Polyphase Structure Based Eigen Design of Two-Channel Quadrature Mirror Filter Bank

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Abstract—This paper presents a method for the design of two-channel quadrature mirror filter (QMF) banks with linear phase in frequency domain. Low-pass prototype filter of the QMF bank is implemented using polyphase decomposition. Prototype filter coefficients are optimized to minimize an objective function using eigenvalue-eigenvector approach without matrix inversion. The objective function is formulated as a weighted sum of four terms, pass-band error and stop-band residual energy of low-pass analysis filter, the square error of the overall transfer function at the quadrature frequency and amplitude distortion of the filter bank. The simulation results clearly show that the proposed method requires less computational efforts in comparison to the other state-of-art existing design methods.

Index Terms—Nonlinear optimization, Polyphase decomposition, Sub-band coding, Perfect reconstruction.

I. INTRODUCTION

Quadrature mirror filters (QMF) are based on the concept of splitting the bandwidth of the original spectrum in two halves, the low and the high bands. This is done by designing special purpose low-pass and high-pass filters [1]. Two-channel QMF bank finds applications in various signal processing fields, such as multichannel modulation systems [2], design of wavelet bases [3], image coding [4], digital trans-multiplexers [5], discrete multi-tone modulation systems [6], ECG signal compression [7], antenna systems [8], speech compression [9], biomedical signal processing [10] and acoustic echo-cancellation [11].

Various unconstrained and constrained optimization techniques [12–25] have been developed for the design of two-channel QMF banks in both time and frequency domains. Analysis and synthesis sections of a typical QMF bank are shown in Fig. 1. Using the low-pass and high-pass analysis filters $H_1(z)$ and $H_2(z)$, an input signal $x(n)$ is divided into two equally spaced frequency sub-bands. These sub-band signals are decimated by a factor of 2 to accomplish signal compression. At the receiver end, sub-band signals are interpolated and recombined using similar set of synthesis filters to obtain the reconstructed output signal. Due to the fact that filters $H_1(z)$, $H_2(z)$, $G_1(z)$, and $G_2(z)$ are not ideal, the output signal $y(n)$ suffers from three errors: aliasing distortion (ALD), phase distortion (PHD) and amplitude distortion (AMD) [26, 27]. Thus, the design problem for the two-channel QMF bank is to find the optimal filters for the analysis/synthesis sections such that the reconstructed signal $y(n)$ approximates the original signal $x(n)$.

The expression for the overall transfer function of the alias free two-channel QMF bank can be written as [16–23]

$$T(z) = \frac{1}{2} \left[ H_2^2(z) - H_1^2(-z) \right]$$

where synthesis filters are defined in terms of analysis filters as given below for alias cancellation

$$G_1(z) = H_2(-z) \quad \text{and} \quad G_2(z) = -H_1(-z),$$

and mirror image analysis filters $H_1(z)$ and $H_2(z)$ are related to each other by following equation

$$H_2(z) = H_1(-z)$$

Equation (1) indicates that the overall design task reduces to the determination of the optimized filter coefficients of the low pass analysis filter $H_1(z)$ only, which is known as low-pass prototype filter. To obtain the exact reconstruction QMF bank, PHD and AMD should also be eliminated, in this case the overall transfer function $T(z)$ must be a pure delay, i. e.,

$$T(z) = cz^{-n_0}$$

Let the low-pass filter $H_1(z)$ is selected to be a linearphase finite impulse response (FIR) with even filter length $N$, then from (1), $T(z)$ also becomes linear phase FIR and PHD of QMF bank is eliminated completely. The inverse $Z$ transform $h_1(n)$ of $H_1(z)$ is given by

$$h_1(n) = h_1(N - 1 - n)$$

The corresponding frequency response has the form

$$H_1(e^{j\omega}) = e^{-j\omega(N-1)/2}H_R(\omega)$$
where \( H_e(\omega) \) is the amplitude function. For real impulse response \( h_1(n) \), the magnitude response \( |H(\omega)| \) is an even function of \( \omega \), therefore, by substituting (6) into (1) yields the overall frequency response of QMF bank as follows:

\[
T(e^{j\omega}) = \frac{(e^{-j\omega(N-1)})}{2} |H_1(e^{j\omega})|^2 (\omega^{-1}) |H_2(e^{j\omega})|^2 \tag{7}
\]

If filter length \( N \) is selected to be odd, then the above equation gives severe amplitude distortion at quadrature frequency. Therefore, \( N \) must be chosen to be even and the condition for exact reconstruction (ER) can be written [1]

\[
|T(e^{j\omega})| = |H_1(e^{j\omega})|^2 + |H_2(e^{j\omega})|^2 = c, \text{ for all } \omega. \tag{8}
\]

After eliminating ALD and PHD completely, we can only minimize amplitude distortion [26] rather than completely eliminated due to mirror image symmetry constraint of (3). If the characteristics of prototype filter are assumed ideal in pass-band and stop-band regions then \( |T(e^{j\omega})| \) will be constant in the pass bands of \( H_1(z) \) and \( H_2(z) \) and ER condition is automatically satisfied in these regions. The main hurdle comes in transition band region. Thus, the aim is to find the optimal coefficients for the FIR low-pass prototype filter such that the flat exact reconstruction condition must be satisfied given in (8).

This paper proposes an improved technique for the design of QMF bank by representing the low-pass prototype filter using polyphase structure and minimization of a quadratic error function by unconstrained iterative method without any matrix inversion. In section 2, polyphase representation and formulation of design problem are discussed. Section 3 presents the design algorithm. Section 4 describes the simulation results with design examples. Finally, conclusions are drawn in section 5.

II. POLYPHASE REPRESENTATION OF QMF BANK

The polyphase decomposition can be used to implement the analysis and synthesis sections of a filter bank in a very computationally efficient manner [1, 26]. In general, \( M \)-fold decimation filter or interpolation filter can be implemented with approximately \( M \)-fold reduction in the number of multiplications per unit time (MPUs) and number of additions per unit time (APUs) by using the polyphase representation. Polyphase component based complete two-channel QMF bank requires only about \((N-1)/2\) MPUs and \((N-1)/2\) APUs [1], where \( N \) is the filter length of \( H_1(z) \). Type1 polyphase representation [1] of analysis filters is given by

\[
H_1(z) = E_1(z^2) + z^{-1}E_2(z^2) \tag{9}
\]

\[
H_2(z) = E_1(z^2) - z^{-1}E_2(z^2) \tag{10}
\]

Where

\[
E_1(z) = \sum_{n=0}^{M} h_1(2n)z^{-n} \text{ and } E_2(z) = \sum_{n=0}^{M} h_1(2n+1)z^{-n} \tag{11}
\]

Equation (5) states that the impulse response \( h_1(n) \) of the prototype filter \( H_1(z) \) is symmetric, this also reflects into the polyphase components \( E_1(z) \) and \( E_2(z) \). Due to the symmetry of \( h_1(n) \), the impulse response \( e_1(n) = h_1(2n+1) \) is the mirror image of \( e_1(n) = h_1(2n) \) for even \( N \) and if \( N \) is odd, then \( e_1(n) \) & \( e_2(n) \) are symmetric sequences [1]. This further impact on computational complexity, we obtain a factor of two additional saving in multiplication rate. Thus, the polyphase structure of a two-fold decimation filter with symmetric impulse response requires only about \((N-1)/4\) MPUs whether \( N \) is even or odd. The length of filter \( H_1(z) \) is taken as even, therefore, the relationship between two polyphase components can be given as

\[
e_1(n) = e_2((N-2)/2 - n) = e_2(M-n) \tag{12}
\]

where \( M = (N-2)/2 \)

then, \( E_2(z) \) can be expressed as

\[
E_2(z) = z^{-(N-2)/2}E_1(z^{-1}) \tag{13}
\]

By using the above concept, the polyphase structure for two-channel QMF bank with noble identities described in [26] can be modified as depicted in Fig. 2.
By substituting $E_t(z)$ from (13) into (9), we obtain

$$H_s(z) = E_t(z^2) + z^{-1}, z^{-(N-2)}E_t(z^{-2})$$

(14)

The frequency response of prototype filter is given by

$$H_s(e^{j\omega}) = E_t(e^{2j\omega}) + e^ {-j\omega(N-1)}E_t(e^{-2j\omega})$$

(15)

Where

$$E_t(e^{2j\omega}) = \sum_{n=0}^{(N-2)/2} e_t(n)e^{-j\omega n}$$

(16)

Comparing (17) with (6) yields

$$H_R(\omega) = \left[\sum_{n=0}^{(N-2)/2} b_n \cos \omega \left(2n - \frac{(N-1)}{2}\right)\right]$$

(18)

$$= \mathbf{b}^T \mathbf{c}(\omega)$$

(19)

where $b_n = 2c_t(n) \pi$ and

$$\mathbf{b} = [b_0, b_1, b_2, ..., b_M]^T,$$

$$\mathbf{c}(\omega) = [\cos \omega \left(0 - \frac{(N-1)}{2}\right) \cos \omega \left(2 - \frac{(N-1)}{2}\right) ... \cos \omega \left(\frac{(N-1)}{2} - 1\right)]^T$$

(20)

A. The Objective Function

The objective function should reflect the stop-band energy as well as the accuracy of pass-band and transition band. In this paper, the QMF design problem is formulated as a multi-objective unconstrained optimization problem. A novel objective function is formulated as a weighted sum of four terms:

$$E = \alpha_1 E_p + \alpha_2 E_s + \alpha_3 E_t + \alpha_4 E_m$$

(21)

where $\alpha_1, \alpha_2, \alpha_3$ and $\alpha_4$ are real constants, and $E_p$, $E_s$, $E_t$, and $E_m$ are the pass-band error, stop-band residual energy, square error of the $T(z)$ at $\omega = \pi/2$, and amplitude distortion, respectively. For exact reconstruction, the $|T(e^{j\omega})|$ must be equal to $|H_R(e^{j\omega})|$ at $\omega = 0$. Consequently, at $\omega = \pi/2$ the exact reconstruction condition of (8) can be expressed as

$$H_R(\pi/2) = 0.707 H_R(0)$$

(22)

where $H_R(\pi/2)$ and $H_R(0)$ are the amplitude responses of prototype filter at $\omega = 0$ and $\omega = \pi/2$, respectively. Using (19) and (22), the square error $E_t$ in transition band can be implemented as

$$E_t = |H_R(\pi/2) - 0.707 H_R(0)|^2$$

(23)

$$= |\mathbf{b}^T \mathbf{q} - 0.707 \mathbf{b}^T \mathbf{c}(0)|^2 = |\mathbf{b}^T \mathbf{q} - H_{R1}|^2$$

(24)

where vector $\mathbf{q}$ is equal to vector $\mathbf{c}(\omega)$, when it is evaluated at $\omega = \pi/2$, and $H_{R1} = 0.707 \mathbf{b}^T \mathbf{c}(0)$. Similarly, $E_p$ and $E_t$ can be obtained

$$E_p = \int_0^{\pi/2} \left[|H_R(0)| - |H_R(\omega)|\right] d\omega$$

(25)

$$= \mathbf{b}^T \mathbf{F} \mathbf{b}$$

(26)

where $\mathbf{F}$ is symmetric and positive definite matrix, given by

$$\mathbf{F} = \int_0^{\pi/2} |\mathbf{c}(0) - \mathbf{c}(\omega)||\mathbf{c}(0) - \mathbf{c}(\omega)|^T d\omega$$

(27)

$$E_s = \int_{\omega_s}^{\pi} |H_R(\omega)| d\omega$$

(28)

$$= \mathbf{b}^T \mathbf{G} \mathbf{b}$$

(29)

where $\mathbf{G}$ is symmetric and positive definite matrix, calculated as
\[ G = \int_{-\pi}^{\pi} \mathbf{c}(\omega) \mathbf{c}(\omega)^T \, d\omega \]  \hspace{1cm} (30)

\[ E_m \text{ can be realized as} \]
\[ E_m = \max_{\omega} |T(e^{j\omega})|^{\min_{\omega}} |T(e^{j\omega})| \]  \hspace{1cm} (31)

III. OPTIMIZATION ALGORITHM

Substituting (24), (26), (29) and (31) into (21) yields
\[ E = \alpha_1 \mathbf{b}^T \mathbf{F} \mathbf{b} + \alpha_2 \mathbf{b}^T \mathbf{G} \mathbf{b} + \alpha_3 \mathbf{b}^T \mathbf{q} - H \mathbf{b} \mathbf{1}^T \mathbf{b} + \alpha_4 E_m \]
\[ = \mathbf{b}^T \mathbf{R} \mathbf{b} + \alpha_3 [-2H \mathbf{R} \mathbf{b} + H \mathbf{b} \mathbf{1}^T] + \alpha_4 E_m \]  \hspace{1cm} (32)

Where matrix \( \mathbf{R} \) is

\[ \mathbf{R} = \alpha_1 \mathbf{F} + \alpha_2 \mathbf{G} + \alpha_3 \mathbf{S} \]  \hspace{1cm} (33)

and \( \mathbf{S} = \mathbf{q} \mathbf{q}^T \)

\( \mathbf{R} \) is a real, symmetric and positive definite matrix and objective function \( E \) is in quadratic form. So, the minimization problem can be formulated to calculate optimal \( \mathbf{b} \) as an eigenvector corresponding to the minimum eigenvalue \( \lambda_{\min} \) of \( \mathbf{R} \). The standard methods for finding the eigenvalues of a large matrix are not efficient. In this paper a modified Power method without any matrix inversion [1] is used to determine minimum eigenvalue and corresponding eigenvector in the eigenspace for the minimization problem. Power method is an iterative method which starts with an initial arbitrarily chosen vector \( \mathbf{p}_0 \) and generates a sequence of approximations \( \mathbf{p}_k \) to get optimized filter coefficients corresponding to \( \lambda_{\min} \) of \( \mathbf{R} \).

A step-by-step algorithm for designing the prototype low-pass filter based on the principle discussed above is as follows:

1. Select design specifications of \( H_1(z) \) such as filter length \( N \), stop-band edge frequency \( \omega_s \) and pass-band edge frequency \( \omega_p \).
2. To satisfy the unit energy constraint, initial eigenvector of length \( N/2 \) is taken as \( \mathbf{p} = [0, 0, 0, \ldots, 0, 1/2] \).
3. Assume initial values of \( a_1, a_2, a_3 \) and \( a_4 \).
4. Set the iteration number, \( i = 0 \).
5. Obtain initial vector \( \mathbf{b}_i \) by constraining \( \mathbf{p}_i \) to be unit norm vector and compute the matrix \( \mathbf{R} \) using (33).
6. Compute the new eigenvector as \( \mathbf{p}_{i+1} = \mathbf{R} \mathbf{b}_i \).
7. Compute \( \mathbf{b}_{i+1} \) from \( \mathbf{p}_{i+1} \) also compute the objective function \( E_{i+1} \), at the design vector \( \mathbf{b}_{i+1} \). If \( E_{i+1} \geq E_i \), choose the optimum point as \( \mathbf{b}_i \), stop the procedure and go to step (11). If \( E_{i+1} \leq E_i \), set \( \mathbf{E}_{i+1} = \mathbf{E}_i \), \( \mathbf{p}_i = \mathbf{p}_{i+1} \), \( \mathbf{b}_i = \mathbf{b}_{i+1} \), and \( i = i+1 \) and go to step (6) until the following condition reached:
8. \( \mathbf{b}_i = \mathbf{R} \mathbf{b}_i = \lambda_{\max} \mathbf{b}_i \).

(9) Compute maximum eigenvalue (\( \lambda_{\max} \)) of matrix \( \mathbf{R} \) from step (7) and define a new matrix \( \mathbf{A} = \lambda_{\max} \mathbf{I} - \mathbf{R} \), which is positive semi-definite.

(10) Again compute the maximum eigenvalue (\( \lambda_{\max} \)) for matrix \( \mathbf{A} \) using same procedure in step (6) and step (7) for matrix \( \mathbf{A} \).

(11) Minimum eigenvalue (\( \lambda_{\min} \)) for matrix \( \mathbf{R} \) can be calculated by the relation \( \lambda_{\min} = \lambda_{\max} - \lambda_{\min} \) without involving any matrix inversion.

(12) The optimum solution is \( \mathbf{b} = \mathbf{b}_{i+1} \) and finally compute \( h_1(n) \).}

IV. DESIGN EXAMPLES AND DISCUSSION

In this section, we present MATLAB based computer simulations for QMF bank using the above algorithm. A desktop computer equipped with Intel Core 2 Duo CPU @ 2.10 GHz, 1 GB RAM is used to test the programs. The performance and effectiveness of the algorithm is evaluated in terms of peak and overall magnitude reconstruction error (PRE) in dB = \( \min_{\omega} 10 \log_{10} |T(e^{j\omega})| + \min_{\omega} 10 \log_{10} |T(e^{-j\omega})| \). Pass band error (\( E_p \)), Stop band error (\( E_s \)), Computational time (CPU time), number of iterations (\( N_I \)), stop-band edge attenuation (\( A_s \)) = -20 \log_{10} (H(z)) and stop-band first lobe attenuation (\( A_l \)). The constants \( a_1, a_2, a_3 \) and \( a_4 \) are selected by trial and error method to find the best possible solution. Table 1 demonstrate the comparison of the proposed method with other state-of-art existing method for filter length (\( N \)) = 24 in terms of significant quantities with similar design specifications.

A. Design Examples

Example 1: For \( N = 48, \omega_s = 0.6\pi, \omega_p = 0.4\pi, a_1 = 0.95, a_2 = 0.1, a_3 = 0.05 \) and \( a_4 = 10^{-2} \), the following filter tap weights for the FIR low-pass prototype filter (\( H_1(z) \)) yields after 12 iterations:

\[ h_1(0) = -0.000030, h_1(1) = 0.000069, h_1(2) = 0.000157, h_1(3) = -0.000357, h_1(4) = -0.000456, h_1(5) = 0.001185, h_1(6) = 0.000951, h_1(7) = -0.00310199, h_1(8) = -0.00151, h_1(9) = 0.00689464, h_1(10) = 0.001689, h_1(11) = -0.013591, h_1(12) = -0.000551, h_1(13) = 0.024433, h_1(14) = -0.003557, h_1(15) = -0.041045, h_1(16) = 0.013497, h_1(17) = 0.066259, h_1(18) = -0.034971, h_1(19) = -0.107700, h_1(20) = 0.084400, h_1(21) = 0.199042, h_1(22) = -0.261766, h_1(23) = -0.929945. \]

The significant quantities obtained are \( E_p = 2.725 \times 10^{-11}, E_s = 7.224 \times 10^{-12}, A_s = 67.7 \text{ dB}, A_l = 97.65 \text{ dB}, \text{CPU-time} = 0.0686 \text{ sec.}, \text{PRE} = 0.0068 \text{ dB}. \) For example 1, the resulting magnitude response of low-pass prototype filter is shown in Fig. 3a. The normalized magnitude plots of analysis filters \( H_1(z) \) and \( H_2(z) \) are displayed in Fig. 3b. Figures 3c and 3d depict the reconstruction error (in dB) and overall magnitude response of the QMF bank, respectively.

Example 2: For \( N = 24, \omega_s = 0.6\pi, \omega_p = 0.4\pi, a_1 = 0.61, a_2 = 0.9, a_3 = 0.06 \) and \( a_4 = 10^{-2} \), the following filter tap
weights for the FIR low-pass prototype filter \( H_1 (z) \) yields after 06 iterations:

\[
\begin{align*}
h_1(0) &= -0.002162, \quad h_1(1) = 0.006417, \quad h_1(2) = 0.003313, \\
h_1(3) &= -0.020964, \quad h_1(4) = -0.000133, \quad h_1(5) = 0.048519, \\
h_1(6) &= -0.015659, \quad h_1(7) = -0.097246, \quad h_1(8) = 0.062790, \\
h_1(9) &= 0.198991, \quad h_1(10) = -0.243114, \quad h_1(11) = -0.940639.
\end{align*}
\]

The significant quantities obtained are \( E_p = 1.9471 \times 10^{-5} \), \( E_s = 9.6599 \times 10^{-7} \), \( A_s = 34.18 \text{ dB} \), \( A_l = 49.96 \text{ dB} \), CPU-time = 0.0288 sec., and PRE = 0.0266 dB. For example 2, the resulting magnitude response of low-pass prototype filter is shown in Fig. 4a. The normalized magnitude plots of analysis filters \( H_1 (z) \) and \( H_2 (z) \) are displayed in Fig. 4b. Figures 4c and 4d depict the reconstruction error (in dB) and overall magnitude response of the QMF bank, respectively.

It can be clearly observed from Table 1 that the performance of the proposed design technique is better than all other methods in terms of \( E_s, A_s, A_l, \) number of iteration (NOI) required and the CPU time of the processor. The performance in terms of reconstruction error is also comparable with other existing methods. Consequently, the main advantage of proposed technique is reduction in computational burden and it is suitable for various engineering fields such as image and speech compression.

**Fig. 3** (a) Magnitude response of low-pass analysis filter for \( N = 48 \)  (b) Normalized Magnitude responses of analysis filters \( H_1 (z) \) and \( H_2 (z) \)  (c) Reconstruction error in dB  (d) Overall magnitude response of the QMF bank
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V. CONCLUSION

A computational efficient method for designing of two-channel QMF bank has been presented in this paper. The prototype filter for the filter bank was designed using polyphase concept to reduce the CPU time. The objective function for the design problem also includes the amplitude distortion term for better results. The improved eigenvalue-eigenvector approach was used for optimization that does not require any matrix inversion which generally affects the effectiveness. The computational burden is very little for the proposed technique in comparison of other state-of-art existing techniques. The proposed method is also very effective for higher filter orders. The extension of this approach for designing more than two-band QMF bank is under investigation. This type of design methods may be suitable various engineering fields such as image and speech compression.

Table 1: Performance comparisons of proposed method with state-of-art existing methods for N = 24

<table>
<thead>
<tr>
<th>Methods</th>
<th>$E_s$</th>
<th>$E_p$</th>
<th>PRE (dB)</th>
<th>$A_a$ (dB)</th>
<th>$A_e$ (dB)</th>
<th>NOI</th>
<th>CPU time(s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ghosh et al. [23]</td>
<td>$1.30 \times 10^{-4}$</td>
<td>$9.14 \times 10^{-7}$</td>
<td>0.030</td>
<td>20.11</td>
<td>30.93</td>
<td>-----</td>
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<td>(MJADE_pBX algorithm)</td>
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<tr>
<td>Upendar et al. [19]</td>
<td>$7.99 \times 10^{-5}$</td>
<td>$1.84 \times 10^{-7}$</td>
<td>0.019</td>
<td>22.78</td>
<td>34.43</td>
<td>122</td>
<td>1.48</td>
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<tr>
<td>PSO [20]</td>
<td>$4.69 \times 10^{-5}$</td>
<td>$1.28 \times 10^{-7}$</td>
<td>0.017</td>
<td>28.86</td>
<td>38.8</td>
<td>128</td>
<td>1.69</td>
</tr>
<tr>
<td>Yue -Dar J. [24]</td>
<td>--</td>
<td>--</td>
<td>0.043</td>
<td>22.05</td>
<td>--</td>
<td>09</td>
<td>--</td>
</tr>
<tr>
<td>Steepest-Descent [21]</td>
<td>$7.06 \times 10^{-5}$</td>
<td>$1.32 \times 10^{-7}$</td>
<td>0.031</td>
<td>25</td>
<td>34.7</td>
<td>76</td>
<td>0.81</td>
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<td>A. Kumar et al. [18]</td>
<td>$1.74 \times 10^{-5}$</td>
<td>$7.86 \times 10^{-8}$</td>
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<td>28.31</td>
<td>37</td>
<td>21</td>
<td>0.11</td>
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<tr>
<td>Sahu [17]</td>
<td>$8.45 \times 10^{-5}$</td>
<td>$9.23 \times 10^{-8}$</td>
<td>0.025</td>
<td>23.03</td>
<td>35.83</td>
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<tr>
<td>Proposed Method</td>
<td>$9.65 \times 10^{-7}$</td>
<td>$1.95 \times 10^{-7}$</td>
<td><strong>0.0266</strong></td>
<td><strong>33.18</strong></td>
<td><strong>48.91</strong></td>
<td><strong>06</strong></td>
<td><strong>0.028</strong></td>
</tr>
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Fig. 4 (a) Magnitude response of low-pass analysis filter for N = 24 (b) Normalized Magnitude responses of analysis filters H1(z) and H2(z) (c) Reconstruction error in dB (d) Overall magnitude response of the QMF bank
REFERENCES


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