a face object has several advantages. The main advantage is that the final procedure could accurately and efficiently complete the automatic reconstruction of object from sketch. It is also an automated algorithm with no user intervention required through the whole process of object shape reconstruction. In addition, to get the final output only a second of time is needed for our examples. This is due to the O(wn) computation/time complexity of the proposed algorithm. The computation/time complexity model shows that the proposed algorithm is more efficient in this aspect compared to any available concave hull algorithm. The lines are also accurately identical to the original object because the edges are drawn based on the vertices. One limitation is that the algorithm is highly dependent on accurate vertex detection. If a vertex is missed then the resulting shape would not produce the actual model.

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