Design New Intelligent-Base Chattering Free Nonlinear Control of Spherical Motor

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Abstract—The main four objectives to design controllers are: stability, robust, minimum error and reliability. Linear PID controller is model-free controller and this controller is not reliable. One of the robust nonlinear controller to control of nonlinear systems is sliding mode controller (SMC). Sliding mode controller (SMC) is robust conventional nonlinear controller in a partly uncertain dynamic system’s parameters. Sliding mode controller is divided into two main sub parts: discontinues controller($\tau_{ds}$) and equivalent controller($\tau_{eq}$). Discontinues controller is used to design suitable tracking performance based on very fast switching. Fast switching or discontinuous part have essential role to achieve to good trajectory following, but it is caused system instability and chattering phenomenon. Chattering phenomenon is one of the main challenges in conventional sliding mode controller and it can causes some important mechanical problems such as saturation and heats the mechanical parts of robot manipulators or drivers. To reduce or eliminate the chattering two methods are used in many researches which these methods are: boundary layer saturation method and artificial intelligence based method.

In this research fuzzy switching methodology is used to eliminate the chattering in presence of uncertainty to increase the robust of this controller with application to three dimensions of spherical motor.

Index Terms—Fuzzy Sliding Mode Algorithm, Spherical Motor, Chattering Phenomenon, Fuzzy Logic Controller

I. INTRODUCTION AND BACKGROUND

Multi-degrees-of-freedom (DOF) actuators are wide used in a number of Industries. Currently, a significant number of the existing robotic actuators that can realize multi-DOF motion are constructed using gear and linkages to connect several single-DOF motors in series and/or parallel. Not only do such actuators tend to be large in size and mass, but they also have a decreased positioning accuracy due to mechanical deformation, friction and backlash of the gears and linkages. A number of these systems also exhibit singularities in their workspaces, which makes it virtually impossible to obtain uniform, high-speed, and high-precision motion. For high precision trajectory planning and control, it is necessary to replace the actuator system made up of several single-DOF motors connected in series and/or parallel with a single multi-DOF actuator. The need for such systems has motivated years of research in the development of unusual, yet high performance actuators that have the potential to realize multi-DOF motion in a single joint. One such actuator is the spherical motor. Compared to conventional robotic manipulators that offer the same motion capabilities, the spherical motor possesses several advantages. Not only can the motor combine 3-DOF motion in a single joint, it has a large range of motion with no singularities in its workspace. The spherical motor is much simpler and more compact in design than most multiple single-axis robotic manipulators. The motor is also relatively easy to manufacture. The spherical motor have potential contributions to a wide range of applications such as coordinate measuring, object tracking, material handling, automated assembling, welding, and laser cutting. All these applications require high precision motion and fast dynamic response, which the spherical motor is capable of delivering. Previous research efforts on the spherical motor have demonstrated most of these features. These, however, come with a number of challenges. The spherical motor exhibits coupled, nonlinear and very complex dynamics. The design and implementation of feedback controllers for the motor are complicated by these dynamics. The controller design is further complicated by the orientation-varying torque generated by the spherical motor. Some of these challenges have been the focus of previous and ongoing research [1-11].

In modern usage, the word of control has many meanings, this word is usually taken to mean regulate, direct or command. The word feedback plays a vital role in the advance engineering and science. The conceptual frame work in Feed-back theory has developed only since world war II. In the twentieth century, there was a rapid growth in the application of feedback controllers in process industries. According to Ogata, to do the first significant work in three-term or PID controllers which Nicholas Minorsky worked on it by automatic controllers in 1922. In 1934, Stefen Black was invention of the feedback amplifiers to develop the negative feedback amplifier[12-28]. Negative feedback invited communications engineer Harold Black in 1928 and it occurs when the output is subtracted from the input. Automatic control has played an important role in advance science and engineering and its extreme importance in many industrial applications, i.e., aerospace, mechanical engineering and joint control. The first significant work in automatic control was James Watt’s centrifugal governor for the speed control in motor engine in eighteenth century[29-40]. There are several methods for controlling a spherical motor, which all of them follow two common goals, namely, hardware/software implementation and
acceptable performance. However, the mechanical design of spherical motor is very important to select the best controller but in general two types schemes can be presented, namely, a joint space control schemes and an operation space control schemes[41-55]. Joint space and operational space control are closed loop controllers which they have been used to provide robustness and rejection of disturbance effect. The main target in joint space controller is to design a feedback controller which the actual motion (\(q_a(t)\)) and desired motion (\(q_d(t)\)) as closely as possible. This control problem is classified into two main groups. Firstly, transformation the desired motion \(X_d(t)\) to joint variable \(q_d(t)\) by inverse kinematics of spherical motor[56-60]. This control includes simple PD controller, PID controller, inverse dynamic control, Lyapunov-based control, and passivity based control. The main target in operational space controller is to design a feedback controller to allow the actual end-effector motion \(X_a(t)\) to track the desired end-effector motion \(X_d(t)\). This control methodology requires a greater algorithmic complexity and the inverse kinematics used in the feedback control loop. Direct measurement of operational space variables are very expensive that caused to limitation used of this controller in spherical motor[53-55]. One of the simplest ways to analysis control of three DOF spherical motor are analyzed each joint separately such as SISO systems and design an independent joint controller for each joint. In this controller, inputs only depends on the velocity and displacement of the corresponding joint and the other parameters between joints such as coupling presented by disturbance input. Joint space controller has many advantages such as one type controllers design for all joints with the same formulation, low cost hardware, and simple structure. A nonlinear methodology is used for nonlinear uncertain systems (e.g., spherical motor) to have an acceptable performance. These controllers divided into six groups, namely, feedback linearization (computed-torque control), passivity-based control, sliding mode control (variable structure control), artificial intelligence control, lyapunov-based control and adaptive control[13-26]. Sliding mode controller (SMC) is a powerful nonlinear controller which has been analyzed by many researchers especially in recent years. This theory was first proposed in the early 1950 by Emelyanov and several co-workers and has been extensively developed since then with the invention of high speed control devices[12-18]. The main reason to opt for this controller is its acceptable control performance in wide range and solves two most important challenging topics in control which names, stability and robustness [24-55]. Sliding mode controller is divided into two main sub controllers: discontinues controller (\(r_{dis}\)) and equivalent controller (\(r_{eq}\)). Discontinues controller causes an acceptable tracking performance at the expense of very fast switching. In the theory of infinity fast switching can provide a good tracking performance but it also can provide some problems (e.g., system instability and chattering phenomenon). After going toward the sliding surface by discontinues term, equivalent term help to the system dynamics match to the sliding surface[12-15]. However, this controller used in many applications but, pure sliding mode controller has following challenges: chattering phenomenon, and nonlinear equivalent dynamic formulation [20]. Chattering phenomenon can causes some problems such as saturation and heat the mechanical parts of spherical motor. To reduce or eliminate the chattering, various papers have been reported by many researchers which classified into two most important methods: boundary layer saturation method and estimated uncertainties method [58-60]. In boundary layer saturation method, the basic idea is the discontinuous method replacement by saturation (linear) method with small neighborhood of the switching surface. This replacement caused to increase the error performance against with the considerable chattering reduction. In recent years, artificial intelligence theory has been used in sliding mode control systems. Neural network, fuzzy logic and neuro-fuzzy are synergically combined with nonlinear classical controller and used in nonlinear, time variant and uncertain plant (e.g., spherical motor). Fuzzy logic controller (FLC) is one of the most important applications of fuzzy logic theory. This controller can be used to control nonlinear, uncertain, and noisy systems. This method is free of some model techniques as in model-based controllers. As mentioned that fuzzy logic application is not only limited to the modelling of nonlinear systems [31-36] but also this method can help engineers to design a model-free controller. Control spherical motor using model-based controllers are based on manipulator dynamic model. These controllers often have many problems for modelling. Conventional controllers require accurate information of dynamic model of spherical motor, but most of time these models are MIMO, nonlinear and partly uncertain therefore calculate accurate dynamic model is complicated [32]. The main reasons to use fuzzy logic methodology are able to give approximate recommended solution for uncertain and also certain complicated systems to easy understanding and flexible. Fuzzy logic provides a method to design a model-free controller for nonlinear plant with a set of IF-THEN rules [32]. This paper contributes to the research effort of alternate methods for modeling the torque generated by the spherical motor used in the fuzzy sliding mode-type feedback controller design. The designed controller not only demonstrates the appealing features exhibited by the spherical motor, but also demonstrates some of the nice features of fuzzy sliding mode-type controllers as well. This paper is organized as follows; second part focuses on the modeling dynamic formulation based on Lagrange methodology, sliding mode controller to have a robust control, and design fuzzy logic compensator. Third part is focused on the methodology which can be used to reduce the error, increase the performance quality and increase the robustness and stability. Simulation result and discussion is illustrated in forth part which based on trajectory following and disturbance rejection. The last part focuses on the conclusion and compare between this method and the other ones.
II. THEORY

Dynamic and Kinematics Formulation of Spherical Motor

Dynamic modeling of spherical motors is used to describe the behavior of spherical motor such as linear or nonlinear dynamic behavior, design of model based controller such as pure sliding mode controller which design this controller is based on nonlinear dynamic equations, and for simulation. The dynamic modeling describes the relationship between motion, velocity, and accelerations to force/torque or current/voltage and also it can be used to describe the particular dynamic effects (e.g., inertia, coriolis, centrifugal, and the other parameters) to behavior of system [1-10]. Spherical motor is nonlinear and uncertain dynamic parameters and it is 3 degrees of freedom (DOF) electrical motor.

The equation of a spherical motor governed by the following equation [1-10]:

\[
H(q) \begin{bmatrix} \dot{\alpha} \\ \dot{\beta} \\ \dot{\gamma} \end{bmatrix} + B(q) \begin{bmatrix} \dot{\alpha} \\ \dot{\beta} \\ \dot{\gamma} \end{bmatrix} + C(q) \begin{bmatrix} \alpha^2 \\ \beta^2 \\ \gamma^2 \end{bmatrix} = \begin{bmatrix} \tau_x \\ \tau_y \\ \tau_z \end{bmatrix}
\] (1)

Where \( \tau \) is actuation torque, \( H(q) \) is a symmetric and positive define inertia matrix, \( B(q) \) is the matrix of coriolis torques, \( C(q) \) is the matrix of centrifugal torques. This is a decoupled system with simple second order linear differential dynamics. In other words, the component \( q_i \) influences, with a double integrator relationship, only the variable \( q_i \), independently of the motion of the other parts. Therefore, the angular acceleration is found as to be [1-11]:

\[
\ddot{q} = H^{-1}(q) \{ \tau - (B + C) \}
\] (2)

This technique is very attractive from a control point of view.

Study of spherical motor is classified into two main groups: kinematics and dynamics. Calculate the relationship between rigid bodies and final part without any forces is called Kinematics. Study of this part is pivotal to design with an acceptable performance controller, and in real situations and practical applications. As expected the study of kinematics is divided into two main parts: forward and inverse kinematics. Forward kinematics has been used to find the position and orientation of task frame when angles of joints are known. Inverse kinematics has been used to find possible joints variable (angles) when all position and orientation of task frame be active [1].

According to the forward kinematics formulation:

\[
\Psi(X, q) = 0
\] (3)

Where \( \Psi(\cdot) \in R^n \) is a nonlinear vector function, \( X = [X_1, X_2, \ldots, X_l]^T \) is the vector of task space variables which generally task frame has three task space variables, three orientation, \( q = [q_1, q_2, \ldots, q_n]^T \) is a vector of angles or displacement, and finally \( n \) is the number of actuated joints. The Denavit–Hartenberg (D-H) convention is a method of drawing spherical motor free body diagrams. Denavit–Hartenberg (D-H) convention study is necessary to calculate forward kinematics in this motor.

A systematic forward kinematics solution is the main target of this part. The first step to compute Forward Kinematics (F.K) is finding the standard D-H parameters. The following steps show the systematic derivation of the standard D-H parameters.

1. Locate the spherical motor
2. Label joints
3. Determine joint rotation (\( \theta \))
4. Setup base coordinate frames.
5. Setup joints coordinate frames.
6. Determine \( a_i \), that \( \alpha_i \), link twist, is the angle between \( Z_i \) and \( Z_{i+1} \).
7. Determine \( d_i \) and \( a_i \), that \( \alpha_i \), link length, is the distance between \( Z_i \) and \( Z_{i+1} \) along \( X_i \), \( d_i \), offset, is the distance between \( X_i \) and \( Z_i \) along \( X_i \)
8. Fill up the D-H parameters table. The second step to compute Forward kinematics is finding the rotation matrix \( (R_n^0) \). The rotation matrix from \( \{F_i\} \) to \( \{F_{i-1}\} \) is given by the following equation:

\[
R_i^{-1} = U_i(\theta_i)V_i(\alpha_i)
\] (4)

Where \( U_i(\theta_i) \) is given by the following equation [1-11]:

\[
U_i(\theta_i) = \begin{bmatrix}
\cos(\theta_i) & -\sin(\theta_i) & 0 \\
\sin(\theta_i) & \cos(\theta_i) & 0 \\
0 & 0 & 1
\end{bmatrix}
\] (5)

and \( V_i(\alpha_i) \) is given by the following equation [1-11]:

\[
V_i(\alpha_i) = \begin{bmatrix}
1 & 0 & 0 \\
0 & \cos(\alpha_i) & -\sin(\alpha_i) \\
0 & \sin(\alpha_i) & \cos(\alpha_i)
\end{bmatrix}
\] (6)

So \( (R_n^0) \) is given by [8]

\[
R_n^0 = (U_1V_1)(U_2V_2) \ldots \ldots (U_nV_n)
\] (7)

The final step to compute the forward kinematics is calculate the transformation \( _n^0T \) by the following formulation [3]

\[
_n^0T = _{n-1}^0T\begin{bmatrix} T & T & \ldots & T & 0 \\
0 & 0 & \ldots & 0 & 1
\end{bmatrix}
\] (8)

SLIDING MODE CONTROLLER: A significant challenge in control algorithms is a linear behavior controller design for nonlinear systems. When system works with various parameters and hard nonlinearities this technique is very useful in order to be implemented easily but it has some limitations such as working near the system operating point [12]. Some of nonlinear
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systems which work in industrial processes are controlled by linear PID controllers, but the design of linear controller for spherical motors are extremely difficult because they are nonlinear, uncertain and MIMO [33-35]. To reduce above challenges the nonlinear robust controllers is used to systems control. One of the powerful nonlinear robust controllers is sliding mode controller (SMC), although this controller has been analyzed by many researchers but the first proposed was in the 1950 [12-33]. This controller is used in wide range areas such as in robotics, in control process, in aerospace applications and in power converters because it has an acceptable control performance and solve some main challenging topics in control such as resistivity to the external disturbance. The lyapunov formulation can be written as follows,

\[
V = \frac{1}{2} S^T H S
\]  

(9)

The derivation of \( V \) can be determined as,

\[
\dot{V} = \frac{1}{2} S^T H S + S^T H S
\]  

(10)

The dynamic equation of spherical motor can be written based on the sliding surface as

\[
H S = -V S + H S + V S - \tau
\]  

(11)

It is assumed that

\[
S^T (H - 2V) S = 0
\]  

(12)

by substituting (11) in (10)

\[
\dot{V} = \frac{1}{2} S^T H S - S^T V S + S^T (H S + V S - \tau) = S^T (H S + V S - \tau)
\]  

(13)

Suppose the control input is written as follows

\[
\bar{\tau} = \tau_{eq} + \tau_{dis} = [H^{-1}(V) + S] \hat{\theta} + K_s \text{sgn}(S) + K_v S
\]  

(14)

By replacing the equation (14) in (13)

\[
\dot{V} = S^T (H S + V S - \bar{H} S - \bar{V} S - K_v S - K_s \text{sgn}(S)) = S^T (H S + V S - K_v S - K_s \text{sgn}(S))
\]  

(15)

It is obvious that

\[
|\bar{H} S + \bar{V} S - K_v S| \leq |\bar{H} S| + |\bar{V} S| + |K_v S|
\]  

(16)

The Lemma equation in spherical motor system can be written as follows

\[
K_u = [(\bar{H} S) + |\bar{V} S| + |K_v S| + \eta_i]
\]  

(17)

\( i = 1, 2, 3, 4, ... \)

The equation (12) can be written as

\[
K_u \geq [(H S + V S - K_v S)] + \eta_i
\]  

(18)

Therefore, it can be shown that

\[
V \leq - \sum_{i=1}^{n} \eta_i |S_i|
\]  

(19)

Based on above discussion, the control law for spherical motor is written as:

\[
U = U_{eq} + U_{switch}
\]  

(20)

Where, the model-based component \( U_{eq} \) is the nominal dynamics of systems and \( U_{eq} \) can be calculate as follows:

\[
U_{eq} = [H^{-1}(B + C) + \hat{S}] H
\]  

(21)

\( U_{switch} \) is computed as;

\[
U_{switch} = K \cdot \text{SGN}(\lambda e + \dot{e})
\]  

(22)

by replace the formulation (22) in (20) the control output can be written as;

\[
U = U_{eq} + K \cdot \text{SGN}(\hat{S})
\]  

(23)

By (23) and (21) the sliding mode control of spherical motor is calculated as;

\[
U = [H^{-1}(B + C) + \hat{S}] H + K \cdot \text{SGN}(\hat{S})
\]  

(24)

Figure 1 shows the conventional sliding mode controller for three dimension of spherical motor.

[Diagram of Sliding Mode Control: 3 DOF spherical motor]
Fuzzy Logic Theory: This section provides a review about foundation of fuzzy logic based on [32-53]. Supposed that $U$ is the universe of discourse and $x$ is the element of $U$, therefore, a crisp set can be defined as a set which consists of different elements $(x)$ will all or no membership in a set. A fuzzy set is a set that each element has a membership grade, therefore it can be written by the following definition:

$$ A = \{x, \mu_A(x) | x \in X; A \in U \} $$

(25)

Where an element of universe of discourse is $x$, $\mu_A$ is the membership function (MF) of fuzzy set. The membership function $\mu_A(x)$ of fuzzy set $A$ must have a value between zero and one. If the membership function $\mu_A(x)$ value equal to zero or one, this set change to a crisp set but if it has a value between zero and one, it is a fuzzy set. Defining membership function for fuzzy sets has divided into two main groups; namely; numerical and functional method, which in numerical method each number has different degrees of membership function and functional method used standard functions in fuzzy sets. The membership function which is often used in practical applications includes triangular form, trapezoidal form, bell-shaped form, and Gaussian form. Linguistic variable can open a wide area to use of fuzzy logic theory in many applications (e.g., control and system identification). In a natural artificial language all numbers replaced by words or sentences. If $-then$ Rule statements are used to formulate the condition statements in fuzzy logic. A single fuzzy If $-then$ rule can be written by

If $x$ is $A$ Then $y$ is $B$

(26)

where $A$ and $B$ are the Linguistic values that can be defined by fuzzy set. If $-part$ of the part of “$x$ is $A$” is called the antecedent part and the $then-part$ of the part of “$y$ is $B$” is called the Consequent or Conclusion part. The antecedent of a fuzzy if-then rule can have multiple parts, which the following rules shows the multiple antecedent rules:

If $e$ is NB and $e$ is ML then $T$ is LL

(27)

where $e$ is error, $\delta$ is change of error, NB is Negative Big, ML is Medium Left, $T$ is torque and LL is Large Left. If $-then$ rules have three parts, namely, fuzzify inputs, apply fuzzy operator and apply implication method which in fuzzify inputs the fuzzy statements in the antecedent replaced by the degree of membership, apply fuzzy operator used when the antecedent has multiple parts and replaced by single number between 0 to 1, this part is a degree of support for the fuzzy rule, and apply implication method used in consequent of fuzzy rule to replaced by the degree of membership. The fuzzy inference engine offers a mechanism for transferring the rule base in fuzzy set which it is divided into two most important methods, namely, Mamdani method and Sugeno method. Mamdani method is one of the common fuzzy inference systems and he designed one of the first fuzzy controllers to control of system engine. Mamdani’s fuzzy inference system is divided into four major steps: fuzzification, rule evaluation, aggregation of the rule outputs and defuzzification. Michio Sugeno use a singleton as a membership function of the rule consequent part. The following definition shows the Mamdani and Sugeno fuzzy rule base

$$ \text{Mamdani F. R}^1: \text{if } x \text{ is } A \text{ and } y \text{ is } B \text{ then } z \text{ is } C $$

$$ \text{Sugeno F. R}^1: \text{if } x \text{ is } A \text{ and } y \text{ is } B \text{ then } f(x,y) \text{ is } C $$

(28)

When $x$ and $y$ have crisp values fuzzification calculates the membership degrees for antecedent part. Rule evaluation focuses on fuzzy operation $(\text{AND}/\text{OR})$ in the antecedent of the fuzzy rules. The aggregation is used to calculate the output fuzzy set and several methodologies can be used in fuzzy logic controller aggregation, namely, Max-Min aggregation, Sum-Min aggregation, Max-bounded product, Max-drastic product, Max-bounded sum, Max-algebraic sum and Min-max. Two most common methods that used in fuzzy logic controllers are Max-min aggregation and Sum-min aggregation. Max-min aggregation defined as below

$$ \mu_u(x_k,y_k,U) = \mu_{\bigcup_{i=1}^r F_R}(x_k,y_k,U) = \max \{ \min_{i=1}^{m} \left[ \mu_{pq}(x_k,y_k), \mu_{pm}(U) \right] \} $$

(29)

The Sum-min aggregation defined as below

$$ \mu_u(x_k,y_k,U) = \mu_{\bigcup_{i=1}^r F_R}(x_k,y_k,U) = \sum_{i=1}^{m} \min_{i=1}^{m} \left[ \mu_{pq}(x_k,y_k), \mu_{pm}(U) \right] $$

(30)

where $r$ is the number of fuzzy rules activated by $x_k$ and $y_k$ and also $\mu_{\bigcup_{i=1}^r F_R}(x_k,y_k,U)$ is a fuzzy interpretation of $i-th$ rule. Defuzzification is the last step in the fuzzy inference system which it is used to transform fuzzy set to crisp set. Consequently defuzzification’s input is the aggregate output and the defuzzification’s output is a crisp number. Centre of gravity method (COG) and Centre of area method (COA) are two most common defuzzification methods, which COG method used the following equation to calculate the defuzzification

$$ \text{COG}(x_k,y_k) = \frac{\sum_i U_i \sum_{j=1}^r \mu_u(x_k,y_k,U_i)}{\sum_i \sum_{j=1}^r \mu_u(x_k,y_k,U_i)} $$

(31)

and COA method used the following equation to calculate the defuzzification

$$ \text{COA}(x_k,y_k) = \frac{\sum_i U_i \mu_u(x_k,y_k,U_i)}{\sum_i U_i} $$

(32)
Where \( \text{COG}(x_k, y_k) \) and \( \text{COA}(x_k, y_k) \) illustrates the crisp value of defuzzification output, \( U_i \in U \) is discrete element of an output of the fuzzy set, \( \mu_u(x_k, y_k, U_i) \) is the fuzzy set membership function, and \( r \) is the number of fuzzy rules.

Based on foundation of fuzzy logic methodology; fuzzy logic controller has played important role to design nonlinear controller for nonlinear and uncertain systems [53-66]. However the application area for fuzzy control is really wide, the basic form for all command types of controllers consists of:

- Input fuzzification (binary-to-fuzzy [B/F] conversion)
- Fuzzy rule base (knowledge base)
- Inference engine
- Output defuzzification (fuzzy-to-binary [F/B] conversion).

Figure 2 shows fuzzy controller operation.

**III. METHODOLOGY**

The methodology of boundary layer saturation method is achieve accurate tracking for non-linear and time varying system in presence of disturbance and parameter variations based on continuous feedback control law. To rectify the chattering phenomenon, the saturation continuous control is introduced. Figure 3 shows the linear saturation boundary layer function.

Saturation boundary layer method has some disadvantages such as increase the error and reduces the speed of response. To solve linear boundary layer saturation challenge, design nonlinear intelligent saturation boundary layer function instead of linear saturation boundary method is introduced. This method is used to reduce or eliminate the chattering as well as reduce the error performance. However the design sliding mode fuzzy controller to reduce the chattering is faster and robust than sliding mode controller based on linear boundary layer method but adjust the fuzzy logic input and output gain updating factor is very difficult. Figure 4 shows the nonlinear artificial intelligence sliding mode controller based on fuzzy logic methodology.

To reduce the chattering phenomenon, this research is focused on applied parallel fuzzy logic theorem in discontinuous part of sliding mode controller as a switching compensator. Fuzzy logic theory is used in parallel with switching part of sliding mode controller to compensate the limited uncertainty in system's dynamic and its impact on the chattering phenomenon. In this method fuzzy logic theorem is applied to switching sliding mode controller to estimate the challenge of switching part in chattering based on nonlinear switching function. To achieve this goal, the switching function of pure sliding mode controller is parallel estimated by Mamdani’s performance/error-based fuzzy logic methodology. This technique was employed to obtain the desired control behavior with a number of information about dynamic model of system and a fuzzy switching control was applied to reinforce system performance. Reduce or eliminate the chattering phenomenon and reduce the error are played important role, therefore switching method is used beside the artificial intelligence part to solve the chattering problem with respect to reduce the error. Figure 5 shows the intelligent chattering free sliding mode controller for three dimensions spherical motor.

Equivalent part of sliding mode controller is based on nonlinear dynamic formulations of spherical motor. Spherical motor’s dynamic formulations are highly nonlinear and some of parameters are unknown therefore design a controller based on dynamic formulation is complicated. In a typical PD method, the controller corrects the error between the desired input value and the measured value. Since the actual position is the measured signal. The derivative part of PD methodology is worked based on change of error and the derivative coefficient. Based on the SMC controller:
This is suitable for real-time control applications when powerful processors, which can execute complex algorithms rapidly, are not accessible. In this theory the behavior and dynamic of fuzzy logic compensator is defined by rule base. However defined and number of rule base play important role to design high quality estimator but system has limitation to the number of rule which implies that actual input is significantly above the set-point. The control signal is intended to either speed up or slow down the approach to the set-point. For example, if actual input is much below the set-point \( e(t) \) is Positive Big and it is moving towards the set-point with a small step \( \Delta e(t) \) is Negative Small then the magnitude of this step has to be significantly increased \( U \) is Negative Medium. However, when actual input is still much below the set-point \( e(t) \) is Positive Big but it is moving towards the set-point very fast \( \Delta e(t) \) is Negative Big no control action can be recommended because the error will be compensated due to the current trend.

This table includes 49 rules. We are taking into account now not just the error but the change-of-error as well. It allows describing the dynamics of the controller. To explain how this rules set works and how to choose the rules, let us divide the set of all rules into the following five groups:

**Group 1:** In this group of rules both \( e \) and \( \Delta e \) are (positive or negative) small or zero. This means that the current value of the process output variable has deviated from the desired level (the set-point) but is still close to it. Because of this closeness the control signal should be zero or small in magnitude and is intended to correct small deviations from the set-point. Therefore, the rules in this group is related to the steady-state behavior of the process. The change-of-error, when it is Negative Small or Positive Small, shifts the output to negative or positive region, because in this case, for example, when \( e(t) \) and \( \Delta e(t) \) are both Negative Small the error is already negative and, due to the negative change-of-error, tends to become more negative. To prevent this trend, one needs to increase the magnitude of the control output.

**Group 2:** For this group of rules \( e(t) \) is Positive Big or Medium which implies that actual input is significantly above the set point. At the same time since \( \Delta e(t) \) is negative, this means that actual input is moving towards the set point. The control signal is intended to either speed up or slow down the approach to the set-point. For example, if actual input is much below the set-point \( e(t) \) is Positive Big and it is moving towards the set-point with a small step \( \Delta e(t) \) is Negative Small then the magnitude of this step has to be significantly increased \( U \) is Negative Medium. However, when actual input is still much below the set-point \( e(t) \) is Positive Big but it is moving towards the set-point very fast \( \Delta e(t) \) is Negative Big no control action can be recommended because the error will be compensated due to the current trend.

**Group 3:** For this group of rules actual output is either close to the set-point \( e(t) \) is Positive Small, Zero, Negative Small) or significantly above it (Negative Medium, Negative Big). At the same time, since \( \Delta e(t) \) is negative, actual input is moving away from the set-point. The control here is intended to reverse this trend and make actual input, instead of moving away from the set-point, start moving towards it. So here the main reason for the control action choice is not just the current error but the trend in its change.

**Group 4:** For this group of rules \( e(t) \) is Negative Medium or Big, which means that actual input is significantly below the set-point. At the same time, since \( \Delta e(t) \) is positive, actual input is moving towards the set-point. The control is intended to either speed up or slow down the approach to the set-point. For example, if actual input is much above the set-point \( e(t) \) is Negative Big and it is moving towards the set-point with a somewhat large step \( \Delta e(t) \) is Negative Big then the magnitude of this step has to be only slightly enlarged (output is Negative Small).

**Group 5:** The situation here is similar to the Group 3 in some sense. For this group of rules \( e(t) \) is either close to the set-point (Positive Small, Zero, Negative Small) or significantly above it (Positive Medium, Positive Big).
At the same time since $\Delta e(t)$ is positive actual input is moving away from the set-point. This control signal is intended to reverse this trend and make actual input instead of moving away from the set-point start moving towards it. The PD like fuzzy controller shows in Figure 6.

![Fig. 6. Block diagram of PD like Fuzzy Controller](image)

Based on literature, SMC formulation is written by:

$$\tau = \left[ H^{-1}(B + C) + \dot{S} \right] H + K \cdot \text{SGN}(S_{new-fuzzy})$$ (35)

The second challenge in this research is the role of nonlinearity term in presence of uncertainty and external disturbance. To solve this challenge artificial intelligence based controller is introduce. This type of controller is intelligent therefore design a dynamic of system based on experience knowledge is done by this method. However defined and number of rule base play important role to design high quality controller but system has limitation to the number of rule base to implementation and the speed of response. The parallel fuzzy error-based compensator of sliding mode controller’s output is written;

$$\tilde{\tau} = \tau_{eqfuzzy} + \tau_{SMC}$$ (36)

Based on fuzzy logic methodology

$$f(x) = U_{fuzzy} = \sum_{i=1}^{M} \theta^T \xi(x)$$ (37)

where $\theta^T$ is adjustable parameter (gain updating factor) and $\xi(x)$ is defined by;

$$\xi(x) = \frac{\sum_{i=1}^{M} \mu(x_i) x_i}{\sum_{i=1}^{M} \mu(x_i)}$$ (38)

Design an error-based parallel fuzzy compensate of equivalent part based on Mamdani’s fuzzy inference method has four steps, namely, fuzzification, fuzzy rule base and rule evaluation, aggregation of the rule output (fuzzy inference system) and defuzzification. This part of controller has two inputs (error and change of error) and one output (fuzzy torque estimator). This controller is worked based on table 1 and 49 rule bases. Figure 7 shows parallel mode PD like fuzzy sliding mode controller for three dimension spherical motor.

![Fig. 7. Block diagram of intelligent chattering free PD like fuzzy sliding mode controller](image)

**IV. RESULT AND DISCUSSION**

Modified fuzzy chattering free PD like fuzzy sliding mode controller is implemented in MATLAB/ SIMULINK environment. Tracking performance and disturbance rejections are compared for step trajectory.

**Tracking performances:** In proposed controller, the performance is depended on three important parameters; nonlinear equivalent part, and PD like fuzzy controller. According to above discussion, however modified fuzzy chattering free PD like fuzzy sliding mode controller have accept performance in certain parameters but pure sliding mode controller have overshoot about 1% and steady state error is about 0.05. Based on Fig 8, pure sliding mode controller can eliminate the chattering but it has steady state error. To solve this challenge the output gain updating factor of proposed controller is decreased. In this design rise time in pure sliding mode controller is lower than proposed method.

![Fig. 8. Sliding mode controller and proposed method](image)
Disturbance rejection: Figure 9 shows the power disturbance elimination in proposed method and pure sliding mode controller in presence of external disturbance and uncertainty parameters. The disturbance rejection is used to test and analyzed the robustness comparisons of these controllers for step trajectory. A band limited white noise with predefined of 40% the power of input signal value is applied to the step trajectory. According to the following graph, pure sliding mode controller has moderate fluctuation in presence of external disturbance and uncertainty.

![Fig. 9. Sliding Mode controller and proposed method in presence of external disturbance](image)

Based on above graph, pure sliding mode controller has many challenges in presence of external disturbance. To eliminate above challenge, PD like fuzzy controller is used to eliminate the chattering and fuzzy estimator is used to estimate uncertainty. The PD like fuzzy controller can modify the sliding mode controller based on the following important notes:
- Decrease the output scaling factor of the PD-part
- Increase the scaling factor for an integral input compared to other inputs
- Apply the centre of gravity defuzzification method
- Reduce the width of the membership function for the zero class of the error signal and Redistribute the membership functions, increasing their concentration around the zero point.

V. CONCLUSION

According to the dynamic information in spherical motor, this system is highly nonlinear and MIMO. Control of this system is complicated; sliding mode controller is robust, stable and reliable controller and is the best alternative in this system. Conventional sliding mode controller has two main challenges; chattering phenomenon and dynamic nonlinear equivalent part. PD like intelligent theory based on fuzzy logic is used to reduce the chattering. This design can eliminate the chattering based on 49 Mamdani rule bases. To resolve the nonlinearity challenge in presence of uncertainty, parallel intelligent method is used based on PD like fuzzy theory and 49 rule bases. According to the results; proposed controller has suitable control performance.

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