Parameter Tuning via Genetic Algorithm of Fuzzy Controller for Fire Tube Boiler

Osama I. Hassanein
Faculty of Engineering, Sohaj University, Sohaj, Egypt
Email: osamhas_74@hotmail.com

Ayman A. Aly
Assistant Professor of Mechatronics Section, Mechanical Engineering, Faculty of Engineering, Assiut University, Assiut, Egypt
Currently: Faculty of Engineering, Taif University, Taif, Saudi Arabia
Email: draymanelnaggar@yahoo.com

Ahmed A. Abo-Ismail
Professor of Automatic control, Mechanical Engineering, Faculty of Engineering, Assiut University, Assiut, Egypt
Email: aabosmail@aun.edu.eg

Abstract—The optimal use of fuel energy and water in a fire tube boiler is important in achieving economical system operation, precise control system design required to achieve high speed of response with no overshoot. Two artificial intelligence techniques, fuzzy control (FLC) and genetic-fuzzy control (GFLC) applied to control both of the water/steam temperature and water level control loops of boiler. The parameters of the FLC are optimized to locating the optimal solutions to meet the required performance objectives using a genetic algorithm. The parameters subject to optimization are the width of the membership functions and scaling factors. The performance of the fire tube boiler that fitted with GFLC has reliable dynamic performance as compared with the system fitted with FLC.

Index Terms—Fire Tube Boiler, Fuzzy Logic Control, Genetic Algorithm.

I. INTRODUCTION

The fire tube boiler has been used extensively for the generation of energy in a wide range of industrial processes and heating applications. The requirements of an efficient boiler are that should generate maximum amount of steam at a required pressure, temperature and quality with minimum fuel consumption. To achieve optimal design, a precise control system design is required. Sufficient and trustworthy information about dynamics properties of the plant is the basis for successful control system design.

Boiler control is the regulating of the boiler outlet conditions of steam demand, pressure, and temperature to their desired values. At the same time, regulating boiler internal parameters such as water level is very important to keep the boiler safely. The quantities of fuel, air, and water are adjusted to obtain the desired steam demand and maintain the steam temperature and water level inside shell at their set point. The studies of dynamics of fire tube boilers and control systems have been studied rarely in the past. Only few simple lumped SISO models for domestic fire tube hot water heater appeared in literature [1], [2], [3], [4], and [5].

Unlike water tube boiler which has been studied extensively in the past [6], [7], [8], [9], [10], and [11]. The closed loop control problem of the process is investigated, where high static accuracy and high speed of response with no overshoot are required as a technical design criterion.

Different control policies such as Fuzzy control and Genetic-Fuzzy control can be applied and tested for applicability under certain operating conditions, or subjected to some constraints.

The theory of fuzzy sets [12] becomes a useful instrument for control engineer as the complexity of the system increases and the ability to understanding and predicts its behavior in a precise and yet significant manner diminishes.

Genetic algorithms are global, parallel, search and optimization methods; founded on Darwinian principles [13] and [14], which based on analogies to natural biological processes.

However, designing a robust control system, which provides performance specifications and guarantee closed loop stability irrespective to parameters variations is appraising target attracting many control designers and researchers.

The effect and viability of the Genetic-Fuzzy control system and comparison with conventional control
methods such as Fuzzy control are investigated by nonlinear dynamic model simulation.
The paper has been organized as follows: Section 2 describes the system dynamic model. Section 3 reviews the FLC tuning method. Section 4 presents the design method of GA while section 5 explains how GA can tune FLC. Section 6 illustrates the simulation results of the proposed controller. Finally, a conclusion of the proposed GFLC technique is presented in Section 7.

II. MATHEMATICAL MODEL

There are two feedback control loops, water/steam temperature control loop, and water level control loop. The schematic diagram for the fire tube boiler control system is shown in Fig. 1. In our case, the process is 2-input 2-output multivariable process with interaction between the two feedback closed loops. The input fuel flow rate \( \dot{m}_f \), will act as control for water/steam \( T_w \), but will act as a disturbance for water level \( hw \), where \( \dot{m}_f \) represents the feed water flow rate. Both control loop operate on its own and interacts with the other loops.

The first step in the analysis of a dynamic system is to drive its mathematical model of the plant. The dynamic model of a fire tube boiler [15] is considered, as previously derived, using heat transfer, mass balance, and heat balance equations, and can be modeled as:

\[
\dot{X} = Ax + Bu + Ef' + Y = Cx
\]

The state vector \( x \), the manipulated input vector \( u \), the output vector \( y \), and the disturbance input vector \( f' \) are defined as:\n\[
x = \begin{bmatrix} T_w & T_y \end{bmatrix}^T
\]
\[
u = \begin{bmatrix} \dot{m}_f & \dot{m}_w \end{bmatrix}^T
\]
\[
f' = \begin{bmatrix} \dot{m}_f & T_y \end{bmatrix}^T
\]
\[
y = \begin{bmatrix} F_y & h_y \end{bmatrix}^T
\]

The妮克 (defuzzified) control output values then is\n\[
A = \begin{bmatrix} C_0 + C_2 C_0 & C_0 + C_2 C_0 & 0 & 0 \\
M_0 C_0 & M_0 C_0 & 0 & 0 \\
C_0 & h_{m-Ac} C_0 & h_{m-Ac} C_0 & 0 \\
M_0 C_0 & M_0 C_0 & 0 & 0 \\
0 & C_0 C_0 + C_0 & C_0 (h_{m-Ac} + U + C_0) & 0 \\
C_0 C_0 + C_0 & C_0 (h_{m-Ac} + U + C_0) & 0 & 0 \\
0 & C_0 C_0 + C_0 & C_0 (h_{m-Ac} + U + C_0) & 0 \\
C_0 C_0 + C_0 & C_0 (h_{m-Ac} + U + C_0) & 0 & 0 \\
\end{bmatrix}
\]
\[
B = \begin{bmatrix}
C_1 - C_{12} - C_x C_{12} & 0 \\
0 & 0 \\
0 & 0 \\
0 & 0 \\
0 & C_1 - C_x & 0 \\
0 & 0 & 0 \\
0 & 0 & 0 \\
C_{12} C_{12} + C_{12} & C_{12} U & 0 \\
C_{12} C_{12} + C_{12} & C_{12} U & 0 \\
C_{12} C_{12} + C_{12} & C_{12} U & 0 \\
C_{12} C_{12} + C_{12} & C_{12} U & 0 \\
\end{bmatrix}
\]
\[
E = \begin{bmatrix}
0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 \\
\end{bmatrix}
\]
\[
and C = \begin{bmatrix} 0 & 0 & 1 & 0 \\
0 & 0 & 0 & 1 \\
\end{bmatrix}
\]

III. FUZZY LOGIC CONTROLLER

The main idea of the fuzzy logic controller (FLC) is the measured value is a crisp quantity fuzzified into a fuzzy set. This fuzzy output is then conceded as the fuzzy input into a fuzzy controller, which is consisted of linguistic rules. The output of the fuzzy controller is then another series of fuzzy sets. Since most physical system cannot interbreed fuzzy commands (Fuzzy Sets), the fuzzy controller output must be converted into crisp quantities using defuzzification methods.

The crisp (defuzzified) control output values then become the input values to the physical system and entire closed loop cycle is repeated. As shown in Fig. 2, the control inputs \( u \) derive the process variables \( y \) for both control loops.
A. Water/steam temperature control loop

For temperature fuzzy logic controller, we use a Mamdani fuzzy controller. The temperature error is fuzzified and will be used as the input to fuzzy controller. The membership functions for both input and output fuzzy variables are triangle shaped functions and symmetrical about zero [16], as shown in fig. 3.

The temperature error, “e”, will be fuzzified by five linguistic variables, “NL” stands for “negative large”, “NS” for “negative small”, “Z” for “zero”, “PS” for “positive small” and “PL” for “positive large”, partitioned on the error space. For the controller output, control quantity “z”, will be described by five linguistic variable labeled CLOSEFAST, CLOSESLOW, NOCHANGE, OPENSLOW, and OPENFAST partitioned on control universe.

A number of rules are used to model the way of the system behavior; fuzzy rules are constructed in the well-known IF-THEN form. Five fuzzy rules base used for the temperature fuzzy controller are

- IF (“e” is NL) THEN (“z” is CLOSEFAST).
- IF (“e” is NS) THEN (“z” is CLOSESLOW).
- IF (“e” is Z) THEN (“z” is NOCHANGE).
- IF (“e” is PS) THEN (“z” is OPENSLOW).
- IF (“e” is PL) THEN (“z” is OPENFAST).

A defuzzification method is required to transform fuzzy control output to a crisp value of the fuzzy logic controller. For the temperature FLC, a widely used defuzzification method is the “center of area”. 

At each time step, the FLC examines the change in water/steam temperature from the set point, temperature error, these data are crisp quantity, and must be fuzzified and given as input to inference engine. Utilizing the current set of rules, a fuzzy control output representing the change in fuel flow rate is defuzzified and applied to the plant.

B. Water level control loop

For level fuzzy logic controller, we use a Mamdani fuzzy controller. The level error fuzzified and will be used as the input to fuzzy controller. The membership functions for both input and output fuzzy variables are triangle shaped functions and symmetrical about zero [16], as shown in Fig. 4.

The level error, “e”, will be fuzzified by five linguistic variables, “NL” stands for “negative large”, “NS” for “negative small”, “Z” for “zero”, “PS” for “positive small” and “PL” for “positive large”, partitioned on the error space. For the controller output, control quantity “z”, will be described by five linguistic variable labeled CLOSEFAST, CLOSESLOW, NOCHANGE, OPENSLOW, and OPENFAST partitioned on control universe.

A number of rules are used to model the way of the system behavior; fuzzy rules are constructed in the well-known IF-THEN form. Five fuzzy rules base used for the level fuzzy controller are

- IF (“e” is NL) THEN (“z” is CLOSEFAST).
- IF (“e” is NS) THEN (“z” is CLOSESLOW).
- IF (“e” is Z) THEN (“z” is NOCHANGE).
- IF (“e” is PS) THEN (“z” is OPENSLOW).
- IF (“e” is PL) THEN (“z” is OPENFAST).

The fuzzy logic control rules were formulated trial and error by making correction to the rule base after examining the system response. The desired response was the quickest rise time with no overshoot and smooth damped rise. The large membership functions have a relatively small domain and are presented to deliver relatively large control inputs when the error is at extremes, this essential for the quick response time to the step input. The small membership functions have a relatively large domain and are presented to deliver relatively small control inputs when the error is around zero, this for no overshoot response.
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A defuzzification method is required to transform fuzzy control output to a crisp value of the fuzzy logic controller. For the level FLC, a widely used defuzzification method is the “center-of-area”.

At each time step, the FLC examines the change in water/steam level from the set point, temperature error, these data are crisp quantity, and must be fuzzified and given as input to inference engine. Utilizing the current set of rules, a fuzzy control output representing the change in fuel flow rate is defuzzified and applied to the plant.

In the fuzzy system, computational effort is spent in finding parameters that give a desired behavior to the system, while no attention is given to the structure of the system because the control engineer is looking for a good enough solution not necessary the optimum one. However, sometimes the parametric adjustment of the selected structure may be too poor.

Besides the large tuning time and the significant amount of wasted resources, the structure is too complex and the dimension of the problem increase unreasonably. Therefore, we will use optimization technique using Genetic algorithm to find the FLC parameter in order to save time and effort that spent in tuning the FLC parameter.

IV. THE GENETIC ALGORITHM

In any design problem there is a multi-dimensional space of possible solutions. Some of these solutions may be acceptable, but not the best (local optimum) and there may exist a single best solution (global optimum). An alternative approach is to use “heuristics” or knowledge required through experience, to search for optimal solutions. One such technique is to employ a Genetic Algorithm (GA) [13] and [14].

The GAs is global, parallel, search and optimization methods; founded on Darwinian principles; the evolution is based on two simple concepts of natural evolution: “survival of the fittest” and “reproduction the basic element of a GA is the “chromosome”. It contains the genetic information for a given solution and is typically coded as binary string. GA operates on a set (population) of strings (individuals that represents a particular solution of the problem), where each string has input data. Each string’s fitness (which expresses how good the solution is at solving the problem) is calculating using an objective function.

In GA terminology, each iteration of the search is called a “generation”. In each generation, taking advantage of the fittest individuals of the previous generation creates a new population.

GA is characterized by attributes such as objective function, encoding the input data, genetic operators, population size, and then the algorithm programming steps.

A. The objective and fitness function

The objective function is used to provide a measure of how individuals have performed in the problem domain. In the problem of a minimization problem (our case), the fit individuals will have the lowest numerical value of the associated problem objective function. This raw measure of fitness is usually only used an intermediate stage in determining the relative performance of individuals in a GA. Another Function, the fitness function, is normally used to transform the objective function value into a measure of relative fitness. A “fitness function”, which is in effect a performance index, is used to select the best solution in the population to be parents to the offsprings that will comprise the next generation. This emulates the evolutionary process of “survival of the fittest”.

\[ F(x) = g(f(x)) \]  (2)

Where “f” is the objective function, “g” transforms the value of the objective function (f(x)) to a non-negative number and “F” is the resulting relative fitness, in the current study (3) is the chosen fitness function. This mapping is always necessary when the objective function is to be minimized.

B. Encoding

In a GA, each solution must be encoded as a binary sequence, i.e., a sequence of 0's and 1's. GAs operates on an encoding of the problem’s input data. The choice of the encoding is extremely important for the execution performance of the algorithm. A poor encoding can lead to long running searches that do not produce good results.

C. GA operator

GAs features the following three basic operators, which are executed sequentially by the GA:

(1) Selection and reproduction.
(2) Crossover.
(3) Mutation.

During the process of Selection and reproduction, pairs of individuals are chosen from the population according to their fitness. The reproduction operator can be implemented in a number of ways. For our purpose, in this paper roulette wheel was considered. The “roulette wheel” mechanism is probabilistically select individuals based on some measure of their performance. A real-
valued interval, Sum, is determined as either the sum of the individuals’ expected selection probabilities or the sum of the raw fitness values over all the individuals in the current population. Individuals are then mapped one-to-one into contiguous intervals in the range \([0, \text{Sum}]\). The size of each individual interval corresponds to the fitness value of the associated individual.

For example, in Fig. 5, the circumference of the roulette wheel is the sum of all six individual’s fitness values. Individual 5 is the fit individual and occupies the largest interval, whereas individuals 6 and 4 are the least fit and have correspondingly smaller intervals within the roulette wheel. To select an individual, a random number is generated in the interval \([0, \text{Sum}]\) and the individual whose segment spans the random number is selected. This process is repeated until the desired number of individuals has been selected.

The basic roulette wheel selection method is stochastic sampling with replacement (SSR). Here, the segment size and selection probability remain the same throughout the selection phase and individuals are selected according to the procedure outlined above. SSR gives zero bias but a potentially unlimited spread. Any individual with a segment size > 0 could entirely fill the next population.

Crossover operators is used to combine the pairs of selected strings (parents) to create new strings (offspring) that potentially have a higher fitness than either of their parents. The crossover likes its counterpart in natural. Crossover operator can be implemented in a number of ways. For our purpose, the simplest recombination operator is that of single-point crossover. Consider the two parent binary strings as Fig. 6. If an integer position, I, is selected uniformly at random between 1 and the string length, L, minus one \([1, L-1]\), and the GA information exchanged between the individuals about this point, then two new offspring strings are produced. The two offspring below are produced when the crossover point \(I = 5\) is selected, this crossover operation is not necessarily performed on all strings in the population. Instead, it is applied with a probability \(P_c\), when the pairs are chosen for breeding.

A further GA operator, called Mutation, is then applied to the new chromosomes, every string resulting from the crossover process; gain with a set probability, \(P_m\). Mutation causes the individual genetic representation to be changed according to some probabilistic rule. In the binary string representation, mutation will cause a single bit to change its state, \(0 \leftrightarrow 1\) or \(1 \leftrightarrow 0\), and modified elements in chromosomes. Therefore, for example, Fig. 7, mutating the third bit leads to the new string, Mutation is generally considered a background operator that ensures that the probability of searching a particular subspace of the problem space is never zero. Therefore, the mutation operator is crucial and providing a guarantee to avoid missing high fitness strings when the current population has converged to a local optimum.

d. Population size

The number of string in a population is defined by the population size. The larger the population size, the better the chance that an optimal solution will be found.

e. How the algorithm works?

GAs uses the operator defined above to operate on the population through an iterative process as shown in fig.8, the GA is terminated when some criteria are satisfied, e.g. a certain number of generations, a mean deviation in the population, or when a particular point in the search space
is encountered, in this paper we terminate the GA when the certain number of generations are satisfied.

V. GFLC CONTROLLER DESIGN

The GA used as an optimization technique to find the optimal FLC parameter, in Fig. 9, shows the technique of the GA works in tuning the FLC parameter. The objective function block used for calculating the FLC performance. The Genetic algorithm block used for finding the optimized FLC parameters to locating the optimal solution of the controller output “u” to meet the required specification of the process variable “y”. In this paper, we will apply the GA to optimize certain parameter of FLC, while leaving others fixed.

![Figure 9. The Structure of GA works on FLC (GFLC)](image)

In this work, our cost function that attempt to optimize the two-control loop, steam/water temperature control loop and water level control loop, keeping the interaction between them, is ISE (Integral of Square Error) for step input over the total simulation time.

\[
ISE = \frac{t}{t_0} \int_0^t e^2 dt
\]  

Suppose \( J_{TOTAL} \) is the overall performance index of the system, which is in the form for a two GFLC controller (four-controller parameter) as shown:

\[
J_T = f(C_{TI}, K_{Tot}) = \max(ISE)
\]

\[
J_L = f(C_{LI}, K_{Lout}) = \max(ISE)
\]

where \( J_T \) is the objective function for temperature controller and \( C_{TI}, K_{Tot} \) is the parameter “C” in the input membership function, and the output-scaling factor respectively for the temperature controller. Also \( J_L \) is the objective function for level controller and \( C_{LI}, K_{Lout} \) are the parameter “C” in the input membership function and the output-scaling factor respectively for level controller, and ISE is Integral of Square Error over the total simulation time.

In order to compatible with the normalization technique, each individual performance index should be dimensionless and represented in term of error for consistency as described below:

\[
FT = J_T / \text{sum}(J_T)
\]

\[
FL = J_L / \text{sum}(J_L)
\]

\[
F_{TOTAL} = 1 / (1 + (FT + FL))
\]

(5)

Where \( F_T \) is the temperature controller fitness, \( F_L \) is the level controller fitness and \( F_{TOTAL} \) is the overall fitness function of the system. The objective function using fitness produces uniformity from its normalized range [0,1]. In this study, the GFLC controller parameters are given by number of generation = 25, the good convergence was achieved in less than 14 generations. The population size = 100; the structure of the chromosome = \([C_{TI}, K_{Tot}, C_{LI}, K_{Lout}]\), 4-bit string elements were used for the encoding of each of the four parameters associated with the two GFLC controller, resulting in a total chromosome length of \([4 \times 4 = 16 \text{ bits}]\).

This results in a search space whose size is approximately 65.5X103 points. The method of selection is the roulette wheel method; crossover factor (P_x) = 0.9; mutation factor (P_m) = (0.7/ length of chromosome.

A. Water/steam temperature control loop

As illustrated previously we attempt to optimize the width of the membership function “Z” and “NOCHANGE” of the input and output membership function respectively and the output-scaling factor at the same time, while leaving other parameters fixed. The parameter “\( C_{TI} \)” was assumed to take values from the interval [5.0, 7.0], for keeping the membership function symmetrical about zero, this will lead to \( A_{TI} = - C_{TI} \) for “Z” membership function, \( C_{To} = 0.006 \times C_{TI} \), and \( A_{To} = - C_{To} \) for “NOCHANGE” membership function. The parameter “\( K_{Tot} \)” was assumed to take values from the interval [2.0, 8.0]. The result in membership functions is shown in Fig. 11.

b. Water level control loop

As illustrated previously we attempt to optimize the width of the membership function “Z” and “NOCHANGE” of the input and output membership function respectively and the output-scaling factor at the same time, while leaving other parameters fixed. The parameter “\( C_{LI} \)” was assumed to take values from the interval [0.003, 0.01], for keeping the membership function symmetrical about zero, this will lead to \( A_{LI} = - C_{LI} \) for “Z” membership function, \( C_{Lo} = 75 \times C_{LI} \), and \( A_{Lo} = - C_{Lo} \) for “NOCHANGE” membership function. The parameter “\( K_{Lout} \)” was assumed to take values from the interval [2.0, 15.0]. The result in membership functions shown in Fig. 12.
VI. SIMULATION RESULTS

A MATLAB program is conducted to simulate the dynamics of the plant by using Rung-Kutta fifth order method with tolerance $1 \times 10^{-5}$.

Figure 13, illustrate the variations in water/steam temperature and water level response due to step variation in water/steam set point (from 169 °C to 180 °C) for fire tube boiler at their nominal capacitance (water content inside shell) with FLC and GFLC controller. From water/steam temperature response Fig.13-a, shows that, with FLC controller, the temperature response is oscillatory; the maximum oscillation of temperature is 0.14 °C, reached zero steady state error at 132 sec. With GFLC controller, the temperature response is oscillatory; the maximum oscillation of temperature is 0.05 °C, reached zero steady state error at 20 sec. From water level response Fig. 14-a, shows that, With FLC controller, the 2% settling time, $t_s$, is 27 sec with no overshoot and zero steady state error at 98.5 sec. With GFLC controller, the 2% settling time, $t_s$, is 5.4 sec with zero overshoot and reached zero steady state error at 15 sec.

From water/steam temperature response Fig.14-a, shows that, with FLC controller, the temperature response is oscillatory; the maximum oscillation of temperature is 0.14 °C, reached zero steady state error at 132 sec. With GFLC controller, the temperature response is oscillatory; the maximum oscillation of temperature is 0.05 °C, reached zero steady state error at 20 sec. From water level response Fig. 14-b, shows that, With FLC controller, the 2% settling time, $t_s$, is 27 sec with no overshoot and zero steady state error at 98.5 sec. With GFLC controller, the 2% settling time, $t_s$, is 5.4 sec with zero overshoot and reached zero steady state error at 15 sec.

Figures 15-a and 15-b illustrate the water/steam temperature step response of water/steam temperature and water level control variable(output) during the process based on FLC and GFLC controller. Fig.16-a and Fig. 16-b illustrate the water level step response of water/steam temperature and water level control variable(output) respectively during the process based on FLC and GFLC controller.
VII. CONCLUSION

From the above results and discussion, it can be seen that the fire tube boiler that fitted with GFLC controller has a reliable dynamic performance as compared with the system fitted with traditional FLC controller. Therefore, The GA differs sensationally from more traditional search and optimization method. The four most significant differences are:

- GAs searches a population of points in parallel, not a single point.
- GAs require only the objective function and corresponding fitness levels, rather than traditional search and optimization method require the derivative information and other auxiliary knowledge.
- GAs based on probabilistic transition rules, not on deterministic rules.
- GAs not only works on the parameter but also on the encoding of the parameter itself. (Except in where real–valued individuals are used).

REFERENCES

Parameter Tuning via Genetic Algorithm of Fuzzy Controller for Fire Tube Boiler


NOMENCLATURE

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
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<tbody>
<tr>
<td>A_f</td>
<td>outer surface area of fire tube boiler, m²</td>
</tr>
<tr>
<td>A_v</td>
<td>heating surface area of fire tubes, m²</td>
</tr>
<tr>
<td>A_m</td>
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<tr>
<td>C</td>
<td>input matrix</td>
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<td>C_p</td>
<td>output matrix</td>
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<td>C_g</td>
<td>specific heat of fuel oil, kJ/kg °C</td>
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<td>specific heat of flue gas</td>
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</tr>
<tr>
<td>U</td>
<td>overall heat transfer coefficient, watt/m² °C</td>
</tr>
<tr>
<td>u_g</td>
<td>internal energy of combustion gases, kJ/kg</td>
</tr>
<tr>
<td>V_w</td>
<td>volume of water inside boiler, m³</td>
</tr>
<tr>
<td>V_o</td>
<td>volume of steam inside boiler, m³</td>
</tr>
<tr>
<td>w</td>
<td>water content in fuel, kg/kg fuel</td>
</tr>
<tr>
<td>o_w</td>
<td>moisture in air, kg/kg air</td>
</tr>
<tr>
<td>σ</td>
<td>Steffen – Boltzman constant = 5.669 * 10⁻⁸ watt/m²k</td>
</tr>
<tr>
<td>ρ_w</td>
<td>density of water, kg/m³</td>
</tr>
<tr>
<td>ρ_v</td>
<td>density of steam, kg/m³</td>
</tr>
<tr>
<td>ε_w</td>
<td>emissivity of mantle wall surface</td>
</tr>
<tr>
<td>ε_g</td>
<td>emissivity of combustion gases</td>
</tr>
</tbody>
</table>

APPENDIX-I

C_1 = \frac{\partial Q_o}{\partial m_f} = H_f + C_f(T_f - T) ; C_2 = \frac{\partial Q_o}{\partial T_f} = -(m_f) C_f 

C_1 = \frac{\partial Q_o}{\partial m_f} = (1 + AFR) - 9H C_v (T_o + T_f) + (w + 9H) A T_f 

C = \frac{\partial Q_o}{\partial T_o} = m_f / (1 + AFR) - 9H C_v 

C = \frac{\partial Q_o}{\partial T_f} = m_f / (1 + AFR) - 9H C_v 

C_6 = \frac{\partial Q_{go}}{\partial T_g} = 4 fr \sigma (T_g) + 273 .13^3 + h_c A_f.
Parameter Tuning via Genetic Algorithm of Fuzzy Controller for Fire Tube Boiler

\[ C_9 = \frac{\partial Q_{net}}{\partial m'} = s = -4 \text{ fr } \sigma (T_w) + 273 \cdot 13 + h_a A_n \]

\[ C_{10} = \frac{\partial Q_{net}}{\partial m w} = s = -h_a \]

\[ C_{11} = \frac{\partial T_g}{\partial T_w} = \frac{\partial h}{\partial T_w} = m' s \frac{\partial h}{\partial T_w} \]

\[ C_{12} = \frac{\partial T_g}{\partial T_w} = \frac{1 - 4 A \cdot \text{ fr } \sigma (T_w) + 273 \cdot 13 + A \cdot h_c}{2m' s (1 + AFR) \sigma} \]

\[ C_{13} = \frac{\partial T_g}{\partial \rho} = \frac{1}{\rho} \]

\[ C_{14} = C_{15} = \left( \rho_a (u_v - u) \right) \]

\[ C_{16} = (V_s \frac{d \rho_v}{dT_w} + \rho_v \frac{d V_s}{dT_w} \right) \]

\[ C_{17} = (u_v \frac{d \rho_v}{dT_w} + \rho_v \frac{d u_v}{dT_w} + \rho_a \frac{d V_s}{dT_w} - u_v \frac{d \rho_a}{dT_w}) \]

\[ C_{18} = (u_v - h_v) \]

Biographical notes: Ayman A. Aly holds a BSc with excellent honour degree (top student) in 1991, MSc in Sliding Mode Control from Mechanical Engineering Department, Assiut University, Egypt in 1996 and PhD in Adaptive Fuzzy Control from Yamanashi University, Japan in 2003. He was an Assistant Professor at Assiut University from 2003–2008. Currently, he is an Associate Professor and the Head of Mechatronics Engineering Section at Taif University, Saudi Arabia. Ayman A. Aly is the author of more than 55 scientific papers in Refereed Journals and International Conferences. He supervised some of MSc. and PhD Degree Students. His main areas of research are Intelligent Control of Mechatronics systems, Automotive control systems, Thermofluid systems modeling and simulation.