Study on the Impact Breakup Model of the Space Target Based on the Thin Plate

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Abstract—In the paper, an engineering model for the impact breakup of the space target is studied based on the thin plate. The average fragment size model for the impact breakup of the thin plate is established depending on the strain rate, according as Poisson statistic fragments are discrete and distribution model is figured out. On the foundation of the constitution analysis for the target and projectile, the target equivalent model based on the thin plate is established, and projectile equivalent model is also given. The length and velocity degraded model are set up against the cylindrical projectile. The simulation case is analyzed and the result indicates that the paper model is effective, flexible and has important engineering reference value.

Index Terms—Space Target; Thin Plate; Impact Breakup model; Strain Rate; Projectile

I. INTRODUCTION

With the increase of the space object (including active spacecraft and space debris) and development of kinetic energy weapon, the risk that space target encounters to be hypervelocity impacted is enhancing, e.g. the accidental collision between US and Russian satellite in 2009 [1], and the USA-193 deliberate space weapon test in 2008 [2], the fragment along with impact breakup of the space target has become the primary source and the collision breakup model also becomes a hotspot of study.

Since 1970s, a series of the impact breakup model has been established, namely historic model, Battelle breakup model, and US National Aeronautics and Space Administration standard collision breakup model (NASA model). Historically, the breakup models currently in use developed over a long period in time. One of the most fundamental works in this context is a publication by Bess originating from 1975 [3]. Many subsequent publications refer to this paper, partly modifying parameters of the model or introducing model extensions. The first version of the breakup model designated as “Battelle” model in this context was developed by a Battelle-led team under the European Space Operations Centre (ESOC) contract between 1990 and 1993 in the wake of the observed disruption of the Spot 1 ARIANE 4 upper stage in November 1986 [4]. In 1998, NASA released a revised breakup model, which later has been implemented into the new version of NASA’s current space debris evolution model, EVOLVE 4.0 [5], and European Space Agency (ESA) further modified the NASA model in 2006 [6], thus, the NASA model acting as the representative of this field is widely used nowadays.

However, all of these models are experiential statistic, only a few of facts are taken into consideration, the spectrum of applicability is limited and couldn’t satisfy the demand of damage effect assessment for the impact of projectile on space target. The essence of hypervelocity impact breakup is the stress wave (including shock, plastic, elastic wave) which is induced by hypervelocity impact and diffusing both in the target and projectile, so the characteristic of space target impact breakup can be studied in terms of stress wave. The paper considers the realistic constitute characteristic both the target and projectile, the fragment average size model for the impact breakup of thin plate is established depending on strain rate, the fragments are discrete according to Poisson statistic and fragment distribution model is figured out, the target is equivalent to a system consisting with some thin plates; the length and velocity degraded model is set up against the cylindrical projectile; the typical case is simulated and analyzed in order to validate the effectiveness of the models. The simulation case indicates the related models established in the paper have important engineering reference value.

II. BREAKUP MODEL FOR THIN PLATE

The plate that the stress and stain have not gradient distribution along the direction of plate thickness during impact body penetrating process is namely thin plate [7], the plate that its thickness is less than characteristic length of projectile is also called thin plate.

A. Impact Model of Projectile on Thin Plate

In the current model, only the case for cylindrical projectiles impacting at normal incidence on thin plate is considered. Fig. 1 shows the sketch map for the normal
impact of projectile on thin plate, the body of projectile is cylindrical shape, the head of projectile takes on semi-sphere with radius of \( R \), the \( P_0 \) is contacting face pressure during impacting instantaneously, the \( P' \) is hole wall pressure, the domain confined by hole radius \( r_0 \) is normal impact domain. Except for the normal impact domain, the stress wave in the thin plate plane induced by projectile hypervelocity impact can be regarded as cylinder wave, the intensity of stress wave decides the failure extent of the thin plate, according to the Ref. [7], when \( r_0 < r < 2.21r_0 \), namely the domain confined by \( r_1 \) is the large plastic distortion domain; when \( 2.21r_0 < r < 3.64r_0 \), namely he domain confined by \( r_2 \) is the small plastic distortion domain; when \( r > 3.64r_0 \), thin plate occurs elastic distortion and doesn’t produce fragment. The domain confined by \( r_1 \) and \( r_2 \) is uniformly called no-normal impact domain.

A large number of penetration models, mostly empirical and some based on mechanics, have been developed for the prediction of hole-diameter in a thin target plate impacted by spherical projectiles at hypervelocity, for the cylindrical projectile, referencing these models to characterize the relationship between projectile radius and radius of hole. Most of these models are of the form [8]

\[
\frac{r_0}{R} = C_1 \left( \frac{\rho_p}{\rho_t} \right)^{\gamma_1} \left( \frac{v_t}{c_p} \right)^{\gamma_2} \left( \frac{v_t}{c_t} \right)^{\gamma_3} \left( \frac{T}{2R} \right)^{\gamma_4} + C_2
\]

(1)

Where \( \rho_p \) and \( \rho_t \) are the projectile and target density respectively; \( c_p \) and \( c_t \) are projectile and target bulk sound speed respectively; \( v_t \) is the impact velocity; \( T \) is the target thickness, namely the thickness of thin plate; \( p1 \sim p4 \), \( C_1 \) and \( C_2 \) are all constant, different models have variant parameter specified in Table 1, in the paper, the Sawle model parameter is chosen. Note that all variable’s unit in the paper is international standard unit.

<table>
<thead>
<tr>
<th>TABLE I. PARAMETERS OF PENETRATION MODEL</th>
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<tbody>
<tr>
<td>Model</td>
</tr>
<tr>
<td></td>
</tr>
<tr>
<td>Maiden</td>
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<tr>
<td>Sawle</td>
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<td>Hill</td>
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<tr>
<td>Chant</td>
</tr>
</tbody>
</table>

B. Fragment Average Size Model

The failure mechanism of thin plate in hypervelocity impact can be classified into three kinds according to the strain rate magnitude, correspondingly for the breakup of thin plate, its average fragment size \( L_c \) (fragment size \( L_c \) will be defined below) can be depicted as the function of strain rate and determined in three different breakup regimes, these are [9]:

Failure model 1: facture toughness dominated failure (low strain rate)

\[
L_c = \left( \frac{\sqrt{24K_c}}{\rho_c c_t \dot{\varepsilon}} \right)^{2/3}
\]

(2-1)

Failure model 2: yield strength dominated failure (medium strain rate)

\[
L_c = \left( \frac{1.2Y_t}{\rho_c c_t \dot{\varepsilon}} \right)^{2/3}
\]

(2-2)

Failure model 3: surface tension dominated failure (high strain rate)

\[
L_c = \left( \frac{48\gamma_t}{\rho_c c_t \dot{\varepsilon}} \right)^{2/3}
\]

(2-3)

Where \( K_c \) is the target fracture toughness; \( \dot{\varepsilon} \) is the stain rate; \( Y_t \) is the target yield strength, the stress which induces material such as aluminum alloy to take on 0.2% plastic strain is acted as yield index; \( \gamma \) is the surface tension. Strictly, \( K_c \), \( Y_t \), and \( \gamma \) are depending on material temperature as following.

\[
Y_t = Y_0 \left( 1 - \frac{T - T_0}{T_m - T_0} \right)^{n_t} \left( \frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} \right)^{n_t}
\]

(3)

\[
K_c = K_{\text{cy}} \left( 1 - \frac{T - T_0}{T_m - T_0} \right)^{n_c}
\]

\[
\gamma = \sigma_0 \left( 1 - \frac{T - T_0}{T_c} \right)^{n_\gamma - 1} \left( 1 + (n_\nu - 1) \frac{T - T_c}{T_c} \right)
\]

Where the variables with subscript “0” is the reference value; \( T \) is temperature, \( T_m \) is the melt temperature, \( T_c \) is critical temperature; \( n_t \), \( m_t \), \( n_c \) and \( n_\gamma \) are constants, for the 7075-T6 aluminum alloy, these constants are 1.5, 0.02, -1 and 1.33 respectively. Considering the paper objective is to establish an engineering calculation model, so the material temperature influence on these variables is neglected.

Model 1 and 2 are fit for the breakup fragment of the material solid region, comparing with the Ref. [7]’s content, these fragments can be uniformly treated as the produce of material plastic distortion, Ref. [10] gives the transition equation between failure modes 1 and 2.
According (3) \( K, \gamma \) are depending on material temperature, so it is very complex to calculate \( \dot{\varepsilon}_r \) and the temperature influence has been neglected, whereas if computing \( \dot{\varepsilon} \), with the parameters of normal temperature, large error will be produced. Reference [10] thinks the transition between failure modes 1 and 2 occurs at strain rates of approximately \( 10^4 \text{s}^{-1} \) for the aluminum, however if letting \( \dot{\varepsilon}_i = 10^{-4} \text{s}^{-1} \), in the instance of simulation case of Part V, namely impact velocity \( v_i = 9000 \text{m/s} \), the radius of projectile \( R = 0.19 \text{m} \), calculating by (5), the max strain rate \( \dot{\varepsilon} = 7.1 \times 10^3 \text{s}^{-1} \), according to Ref. [10] in this circumstance, model 2 will fail, obviously this doesn’t match with the fact, by large calculation, letting the transition strain rate \( \dot{\varepsilon}_i = 1.0 \times 10^3 \text{s}^{-1} \) in the paper.

Model 3 is fit for the fragment of the material liquid region, is used when material temperature is higher than its melting point. For the target and projectile consisting of aluminum alloy, when impact velocity is above \( 8 \text{km/s} \), the material will appear melting, taking the 7075-T6 aluminum alloy, when impact velocity is above \( 8 \text{km/s} \), its surface tension \( \gamma = 1.188 \text{N/m} \), density \( \rho = 2800 \text{kg/m}^3 \), the strain rate is commonly above \( 10^3 \text{s}^{-1} \) when material is liquefied, according as these parameter, the average fragment size is on the order of \( 10^{-3} \text{m} \). Evidently, the risk of the fragment produced by model 3 to spacecraft is limited and the liquefied material is few part of the target through simulation analysis, so the paper doesn’t consider the fragment produced by model 3.

**C. Solution Model of Strain Rate**

Equation (2) indicates that average fragment size is the function of strain rate, the way to solve the strain rate is essential to calculate the average fragment size.

1. **Solution Model for Normal Impact Domain**

Normal impact domain suffers the effect of shock wave which is the discontinuous wave. Reference [10] considers the complexity of the shock wave diffuse and gives an engineering model to solve the strain rate

\[
\dot{\varepsilon} = f_1 \frac{v_i}{2R}
\]

(5)

Where factor \( f_1 < 1 \) is used to fit experimental data, may be \( f_1 = 0.3 \). For the strain rate of normal impact domain, the paper refers to this model.

2. **Solution Model for No-Normal Impact Domain**

No-normal impact domain suffers plastic wave effect to produce fragment, by the characteristic of cylinder wave, the strain rate of this domain can be solved. In the polar coordinate, the strain rate model of cylinder wave is

\[
\begin{align*}
\dot{\varepsilon}_r &= \frac{\partial v}{\partial r} \\
\dot{\varepsilon}_\theta &= \frac{v}{r}
\end{align*}
\]

(6)

Where \( \dot{\varepsilon}_r \) and \( \dot{\varepsilon}_\theta \) are the radial and hoop component of strain rate, so the strain rate \( \dot{\varepsilon} = \sqrt{\dot{\varepsilon}_r^2 + \dot{\varepsilon}_\theta^2} \); \( v \) is the radial particle velocity. It can be seen the way to calculate \( v \) is key to solve strain rate, whereas \( v \) depends on impact parameter.

When projectile impacts target, the initial pressure \( P_0 \) can be acquired by conservation of mass and momentum. According to the one-dimensional shock wave theory [11], the initial conservation equations of mass and momentum for the thin plate are in the following form

\[
\rho_i D_i = \rho'(D_i - v')
\]

(7-1)

\[
(\rho_i D_i)D_i = [\rho'(D_i - v')](D_i - v') + P_0
\]

(7-2)

Where \( v' \) and \( \rho' \) are the article velocity and density behind the shock wave; \( D_i \) is the velocity of shock wave in the target, according to Ref. [9], to first order, \( D_i \) can be replaced by bulk sound speed \( c_i \), considering the engineering applicability, the paper refers to this way, bringing (7-1) into (7-2), obtaining

\[
P_0 = \rho_i c_i v'
\]

(8-1)

Likewise, for the projectile, there is

\[
P_0 = \rho_i c_i (v_i - v')
\]

(8-2)

Combining (8-1) and (8-2), expunging \( v' \), so

\[
P_0 = \frac{\rho_i c_i \rho c_i \gamma}{\rho_i + \rho c_i \gamma} v_i
\]

(9)

Radial particle velocity \( v \) and initial pressure \( P_0 \) have following relationship [12]

\[
v = \frac{P_0 r_0^2}{\rho c_i r^2}
\]

(10)

Where \( r \) is the variable of the equation, consequently,

\[
\dot{\varepsilon}_0 = \frac{P_0 r_0^2}{\rho c_i r^2}
\]

\[
\dot{\varepsilon}_r = \frac{-2P_0 r_0^2}{\rho c_i r^2}
\]

Therefore

\[
\dot{\varepsilon} = \frac{P_0 r_0^2 \sqrt{r^2 + 4}}{\rho c_i r^2}
\]

(11)

**D. Fragment Distribution Model**
The strain rate is continuous with \( r \) and needs to be dispersed into some bins, then the distribution characteristic of fragment is depicted by average fragment size of every bin, Ref. [9] regards the fragment distribution of single bin as Poisson statistic, the disposed fragment data is consistent with experimental data, the paper refers to Ref. [9] and processes the fragment discretely.

The strain rate is divided into \( N \) bins, the target mass of \( i \)th bin is \( m_i \), the fragment size is \( L_i \), the data is arranged in order of increasing average fragment size, so \( L_i < L_{i+1} \). According to the characteristic of the Poisson statistic, in \( i \)th bin, a probability distribution of finding a fragment of mass \( \mu \) within a tolerance \( d\mu \) given by

\[
dP(\mu) = \frac{1}{\mu} e^{-\frac{\mu}{\Pi}} d\mu
\]

Where \( \Pi \) is the mean value of the fragment mass in the bin. Integrating from 0 to \( \mu \) and multiplying by the total mass \( m_i \) of the bin gives the cumulative mass of fragments of mass less than or equal to \( \mu \) in the bin

\[
M(\mu) = m_i \left[ 1 - e^{-\frac{\mu}{\Pi}} \right] d\mu
\]

There is certain relationship between fragment mass and size, Ref. [9] assumes that the mass of the fragment is related to the cube of the fragment size (such as for cubic or spherical particles), and establishes the relationship model in the following

\[
\frac{\mu}{\Pi} = \left( \frac{L_i}{L_c} \right)^3
\]

However if given fragment size \( L_c \), the fragment mass \( \mu \) can be figured out only on condition that fragment is cubic or spherical, for the breakup fragment of the thin plate, except very small particles, most fragments will take on shape of sheet, actually NASA model also gives up the assumption that fragment is spherical and adopts the “characteristic length” to specify the fragment shape, the characteristic length is defined as the mean length of fragment three main axes as Fig. 2 shows.

Referring to the NASA model, the paper adopts the characteristic length or fragment size to characterize the shape of fragment, namely \( L_c = \frac{x + y + z}{3} \). Meanwhile by large calculations the following empirical equation is given to describe the relationship between size and mass against the fragment with the shape of sheet.

\[
\mu = \left( \frac{T_c}{L_c} + 0.1 \right)L_c^3 \rho_i
\]

For the fragments produced by same thin plate, assuming that (14) still satisfies (12).

Therefore, in the bin \( i \), the cumulative mass of fragments having a size less than or equal to \( L_i \) is

\[
M_f(L_i) = \sum_{i=1}^{N} m_i \left[ 1 - e^{-\frac{L_i}{\Pi}} \right]
\]

Finally, the total cumulative mass of all fragments in all bins have a size less than or equal to \( L_c \) is

\[
M_f(L_c) = \sum_{i=1}^{N} m_i \left[ 1 - e^{-\frac{L_c}{\Pi}} \right]
\]

The fragment mass distribution is given, actually the fragment number distribution can be figured out by substituting fragment population \( N_i \) for \( m_i \) in (16) and (17), where the fragments population in the bin \( i \) is \( N_i = m_i / \Pi \). The fragment population transition from average size to Poisson statistic is depicted in Fig. 3. Note that although the distribution is exponential in mass, it is exponential in the cube of the size leading to the characteristic of the statistical distribution in Fig. 3(b).

III. SPACE TARGET AND PROJECTILE MODEL

In the paper, space target is orbiting satellite, therefore, modeling target is modeling satellite.

A. Target Characteristic Analysis

The mass of satellite mainly consists of three type of material: metal material, the representative is aluminum alloy, the density is about 2800kg/m\(^3\); composite material, the representative is Carbon Fiber Reinforced Plastics (CFRP), the density is 1760–1800kg/m\(^3\); propellant, the representative is hydrazine, the density is 1008kg/m\(^3\). The density of US spacecraft launched from 1987–1984 is between 20–172kg/m\(^3\), mean is 79 kg/m\(^3\). Reference [14] gives the relationship between satellite volume \( V \) and wet weight \( M_w \) (namely including propellant mass):
According to this equation, the density of satellite wet weight is only 100 kg/m$^3$. In conclusion, there is large spacing inside the satellite. On the structure, satellite usually adapts cabin constitution [15], every cabin includes many faceplates. Fig. 4 shows a typical satellite model which is utilized in the hypervelocity impact test by NASA [16]. Reference [17] studies the damage effect for the hypervelocity impact of Projectile on the Tactical Ballistic Missile (TBM), the target is equivalent to a system consisting of seven steel plates with a thickness of 5mm, referring to this reference and considering the characteristic of satellite, the equivalent model of space target is set up based on the thin plate.

B. Target Equivalent Model

Effect domain of cylinder with projectile vertical axis and 3.64$r_0$ radius is shaped when projectile impacts space target, letting $D_1$ be this domain index and $D_2$ be the space domain that space target occupied, the intersection $D = D_1 \cup D_2$, is called breakup domain (Note that the precondition is the vertical axis of projectile interacting with $D_2$), the target mass $M$ marked by the breakup domain $D$ will partially or outright turn into fragments, where $M$ consists of aluminum alloy and CFRP, the propellant hydrazine is liquid and doesn’t produce fragment, so it isn’t considered. $M$ could be determined by the encounter model between projectile and target, this doesn’t belong to the paper category and isn’t studied further. Letting $k_1$ and $k_2$ be the aluminum alloy and CFRP fraction in the satellite dry weight (namely except for the propellant mass), and $\rho_1$, $\rho_2$ be the aluminum alloy and CFRP density, the radius of thin plate is $r_i = 3.64r_0$, so the equivalent aluminum alloy and CFRP thin plate number are respectively

$$n_i = \frac{k_i M}{\pi r_i^2 T \rho_i} \quad (19)$$

Where $i = 1$ represents the aluminum alloy and $i = 2$ represents CFRP. If the target characteristic length such as side or radius, is less than $r_i$, (19) should be recalculated by the target characteristic length.

IV. PROJECTILE DEGRADED MODEL

When projectile impacts a thin plate, its velocity and mass will be consumed until all thin plates is impacted or the number of thin plates are sufficient to use up the projectile. Actually, the debris cloud induced by projectile impacting the former thin plate will bring on certain extent damage to the later thin plate, but comparing with the projectile impact, this damage is minor and isn’t considered. Reference [19] studied the residual length and velocity of the projectile after impacting the thin plate. Referring to this reference and modeling the degraded model of projectile impacting target.

A. Projectile Length Degraded Model

Projectile length degraded model is established based on the projectile penetrating target rate, the form given by Ref. [19] is

$$l_r = l_0 \exp\left[-\frac{\rho_r}{2Y_p}(v_r - u_0)^2\right] \quad (20-1)$$

Where $l_r$ is the projectile residual length; $l_0$ is the projectile initial length; $Y_p$ is the yield strength of projectile; $u_0$ is initial penetration rate given by

$$u_0 = \begin{cases} v_i & : v_i \leq v_c \\ \frac{v_i}{1 + \gamma} - \frac{\cos Q}{1 + \gamma} (v_c - 1.1Y \sin Qu_r) & : v_c < v_i \leq c_i \\ \frac{v_i}{1 + \gamma} & : c_i < v_i \end{cases}$$

C. Projectile Equivalent Model

For the cylindrical projectile, the paper refers to the Miniature Homing Vehicle (MHV) which is used by the US P-78 space test in 1985 [18], establishes the equivalent model. MHV takes on a right-circular cylinder with a diameter of 30.5cm and a length of 33cm, and mass is 16kg, so its mean density is 660kg/m$^3$, most of the experiments used projectiles are made of some of mental, aluminum projectile are very common, as stated before aluminum density is about 2800kg/m$^3$, so there also is many space in the MHV, by simulation analysis, it can be found that the influence of the projectile density on outcome is less than the size of projectile, meanwhile the size of projectile depends on the volume, for the same size, density determine the volume, e.g. for the MHV, if letting density be 2800 kg/m$^3$, both the diameter and height only are 19.4cm. Considering above factor, the projectile is equivalent to a body in which many equal voids evenly evenly distribute, the projectile size is determined by its mean density, other parameters needed in computation accord to the material actual value, such as bulk sound speed and strength.

Figure 4. Typical satellite model
Where $\gamma = \sqrt{\frac{\rho_1}{\rho_2}}$ is density ratio; $v_c = \sqrt{\frac{2Y_p}{\rho_p}}$ is critical impact velocity required to initiate penetration; $u_c = \sqrt{\frac{2Y_p}{\rho_p}}$ is critical penetration rate to initiate projectile erosion, where $Y_p$ is the yield strength of projectile; $Q = \frac{\pi}{2} (v_t - v_c)$. As simulating and calculating, the residual length $l_r$ that projectile impacts the former thin plate will be the initial length that projectile impacts the later thin plate, when residual length is less than a certain value, the projectile is deemed to be used up and simulation ceases.

However, in the light of (20-1), after impacting only one thin plate with a thickness of 5mm and a velocity of 9km/s, the projectile with a diameter of 38cm and a length of 42cm will be thoroughly used up, this case obviously doesn’t match with the truth. By large computation and analysis, it finds that replacing the strength $Y_p$ with the projectile Young’s modulus $E_p$ will be rational. Therefore (19-1) can be rewrite

$$l_r = l_0 \exp\left[-\frac{\rho_p}{2E_p} (v_t - u_0)^2\right] \quad (20-2)$$

The paper adopts the (20-2).

B. Projectile Velocity Degraded Model

The projectile velocity degraded model is established based on hydrodynamic-resistance kinematics [12]

$$v_c = v_t \exp\left(-\frac{T_v}{2l_0}\right) \quad (22)$$

When the projectile velocity is less than the ballistic limit velocity of the thin plate $v_t$, the projectile will stop inside target. If the projectile hydrodynamic penetration depth is $P_e = \frac{l_0}{\gamma}$, $v_t$ can be figured out by the following equation [19]

$$v_t = \sqrt{\frac{4\kappa(1+\gamma) S_p}{\alpha \rho_p} \left[\frac{T_v}{2R} + \frac{1}{2}\right]^{0.5}} \quad (23)$$

Where $a = 1 + \kappa \left(\frac{\gamma}{\alpha} \left[\frac{S_p}{S_t}\right]\right)$,

$$b = 2\kappa \sqrt{\frac{\beta}{\alpha}} \left[\frac{T_v}{2R} \left(\frac{P}{R}\right) - \kappa \right]$$

As $T_v \leq P_e$, $P = T_v$; $T_v > P_e$, $P = P_e$; $\kappa$, $\alpha$, $\beta$, $\lambda$ are constant related with material can let them be 1.0, 1.3, 0.465, 0.5 respectively. Ditto as simulating and calculating, the residual velocity that projectile impacts the former thin plate will be the initial velocity that projectile impacts the later thin plate.

V. THE SIMULATION CASE ANALYSIS

Based on the above model, programming and realizing with Matlab, 1999-025A satellite breakup event is chosen to validate the model, where projectile structure is also referred to the MHV [18] and parameter value is estimated according to Ref. [20]; the target parameter is referred to Ref. [21], because the mass component of target is unknown, assuming target wholly consists of aluminum alloy. Table 2 gives the parameters value both the target and projectile, except these for the projectile $E_p = 7 \times 10^{10}$ Pa, for the target $K_v = 2.3 \times 10^5$ Pa.m$^{1/2}$.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>$m$</th>
<th>$\rho$</th>
<th>$c$</th>
<th>Size</th>
<th>$Y$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Target</td>
<td>950</td>
<td>2800</td>
<td>5200</td>
<td>1.5</td>
<td>1.5</td>
</tr>
<tr>
<td>Projectile</td>
<td>32</td>
<td>660</td>
<td>5200</td>
<td>0.38</td>
<td>0.42</td>
</tr>
</tbody>
</table>

In order to compare with NASA standard collision breakup model, assuming that projectile head-on normally impacts target, the impact velocity is 9km/s [22], considering the real structure of satellite, letting the thickness of thin plate be 5mm. Table 3 shows the number of fragments having a size larger or equal 5cm getting through the paper model, NASA model and US Space Surveillance Network (SSN), where SSN data is referred to Ref. [23].

<table>
<thead>
<tr>
<th>Model</th>
<th>Number of fragments</th>
</tr>
</thead>
<tbody>
<tr>
<td>The paper model</td>
<td>2589</td>
</tr>
<tr>
<td>NASA model</td>
<td>2950</td>
</tr>
<tr>
<td>SSN data</td>
<td>2378</td>
</tr>
</tbody>
</table>

Table 3 shows that the paper model data is more close to the surveillance data comparing with NASA model data. In the table, the data of the paper model and NASA model are get by assuming the projectile head-on normally impacts the target, based on the approximate extent of three series data, this impact pattern can be concluded to be reason that why so many fragments is produced in the 1999-025A satellite breakup event. The advantage of the paper model over NASA model is that comprehensively takes into account the factors influence on impact outcome such as projectile-target characteristic, impact velocity, impact position, impact angle, overcome the localization of the NASA model that only considers the impact velocity and mass of projectile and target. The result indicates that the paper model is effective and feasible, having important engineering reference value.
VI. CONCLUSIONS

(1) Establishing the average fragment size model depending on strain rate, according with Poisson statistic, fragments are discrete and distribution model is set up;
(2) On the foundation of the constitution analysis for the space target and projectile, both the target and projectile equivalent model is established;
(3) The length and velocity degraded model is set up against the cylindrical projectile;
(4) Choosing typical case, Comparing the paper model, NASA model simulation data and SSN surveillance data, the paper model is validated.

The objective of the paper is to establish an effective and feasible engineering model for the impact breakup of the space target, the simulation case indicates that the goal is achieved and the paper model has important engineering reference value. Next step combing with the projectile-target interaction model the relation between impact parameters and impact effect will be studied, and the model can be further modified.

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