Performance Comparison of Various Diversity Techniques using Matlab Simulation

Sanjiv Kumar
Department of Computer Engineering, BPS Mahila Vishwavidyalaya, Khanpur, Kalan-131305, India
E-mail: skganghas@rediffmail.com

P. K. Gupta
Department of Computer Science and Engineering, Jaypee University of Information Technology, Waknaghat, Solan – 173 234, India
E-mail: pradeep1976@yahoo.com

G. Singh
Department of Electronics & Communication Engineering, Jaypee University of Information Technology, Waknaghat, Solan – 173 234, India
E-mail: drghanshyam.singh@yahoo.com

D. S. Chauhan
Uttarakhand Technical University, Dehradun, India
E-mail: drdschauhan@gmail.com

Abstract— Due to the time-varying nature of the wireless channel and presence of limited resources for the signal transmission, which faces various detrimental effects such as path-loss, delay spread, Doppler spread, shadowing and interference make it very difficult to achieve sufficient data rates. To combat the effect of multi-path fading in the wireless communication system, the diversity combining mechanism has been introduced. In this paper, we have developed an algorithm for the performance evaluation of various spatial diversity combining techniques by using Matlab simulation. The developed new algorithm combine all three diversity techniques such as maximal ratio combining (MRC), selection combining (SC) and equal gain combining (EGC) techniques. The combined diversity techniques algorithm computes and compares the MRC, SC, and EGC combining techniques theoretically by using the Matlab simulation.

Index Terms— Maximal-Ratio Combining, Selection Combining, Equal-Gain Combining, Fading, Rayleigh Channel

I. Introduction

Diversity combining is a potential method by which multiple replicas of the same information carrying signal received over several diversity branches are combined with specific manner in order to combat the diverse effects of the multipath fading in wireless communication systems [1-6]. However, the diversity combining methods have been implemented either at receiver or transmitter, or on both for combating very effectively the effects of multipath fading at a relatively low cost. For instance, let us consider the design of an antenna array receiver for the millimeter-wave communications, where several tens of array elements have been placed on the surface of a portable receiver [7-10]. Thus, there is a need for significant diversity combining techniques to be used effectively with large antenna arrays. However, the suboptimal receiver structures may exploit other statistics or consider a partitioned diversity combining scheme [10] to achieve the performance comparable to the optimal receiver. Then, it would be highly desirable to assess the efficacy of several receiver design options to obtain the most appropriate choice with reference to the complexity and implementation constraints.

Due to the time-varying nature of the wireless channel and presence of limited resources for transmission, the transmitted signal faces various detrimental effects such as path loss, delay spread, Doppler spread, shadowing and interference which make it very difficult to achieve high data rates. To mitigate the effect of multipath fading in the wireless communication, a most popular mechanism known as diversity has been introduced. In the telecommunication system, the diversity schemes is a method for improving the reliability of a message signal by using two or more communication channels with different characteristics. It plays significant role in combating the signal fading and co-channel interference without error bursts.
Alternatively, a redundant forward error correction code can be used. The diversity technique exploits the multipath propagation and provides the diversity gain (measured in decibels) [2-10]. The diversity combining technique can be exploited over time, frequency and space domains. However, it is well known that the diversity reception is an efficient communication receiver technique for mitigating the detrimental effects of multipath fading by increasing the overall signal-to-noise ratio (SNR) and improve the radio link performance in the wireless mobile channels at relatively low cost [11-21].

In this paper, we have developed an algorithm for the performance evaluation of various spatial diversity combing techniques by using Matlab simulation. The most important diversity reception methods employed in digital communication receivers are maximal ratio combining (MRC), equal gain combining (EGC), and selection combining (SC). However, MRC is the optimal technique in the sense that it attains the highest SNR as compared to any combining scheme as well as independent of the distribution of the branch signals since it results in a maximum-likelihood receiver. The remainder of the paper is organized as follows. Section 2 is concerned with the diversity system model. In section 3, proposed algorithm for the performance evaluation has been developed. Section 4 discusses about the simulation results for various diversity techniques by using developed algorithm. Finally, section 5 concludes the work.

II. Diversity System Model

The diversity system model consists of a physical model by assuming the fading to be independent from one element to the next and each element acts as an independent sample of the random fading process (Rayleigh) means each element of the array receives an independent copy of the transmitted signal [9, 11]. In this system model, we emphasized to combine all these independent samples to yield the enhanced signal-to-noise ratio (SNR) and reducing bit-error-rate (BER). However, the diversity works because we receive N independent copies of the same signal at array of N antennas. If at least one copy has sufficient power, one should be able to process the signal. Here, we consider a single-user system model wherein the received signal is a sum of the desired signal and noise [2, 3].

\[ x = hu(t) + n \]  

(1)

where \( u(t) \) is the unit power signal transmitted, \( h \) represents the channel (including the signal power) and \( n \) the noise. The power in the signal over a single symbol period, \( T_s \), at element \( n \), is

\[ P = \frac{1}{T_s} \int_0^{T_s} |h_n(t)|^2 |u(t)|^2 \, dt \]

\[ = |h_n(t)|^2 \frac{1}{T_s} \int_0^{T_s} |u(t)|^2 \, dt = |h_n|^2 \]  

(2)

Since we are assuming slow fading, the term \( |h_n(t)| \) remains constant over a symbol period and can be brought out of the integral and \( u(t) \) is assumed to have unit power. Setting \( E\{|h_n(t)|^2\} = \sigma^2 \) and we get the instantaneous SNR at the nth element \( (\gamma_n) \) as:

\[ \gamma_n = \frac{|h_n|^2}{\sigma^2} \]  

(3)

This instantaneous SNR is a random variable with a specific realization given the channel realization \( h_n \).

The expectation value taken to estimate the noise power is therefore consider over a relatively short time period [2]. We are assuming Rayleigh fading, so \( h_n = |h_n| e^{j\angle h_n} \) where \( \angle h_n \) is uniform in \([0, 2\pi]\) and \( |h_n| \) has a Rayleigh pdf, implying \( |h_n|^2 \) and \( \gamma_n \) has an exponential pdf such as [3]:

\[ |h_n|^2 = \frac{2|h_n|^2}{P_0} e^{-\frac{|h_n|^2}{P_0}} \]  

(4)

\[ \gamma_n \approx \frac{1}{T} e^{-\gamma_n \cdot T} \]  

(5)

\[ \Gamma = E\{\gamma_n\} = E\{\frac{|h_n|^2}{\sigma^2}\} = \frac{P_0}{\sigma^2} \]  

(6)

The instantaneous SNR at each element which is an exponentially distributed random variable. \( \Gamma \) represents the average SNR at each element. This is also the SNR of a single element antenna that is the SNR if there is no array. Therefore \( \Gamma \) serve as a baseline for improvement in the SNR.

2.1 Selection Combining Diversity

At the receiver, if we have now N copies of the same transmitted symbol. Then we have to combine them effectively to reliably recover the transmitted data. We consider the fading for each signal is independent. In the selection combining diversity, the receiver selects the antenna with the highest received signal power and ignores observations from the other antennas. We assign weights such that for maximum power signal provide weight 1 and for rest of others weight 0. Therefore, we are able to get one significant signal at
the output. For deriving the mathematical expressions for the selection combining diversity, we obtain the set of weights \( w \). To obtain the weight vector value, we assume that the receiver has the required knowledge of the channel fading vector \( h \). As each element is an independent sample of the fading process, the element with the greatest SNR is chosen for further processing. In the selection combining diversity, the expression instantaneous SNR with weight function can be written as [2-5]:

\[
    w_k = \begin{cases} 
        1 & \gamma_k = \max_n \{ \gamma_n \} \\
        0 & \text{otherwise}
    \end{cases} \tag{7}
\]

Since the element chosen is the one with the maximum SNR, the output SNR of the selection diversity scheme is \( \gamma = \max_n \{ \gamma_n \} \). This technique requires only the measurement of the signal power no phase shifters and variable gain. The parameters for analyzing such systems are the outage probability, BER and resulting improvement in SNR. The outage probability provides the probability that the output SNR falls below a threshold value \( \gamma_s \). This expression is valid only when the fading at each element is assumed independent. By using the pdf of \( \gamma_n \), then the outage probability is [2, 8]:

\[
    P_{\text{out}}(\gamma_s) = \left[ 1 - e^{\gamma_s/\Gamma} \right]^N \tag{8}
\]

From (8), the outage probability decreases exponentially with the number of elements. \( P_{\text{out}} \) represents the cdf of the output SNR as a function of threshold \( \gamma_s \).

### 2.2 Maximal Ratio Combining Diversity

In order to maximize the output SNR of the signal, we cannot choose one signal and neglect others. So we combine the signals on such a way that the output signal provides all transmitted information. In MRC, we assign the weighted bits to the signal in such a way that all the signals are strong, which is performed in the order to improve the faded signals. The branches with strong signals are further amplified and those which are weak are attenuated. Then we combine the signals to get output signal, which improved the performance than the selection combining diversity, however it is too complex to implement. Its weighted bit allocation process is complex and we have to know the exact signal at the receiver [10, 16]. The received signal at the array elements as a vector \( x(t) \), and the output signal as \( r(t) \) [2, 3]:

\[
    x(t) = h(t)u(t) + n(t) \tag{9}
\]

where

\[
    \begin{cases} 
        h = [h_0, h_1, \ldots, h_{N-1}]^T \\
        n = [n_0, n_1, \ldots, n_{N-1}]^T
    \end{cases} \quad \text{(10)}
\]

and

\[
    r(t) = w^H x = w^H h u(t) + w^H n \tag{11}
\]

Since the signal \( u(t) \) has unit average power, the instantaneous output SNR is:

\[
    \gamma = \frac{|w^H h|^2}{E\{w^H n^H w\}} \tag{12}
\]

The noise power in the denominator is given by:

\[
    P_n = E\{w^H n^H w\} = E\{w^H n n^H w\} = \sigma^2 w^H I_N w
\]

\[
    \sigma^2 w^H w = \sigma^2 \|w\|^2 \tag{13}
\]

and \( I_N \) represents the \( N \times N \) identity matrix. Since the constants do not matter, one could always scale \( w \) such that \( \|w\| = 1 \). The SNR is therefore given by [2]:

\[
    \gamma = \frac{|w^H h|^2}{\sigma^2} \tag{14}
\]

By the Cauchy-Schwarz inequality, it has a maximum value when \( w \) is linearly proportional to \( h \), or \( w = h \), then

\[
    \gamma = \frac{|w^H h|^2}{\sigma^2} = \frac{h^H h}{\sigma^2} = \frac{\sum_{n=0}^{N-1} |h_n|^2}{\sigma^2} \tag{15}
\]

or

\[
    \gamma = \sum_{n=0}^{N-1} \gamma_n \tag{16}
\]

The output SNR is, therefore, the sum of the SNR at each element. However, the better diversity combiner can choose the weights to the fading for each element. In some sense, this answer is expected since the solution is effectively the matched filter for the fading signal. We know that the matched filter is optimal in the single user case. By using (15) expected value of the output SNR is therefore \( N \) times the average SNR at each element, which is [3]:

Copyright © 2013 MECS

*I.J. Information Technology and Computer Science, 2013, 11, 54-61*
\[ E\{\gamma\} = N\Gamma \]  

(17)

This indicates that on average, the SNR improves by a factor of \(N\), which is significantly better than the factor of (ln\(N\)) improvement in the selection combining diversity case. To determine the pdf of the output SNR, we use the fact that the pdf of the sum of \(N\) independent random variables is the convolution of the individual pdfs. Further, the convolution of two functions is equivalent to multiplying the two functions in the frequency (or Laplace) domain. We know that each \(Y_n\) in (15) is exponentially distributed. The characteristic function of a random variable \(X\) is given by \(E\{e^{-sX}\}\) that is, the characteristic function (the Laplace transform) of the pdf.

\[ F \Gamma (s) = E\{e^{-s\gamma}\} = \frac{1}{1 + s\Gamma} \]  

(18)

\[ F \Gamma (s) = \left[ \frac{1}{1 + s\Gamma} \right]^N \]  

(19)

\[ PDF (\gamma) = f \Gamma (\gamma) = L^{-1} \left[ F \Gamma (s) \right] = \frac{1}{2\pi j} \int_{c-j\infty}^{c+j\infty} e^{\gamma \gamma} \left( 1 + s\Gamma \right)^{\gamma} d\gamma \]  

(20)

or

\[ PDF(\gamma) = \frac{1}{(N-1)!} \frac{\gamma^{N-1}}{\Gamma^N} e^{-\gamma/\Gamma} \]  

(21)

Using this pdf, the outage probability for a threshold \(\gamma_s\) is given by [3]:

\[ P_{out} = P(\gamma < \gamma_s) = \int_0^{\gamma_s} \frac{1}{(N-1)!} \frac{\gamma^{N-1}}{\Gamma^N} e^{-\gamma/\Gamma} d\gamma \]  

(22)

\[ P_{out} = 1 - e^{-\gamma_s/\Gamma} \left( \frac{\gamma_s}{\Gamma} \right)^N \frac{1}{N!} \]  

(23)

2.3 Equal Gain Combining Diversity

In this process, we have assigned the equal weights to the receiver branches which amplify the signals equally. With reference to the performance comparison it is comparable to MRC, however easy to implement [16-21]. So it is a better option than the selection combining diversity. We require a technique in which the weights vary with the fading signals and the magnitude of which fluctuate over several 10s of dB. In the equal gain combiner, [2]:

\[ w_n = e^{j\gamma h_n} \]  

(24)

\[ w_n * h_n = |h_n| \]  

(25)

\[ w^H h = \sum_{n=0}^{N-1} |h_n| \]  

(26)

The noise and instantaneous SNR are given by:

\[ P_n = w^H w \sigma^2 = N\sigma^2 \]  

(27)

\[ \gamma = \frac{\left( \sum_{n=0}^{N-1} |h_n| \right)^2}{N\sigma^2} \]  

(28)

Using the fact that \(|h_n|\) is Rayleigh distributed, we have:

\[ E(|h_n|) = \sqrt{\Pi P_0} \]  

(29)

\[ E(|h_n|^2) = P_0 \]  

(30)

By using the SNR defined in (28) together with (29) and (30), we can find the mean SNR as:

\[ E\{\gamma\} = \frac{E \left\{ \sum_{n=0}^{N-1} |h_n|^2 \right\}}{2N\sigma^2} = \frac{1}{2N\sigma^2} E \left\{ \sum_{n=0}^{N-1} \sum_{m=0}^{N-1} |h_n||h_m| \right\} \]  

(31)

After some mathematical manipulation and simplifying (31), we get:

\[ E\{\gamma\} = \left[ 1 + \frac{\Pi}{4} \right] \Gamma \]  

(32)

This analysis reveals that, despite being significantly simpler to implement, the equal gain combiner results in an improvement in SNR that is comparable to that of the optimal maximal ratio combiner. The SNR of both combiners increases linearly with \(N\).
III. Proposed Combined Algorithm for Diversity Techniques MRC, SC and, EG

In this section, we have proposed a combined algorithm for the discussed diversity techniques in the preceding sections like maximal ratio combining, selection combining and equal gain. The proposed algorithm completes its functioning in 12 different steps. User has to make the choice A, B, and C to implement the discussed diversity technique MRC, SC, and EG, respectively and based on the given choice algorithm computes the various operations which are listed in various steps for each diversity techniques. Finally, algorithm computes and compares the simulated outage probability/BER as well as SNR enhancement with the theoretical results.

Algorithm: Combined diversity techniques

**STEP 1: VARIABLE DECLARATION**
- N: Number of bits or symbols
- ip: Matrix of [0,1]
- S: Represents BPSK Modulation
- X: input for number of receiver of antennas
- Eb_No_dB: required signal to noise ratio in digital communication systems
- n: Additive white noise
- ii, jj: input of argument specifying the SNR in dB.
- h: Rayleigh channel
- sD, y: Channel and noise addition
- nErr: Counting the number of errors.
- ch: enter choice

**STEP 2: Define Switch**

```
SWITCH(ch)
ch == A : Maximal Ratio Combining (MRC)
ch == B : Selection Combining (SC)
ch == C : Equal Gain (EG)
```

if (ch == A) THEN

**STEP 3: Functioning Of MRC Algorithm**

```
N  Input;
generate matrix of [0,1] with equal probability
ip  rand(1,N)>0.5;
find BPSK modulation S  2 * ip -1 where 0 -1, 1
input X;
Eb_No_dB  [0:35] for multiple values of Eb/No.
FOR jj  1:length(nRx)
    FOR ii  1:length(Eb_No_dB)
        Calculate white Gaussian noise n with 0 dB variance;
        Make and Find the value of h;
```

**STEP 4: Channel and noise addition**

```
sD  Kron(Ones(nRx(jj),1),S);
y  h.*sD + 10^(-Eb_No_dB(ii)/20)*n;
```

**STEP 5: Equalization of MRC**

```
Find the value of yHat;
```

**STEP 6: Receiver hard decision decoding**

```
Find the value if ipHat;
```

**STEP 7: Counting of Errors**

```
Find the value of nErr(jj,ii);
END
```

ELSEIF (ch == B)

**STEP 8: Functioning of SC algorithm**

```
REPEAT STEP 3 and STEP 4
STEP 9: Finding the power and max power of channel
Find the hPower and hMaxVal of the signal on all rx chain;
STEP 10: Deleting the chain with maximum power
Find the value of ySel and hSel;
REPEAT STEP 6 and STEP 7;
ELSEIF (ch==C)
```

**STEP 11: Functioning of EG algorithm**

```
REPEAT STEP 3 and STEP 4 ;
STEP 12: Equalization with EQUAL GAIN combining
Find the value of yHat;
ENDIF
ENDIF
```

Calculate and compare simulated BER and theoretical BER:

IV. Simulation Results for Comparison of above Diversity Techniques

Fig. 1 shows the plot between signal-to-noise ratio and number of received antennas. As we increase the number of received antenna, the SNR is increased significantly. The above plot shows us that the MRC is the best among the three diversity techniques. Equal Gain combining technique is closest to the MRC and the Selection Combining is worst among them. In terms of the required processing, the selection combiner is the easiest - it requires only a measurement of SNR at each element, however not the phase or the amplitude. The results presented, used a coherent receiver (the phase of channel is removed after the fact). However, both the maximal ratio and equal gain combiners, on the other hand, require phase information. The maximal ratio combiner requires accurate measurement of the gain too. This is clearly difficult to implement, as the dynamic range of a Rayleigh fading signal may be quite large. For this additional cost, for two elements, the MRC improves performance by about 0.6dB over the equal gain combiner at a BER of 1%. Table 1 compares the various diversity techniques.

<table>
<thead>
<tr>
<th>Technique</th>
<th>Circuit Complexity</th>
<th>C/N Improvement factor</th>
</tr>
</thead>
<tbody>
<tr>
<td>Selection Diversity</td>
<td>N receivers</td>
<td>1+1/2+...+1/N</td>
</tr>
<tr>
<td>EGC Diversity</td>
<td>N receivers co-phasing</td>
<td>1+(N-1) × /4</td>
</tr>
<tr>
<td>MRC Diversity</td>
<td>N receivers co-phasing channel estimator</td>
<td>N</td>
</tr>
</tbody>
</table>
V. Conclusion

The diversity combining techniques are one of the most significant solutions to mitigate the fading problem in the wireless communication systems. It overcomes the effects of flat fading by combining multiple independent fading. However, it entails some penalty in terms of rate, bandwidth, complexity or size. However, various combining techniques offer different level of complexity and performance. Among all the combining techniques, MRC offer the best performance, however the highest complexity, whereas the selection combining has the lowest performance and least complexity. These techniques are used to improve the performance of radio channel without any increase in the transmitted power. In this paper, we have developed an algorithm for the diversity combining techniques in MATLAB for the comparative analysis. We observed their performance by varying the number of receiver antennas and measuring the SNR at the receivers, which reveals that MRC is the best diversity among all three and selection combing is the worst. We can also observe that the equal gain is also close to MRC in terms of the performance. To compare MRC with selection combining, we have to increase the number of receivers to 4 which will result into a difference of 2.5 dB in SNR. This difference widens if we further increase the number of antennas at receiver. MRC is considered better than equal gain as it differs by a gain of 0.5 dB. The output curve steeply rises initially but then becomes smooth. It might be because if we go on increasing the number of receiver antennas the complexities in obtaining the desired signal will also increase.

Acknowledgement

The authors are very much thankful to the potential reviewers for their critical comments and suggestions to improve the quality of the manuscript.

References


Authors’ Profiles

Sanjiv Kumar was born in Kurukshetra, in 1975. He received his B. E. in Electronics and Communication Engineering from the Institution of Engineers (India), Calcutta and M. E. in Electronics and Communication Engineering from Maharishi Dayanand University, Rohtak (Haryana). He is working as a lecturer in the Department of Computer Engineering at B. P. S. Mahila Vishwavidyalaya, Khanpur Kalan (Haryana), India. Currently, he is pursuing his Ph. D. from Uttarakhand Technical University, Dehradun. His research interests include wireless communication, fading channel models.

P. K. Gupta received Ph D degree in Computer Science and Engineering from the Jaypee University of Information Technology, Waknaghat, Solan, India in 2012. He graduated in Informatics and Computer Engineering from Vladimir State University, Vladimir, Russia, in 1999 and received his M.E. degree in Informatics and Computer Engineering in 2001 from the same university. He has been associated with academics more than ten years in different institutions like BIT M.Nagar, RKGIT Ghaziabad in India. Currently, he is working as Senior Assistant Professor with the Department of Computer Science and Engineering & IT, Jaypee University of Information Technology, Waknaghat, Solan, India. He has supervised a number of B.Tech/M.Tech/M.Phil. theses from various universities of India. His research interests include Storage Networks, Green Computing, Software Testing and Cloud Computing. He is a Member of IEEE, Life Member of CSI and Life member of Indian Science Congress Association.

G. Singh: received Ph D degree in electronics engineering from the Institute of Technology, Banaras Hindu University, Varanasi, India, in 2000. He was associated with Central Electronics Engineering Research Institute, Pilani, and Institute for Plasma Research, Gandhinagar, India, respectively, where he was Research Scientist. He was also worked as an Assistant Professor at Electronics and Communication Engineering Department, Nirma University of Science and Technology, Ahmedabad, India. He was a Visiting Researcher at the Seoul National University, Seoul, S. Korea. At present, he is Professor with the Department of Electronics and Communication Engineering, Jaypee University of Information Technology, Waknaghat, Solan, India. He is an author and co-author of more than 170 scientific papers of the refereed Journal and International/National Conferences. His research interests include relativistic electronics, surface-plasmons, Electromagnetics and its applications, nanophotonics, microwave/THz antennas and its potential applications.

Prof. D. S. Chauhan was born in 1949 at Dholpur, Rajasthan and his parents belong to Mainpuri, Uttar Pradesh. His education took place in Rajasthan, Madhya Pradesh, Uttar Pradesh, Tamil Nadu and New Delhi.
He did his post doctoral work at Goddard Space Flight Centre, Greenbe, Maryland, USA (1988-91). He did his B.Sc Engg.(1972) in electrical engineering at I.T. B.H.U., M.E. (1978) at R.E.C. Tiruchirapalli (Madras University) and Ph.D. (1986) at IIT/Delhi. His brilliant career brought him to teaching profession at Banaras Hindu University where he was Lecturer, Reader and then has been Professor till today. He has been director KNIT sultanpur in 1999-2000 and founder vice Chancellor of U.P.Tech. University (2000-2003-2006). Later on, he has served as Vice-Chancellor of Lovely Profession University (2006-07) and Jaypee University of Information Technology (2007-2009) Currently he has been serving as Vice- Chancellor of Uttarakhand Technical University for (2009-till) Tenure. He has been member, NBA-executive AICTE, (2001-04)-NABL-DST executive (2002-05) and member, National expert Committee for IIT-NIT research grants. He was Member, University Grant Commission (2006-09). He has been member, CAPART, National executive and chairman central zone, Lucknow from (2001-2004). He has been nominated by UGC as chairman of Advisory committees of four medical universities. Dr Chauhan got best Engineer honour of institution of Engineer in 2001 at Lucknow.

How to cite this paper: Sanjiv Kumar, P. K. Gupta, G. Singh, D. S. Chauhan,”Performance Comparison of Various Diversity Techniques using Matlab Simulation", International Journal of Information Technology and Computer Science(IJITCS), vol.5, no.11, pp.54-61, 2013. DOI: 10.5815/ijitcs.2013.11.06