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# Performance Analysis and Enhancement of TCP in Presence of Jitter in Wireless Networks

#### Goudru N.G

Department of Mathematics, BMS Institute of Technology (affiliated to Visvesvaraya Technological University),
Bangalore, India. Mobile: 90-9341384414,
E-mail: nggoudru@gmail.com

# Vijaya Kumar B.P

Department of Information Science and Engineering, MS Ramaiah Institute of Technology (affiliated to Visvesvaraya Technological University), Bangalore, India. Mobile: 90-9980634134, E-mail: vijaykbp@yahoo.co.in

Abstract—In wireless networks two types of losses namely congestion loss and transmission loss are significant. One of the important transmission losses is jitter. Variation in inter-arrival time is called jitter. When jitter value is greater than half of the average round trip time cause timeout loss and sender window size falls to one packet resulting reduction in throughput and degradation in the quality of service (QoS). In this paper, we are discussing a new model for transmission control protocol (TCP) which is capable of changing its window size based on the feedback. In the new model TCP is added with intelligence so that it can distinguish the type of losses. If the loss is due to congestion, congestion control algorithm is invoked and loss is due to jitter immediate-recovery algorithm is invoked to recover from the throughput loss. The technique also provides an endto-end congestion control. The performance of TCP is further enhanced by discussing stability. Time-delay control theory is applied for the analysis of asymptotic stability. The stability boundaries of random early detection (RED) control parameter P<sub>max</sub> and jitter control parameter  $\beta$  are derived. Using the characteristic equation of Hermite matrix an approximate solution of q(t) (queue length) which converges to a given target value is derived. The results are analyzed based on graphs and statistical data using Matlab R2009b.

*Index Terms*—Congestion, convergence, immediate-recovery, jitter, stability, TCP, wireless networks.

## I. INTRODUCTION

Because of popularity in Internet services, current network traffic is dominated by the data generated by the applications such as web, email, multimedia downloads, file transfer, etc. [1]. One of the important affecting factors for providing QoS in wireless networks is packet losses. In wireless network, packet losses are due to congestion as well transmission. The congestion loss is due to burst traffic in the network and transmission loss is due to high bit error rate or jitter or frequent

disconnections. Transmission loss occurs very frequently in wireless links which cannot be ignored. Packet loss due to transmission in wired links can be ignored [2], [3]. In addition to this, challenges for applying TCP over wireless link is an end-to-end congestion control. An end-to-end congestion control results in seamless data transportation. For a packet sent by the source, acknowledgement (ACK) is received before the timeout period. Otherwise this leads to a timeout loss and sender window (cwnd) size set to 1 packet. In this paper, we consider jitter which causes wireless transmission loss. Jitter is the variation in inter arrival time. Positive jitter value which is greater than half of the average round-trip value results in timeout loss. Any packet arriving after its scheduled time is discarded by the receiver. The problem of delay-jitter is thereby transformed into end-to-end delay and packet losses. Moreover, for a timeout loss, the sender TCP does an exponential backoff for some time. The effect of the backoff is that the window size does not grow for a small period, after which it starts growing at a normal rate. For timeout loss source reduces its sending rate which is unnecessary [4], [5], [6], [7], [20], [21]. Researcher tried to provide some solutions to these problems. Some of the proposed solutions by the researchers are Indirect TCP (I-TCP) Protocol [8], SNOOP protocol [9], Wireless-TCP [10], TCP Westwood [11], ACK pacing [12], ACK splitting [13] and so on. To recognise the loss is due to congestion or transmission, the researchers has proposed some schemes. Some techniques proposed to judge the loss events and improve TCPs throughput are [14], [15]. The problem with these proposed techniques is too difficult in implementation. To satisfy these problems for applying TCP over wireless link, we propose a scheme that can dynamically change the sending rate to the packet loss caused due to congestion or jitter. The model works on the principle of additive increase and multiplicative decrease (AIMD) to satisfy the properties of congestion control algorithm and also has the capability of distinguish the packet loss caused due to congestion or jitter. If the loss is due to congestion, congestion control algorithm is invoked and the loss is due to jitter,

immediate-recovery algorithm is invoked. This makes sender window to recover from unnecessary reduction made at the source. To enhance the performance of TCP for further, we apply the stability analysis [16], [17], [18]. Conditions are obtained for asymptotic stability of wireless system using time-delay control theory. Using Hermit matrix method, a relationship between  $P_{\text{max}}$  (RED controlling parameter) and  $\beta$  (jitter controlling parameter) is established. A stability boundary for  $P_{\text{max}}$  and  $\beta$  is established in terms of wireless network resource parameters. Queue convergence analysis is made. An approximate solution for q(t) is derived. Models validation is made using Matlab. Result analysis is made using graphs and the statistical data.

#### II. RATE BASED JITTER ESTIMATION

The packet delay variation is called jitter. Jitter also can be an indicator of network health. Increasing jitter is an indication of increase in congestion and decreasing jitter is an indication of smoother transmission. This nature of jitter helps to distinguish the congestion loss and the transmission loss [19].

Let  $B_{bi}$  be the bottleneck bandwidth, S be the packet size,  $t_0^s$  and  $t_1^s$  be the time when the first and second packets are send one after the other from a source. Let  $t_0^d$  and  $t_1^d$  be the time when first and second packets are received at the destination. Without loss of generality, we can write  $B_{bn}$ = $S/(t_1^d - t_0^d)$ .

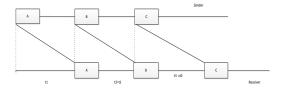


Fig.1. Time Diagram Showing Jitter

Let the receiver receives  $i^{th}$  packet at time  $t_i^d$ . But,  $t_i^d = t_i^s + tt_i$ , where  $t_i^s$  is the time that  $i^{th}$  packet was sent, and  $tt_i$  is the transmission time. The transmission time  $tt_i = pt_i$  (propagation delay)  $+ q_i$  (queuing delay at the router). In a single hop network where propagation time is same,  $pt_i$  is almost same (constant). The queuing time,  $q_i$  depends on (i) waiting time in the queue, and (ii) processing time which is very negligible. Under these assumptions, the difference between inter-reception time and inter sending time called Jitter. The inter-receipt time between two consecutive packets i-1 and i is denoted by irt<sub>i</sub>.

$$\begin{split} & irt_i = t_i^{\;d} - t_{i\text{-}1}^{\;\;d} \; = (t_i^{\;s} + tt_i) - (t_{i\text{-}1}^{\;s} + tt_{i\text{-}1}) = (\;t_i^{\;s} - t_{i\text{-}1}^{\;s}) + (tt_i \\ - tt_{i\text{-}1}) \\ & irt_i = (\;t_i^{\;s} - t_{i\text{-}1}^{\;s}) + ((pt_i + q_i) - (pt_{i\text{-}1} + q_{i\text{-}1})) \\ & irt_i = (\;t_i^{\;s} - t_{i\text{-}1}^{\;s}) + (pt_i - pt_{i\text{-}1}) + (q_i - q_{i\text{-}1}) \end{split}$$

In single hop network propagation time is constant. This implies that  $pt_i$  is constant. Thus  $(pt_i - pt_{i-1}) \rightarrow 0$ . Also, the sending timings of the packets,  $t_i^s$  and  $t_{i-1}^s$  are known entities. Hence, the only variant is

the queuing time. Therefore, jitter is the varying queuing

time measured at the destination. Jitter $_i = q_i - q_{i-1}$ . The occurrence of jitter can be noticed by measuring the variation in queuing-delays at the destination. Jitter can be positive, negative, or zero. This leads to the following conclusions. (i) When variation in queuing-delay is positive then i<sup>th</sup> packet gets more delayed than the (i-1) <sup>th</sup> packet, (ii) Variation is negative then the i<sup>th</sup> packet reach destination in less time than (i-1) th packet, and (iii) variation zero indicates that the network congestion remains unchanged over the time scale of consecutive packets. We are interested in (i). The later packet reaches the destination taking more time than the previous packet, causing positive delay-variation in the inter arrival time. This is due to transmission error and in wireless networks this occurs in more frequent. The positive delay-variation in the inter arrival time results jittering and triggers into timeout loss.

## A. K/W Transmission loss-predictor

Let L<sub>t</sub>(t) be the wireless transmission loss occurrence after the first packet transferred and ACK has received by the source. Source TCP check whether the jitter-loss is greater than the value of k/w or not, where k is a control parameter and w is the current window size. The ratio k/w indicates that k packets are in the queue at the router when TCP injects w packets into the network. Since TCP adds one packet per RTT,  $0 < k \le 1$ . Using the scheme proposed in [2], K/W loss-predictor, distinguish the packet losses as follows. (i) The next packet loss is due to congestion when, (a) the source receives triple-duplicate acknowledgement, (b) the arrival of ACK is longer than one RTT (Next-RTT), and Jitter value is greater than k/w value. (ii) the next packet loss is due to transmission when, the arrival of ACK is longer than one RTT (Next-RTT), and Jitter value is less than or equal to k/w.

## B. Pseudo-code for loss identification

$$\label{eq:congestion} \begin{split} &jitter_i = q_i - q_{i\text{-}1} \\ &if \; (next\text{-rtt} > 0 \; and \; jitter_i > k/w), \setminus congestion \; loss \\ &\beta = 0, \setminus Invoke \; congestion \; control \; algorithm \\ &end \end{split}$$

 $\begin{array}{ll} \text{if ( next-rtt >0 and jitter}_i \leq k/w) \setminus Transmission \ loss \\ \beta > 0, \ \ \text{timeout-loss, invoke immediate-recovery} \\ \text{algorithm} \\ \text{end} \end{array}$ 

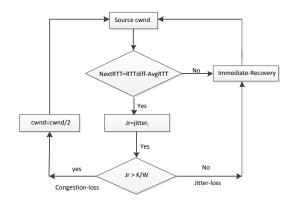


Fig.2. TCP Loss Prediction and Recovery Flow Diagram

When loss is due to congestion, the jitter control parameter,  $\beta$  =0. The threshold value of sender window is fixed to half of the current window size, and slow start phase started. When the loss is due to transmission because of jitter, the sender TCP has experienced it as timeout-loss and decreases the window size to 1 which is unnecessary. To recover from this loss the system invoke immediate-recovery module. The recovery rate is proportional to  $\beta$  times the flow rate of the previous rtt.

# III. SYSTEM MODEL FOR WIRELESS NETWORKS

The extended fluid model [19, 20, 21] that describe the dynamics of the TCP congestion window size in wireless networks in presence of jitter is,

$$dW(t) = \frac{dt}{RTT} - \alpha W(t) L_a(t) + \beta L_t(t)$$
 (1)

TCP operates on AIMD congestion control strategy. The factor  $\alpha$  is decrease rate of source window which is considered as 0.5,  $L_a$  (t) is the arrival rate of packet losses due to congestion at time t and  $L_a(t) = \frac{w(t-R(t))}{R(t-R(t))} \; p(t-R(t-R(t)))$ . This loss is proportional to the throughput at the source. First term on the right hand side of equation (1) refers to linear increase of the sender window size until congestion occurs at the destination. The second term refers to congestion control based on the feedback received from the RED router. The third term  $L_t(t)$  refers to immediate-recovery due to jitter loss. The jitter loss is proportional to the sending rate of the source. Therefore,  $L_t$  (t) is proportional to  $\frac{w(t-R(t))}{R(t-R(t))}$ .

The equation (1) can be modified to

$$\frac{\partial w}{\partial t} = \frac{1}{R(t)} - \frac{w(t)w(t - R(t))}{2R(t - R(t))} p(t - R(t)) + \beta \frac{w(t - R(t))}{R(t - R(t))} \quad (2)$$

 $\beta$  is jitter loss control parameter and by choice  $\beta \in [0,1]$ . The dynamic behaviour of instantaneous queue length is given by

$$\frac{\partial q(t)}{\partial t} = \frac{N w(t)}{R(t)} - C_d$$
 (3)

Where, w(t)/R(t) is increase in queue length due to sending rate of the packets by N- TCP flows.  $C_{\text{d}} = q(t)/R(t)$  is the decrease in queue length due to servicing of packets and delay due to packet departure from the router. The mathematical version which represents packet dropping probability of RED is given by

$$P(t) = \begin{cases} 0 \ , & q(t) \in [0, t_{min}] \\ \frac{q(t) - t_{min}}{W_{max} - t_{min}} \ P_{max} \ , q(t) \in [t_{min}, W_{max}] & (4) \\ 1 \ , & q(t) \ge W_{max} \end{cases}$$

Congestion loss is assumed to happen when queue buffer of the router reaches a value of  $W_{\text{max}}$  packets. The

maximum buffer size,  $W_{max}$  of the router is calculated by,  $W_{max} = \frac{C_d}{s} \, R(t) + M$ , Where  $C_d/S$  is the bandwidth-delay product, M (in packets) is the maximum buffer size of the router and R(t) is the round trip time. The buffer overflow takes place when the queue length becomes larger than  $W_{max}$  value.  $C_d$  is the down-link bandwidth. The model describing round trip time (RTT) in wireless networks is given by,  $R(t) = \frac{q(t)}{C_d} + T_p$ ,  $T_p$  is the propagation delay in the wireless media,  $q(t)/C_d$  models the queuing delay.

#### IV. TIME-DELAY FEEDBACK CONTROL SYSTEM

In this section, we study the stability analysis of TCP in presence of jitter in wireless network system. The procedure applied is as follows: First linearize the system models, using Hermite matrix for time-delay control system, explicit condition under which the system is asymptotically stability is derived. A relationship for  $P_{max}$  and  $\beta$  is obtained. Mathematical relations are derived for stability boundary of RED control parameter  $P_{max}$  and jitter control parameter  $\beta$  in terms of network resource parameters. Convergence analysis of queue length in presence of jitter is discussed.

#### A. Linear Model Derivation

Let x(t) be a general non-linear function defined by, x(t) = f(u(t), v(t), t), where, u(t) represents the sender window dynamics, and v(t) represent the queue dynamics at the bottleneck link. We assuming that f(u(t), v(t), t) has smooth and continuous derivatives around the equilibrium point,  $Q_0 = (w_0, R_0, q_0, p_0)$ . Using Taylor's series expansion, the linear function of non-linear function, ignoring second and higher order partial derivatives is,

$$\begin{aligned} f(u(t), v(t), t) &= f(u_0(t), v_0(t), t_0) + f_u(t) \delta_u(t) \\ &+ f_v(t) \, \delta_v(t) + O(\delta_u(t), \delta_v(t)) \end{aligned}$$

where  $\mathrm{f}_{u}(t)=\frac{\partial \mathrm{f}}{\partial \mathrm{u}}|(u_{0},v_{0})$  ,  $\mathrm{f}_{v}(t)=\frac{\partial \mathrm{f}}{\partial \mathrm{v}}|(u_{0},v_{0})$  . The linear models of the equations (2) to (4) are derived around the equilibrium point  $\mathit{Q}_{0}=(w_{0},\mathsf{R}_{0},q_{0},p_{0}).$  Let N be the number of TCP flows. At  $\mathsf{Q}_{0}$ , the steady state conditions of equations (2) and (3) are given by,  $\dot{w}(t)=0,\ \dot{q}(t)=0.$ 

The estimation algorithm is based on small signal behaviour dynamics, therefore, at the equilibrium point, without loss of generality, we can assume,

$$w(t) = w(t - R(t)) = w_0,$$

$$q(t) = q(t - R(t)) = q_0,$$

$$p(t) = p(t - R(t)) = p_0,$$

$$R(t) = R(t - R(t)) = R_0$$
(5)

Using equations (5) in  $\dot{w}(t) = 0$ ,  $\dot{q}(t) = 0$ , and after simplification we get,

$$p_0 = \frac{2\beta w_0 + 2}{{w_0}^2}$$
 ,  $w_0 = \frac{R_0 C_d}{N}$  ,  $N = \frac{R_0 C_d}{w_0}$ 

Let,  $w_R = w(t - R(t))$ ,  $p_R = p(t - R(t))$ . From (2) we get,

$$u(w, w_{R}, q, p_{R}) = \frac{1}{R(t)} - \frac{w(t) w_{R}(t)}{2 R(t)} p(t - R(t)) + \beta \frac{w_{R}(t)}{R(t)}$$
(6)

To linearize equation (6), find all the partial derivatives of  $u(w, w_R, q, p_R)$  with respect to the variables at the equilibrium point and defining,

$$\delta w(t) = w(t) - w_0, \delta q(t) = q(t) - q_0, \delta p(t) = p(t) - p_0$$

$$\delta \dot{w}(t) = \dot{w}(t) - w_0, \ \delta \dot{q}(t) = \dot{q}(t) - q_0$$

$$\delta p(t) = \frac{L}{B} \left( q(t) - t_{min} \right) - p_{0,} \text{ where } B = W_{max} - t_{min},$$
  $L = p_{max}$ 

$$\delta \dot{w}(t) = -\left(\frac{\beta}{R_0} + \frac{2N}{{R_0}^2 C_d}\right) \delta w - \frac{{C_d}^2 R_0}{2N^2} \delta p_R$$
 (7)

$$\delta \dot{q}(t) = \frac{N}{R_0} \delta w(t) - \frac{1}{R_0} \delta q(t) \tag{8}$$

$$\delta p(t - R_0) = \frac{L}{B} (\delta q(t - R_0)) + \frac{L}{B} (q_0 - t_{min}) - p_0$$
(9)

Using equation (9) in (7), we get

$$\delta \dot{w}(t) = -\left(\frac{R_0}{w_0} + \frac{2N}{R_0^2 c_d}\right) \delta w(t) - \frac{LC_d^2 R_0}{2N^2 B} \delta q(t - R_0) + \frac{LC_d^2 R_0}{2N^2 B} (t_{min} - q_0) + \frac{R_0 C_d^2 p_0}{2N^2}$$
(10)

Denote, 
$$x(t) = \begin{bmatrix} \delta w(t) \\ \delta q(t) \end{bmatrix}$$
, then

$$\dot{\mathbf{x}}(t) = \mathbf{A}\mathbf{x}(t) + \mathbf{E}\mathbf{x}(t - \mathbf{R}(t)) + \mathbf{F} \tag{11}$$

Where,

$$\begin{split} A = \begin{bmatrix} -(\frac{\beta}{R_0} + \frac{2N}{{R_0}^2 C_d}) & 0\\ \frac{N}{R_0} & \frac{-1}{R_0} \end{bmatrix} E = \begin{bmatrix} 0 & \frac{-LR_0{C_d}^2}{2N^2B} \\ 0 & 0 \end{bmatrix}, \\ F = \begin{bmatrix} \frac{-LR_0{C_d}^2}{2N^2B} (t_{min} - q_0) + \frac{R_0{C_d}^2p_0}{2N^2} \\ 0 & 0 \end{bmatrix} \end{split}$$

Solving linear differential equation (11) using Laplace transform technique with

$$L{x(t)} = x(s)$$
, we get

$$(sI - A - Ee^{-R_0 s}) x(s) = \frac{F}{s}$$
 (12)

The characteristic equation of (12) is,

$$|sI - A - Ee^{-R_0 s}| = 0$$
 (13)

After simplification,  $s^2 + \left(\frac{\beta}{R_0} + \frac{2N}{{R_0}^2 C_d} + \frac{1}{R_0}\right)s +$ 

$$\left(\frac{\beta}{R_0^2} + \frac{2N}{R_0^3 C_d} + \frac{LC_d^2}{2NB} e^{-R_0 s}\right) = 0$$
 (14)

The characteristic equation (14) determines the stability of the closed-loop time-delay wireless system in terms of the state variables  $\delta w(t)$  and  $\delta q(t)$ .

## B. Stability Analysis

Denote,  $P(s, e^{-R_0 s}) = s^2 +$ 

$$\begin{split} \left(\frac{\beta}{R_0} + \frac{2N}{R_0^2 C_d} + \frac{1}{R_0}\right) s + \left(\frac{\beta}{R_0^2} + \frac{2N}{R_0^3 C_d} + \frac{LC_d^2}{2NB} e^{-R_0 s}\right) \\ \text{Let } e^{-R0s} &= z, \text{ and } a_0 = 1, a_1 = \frac{\beta}{R_0} + \frac{2N}{R_0^2 C_d} + \frac{1}{R_0}, \\ a_2 &= \frac{\beta}{R_0^2} + \frac{2N}{R_0^3 C_d} + \frac{LC_d^2}{2NB} e^{-R_0 s} \\ P(s, z) &= a_0 s^2 + a_1 s + a_2 \end{split}$$

The Hermit matrix for time-delay control system of equation (15) is

$$H = \begin{bmatrix} (0,1) & (0,2) \\ (0,2) & (1,2) \end{bmatrix}$$

$$(0,1) = 2a_0a_1 = \frac{2(\beta+1)}{R_0} + \frac{4N}{R_0^2C_d}$$

$$(0,2) = -2a_2 \operatorname{Im}(z) = \frac{-Lc_d^2}{NB} \operatorname{Im}(z)$$

$$(1,2) = 2a_1\operatorname{Re}(a_2) =$$

$$2(\frac{\beta}{R_0} + \frac{2N}{R_0^2C_d} + \frac{1}{R_0})(\frac{\beta}{R_0^2} + \frac{2N}{R_0^3C_d} + \frac{Lc_d^2}{2NB})$$

$$\operatorname{Put}, x_1 = \frac{\beta}{R_0} + \frac{2N}{R_0^2C_d} + \frac{1}{R_0}, \ x_2 = \frac{LC_d^2}{NB},$$

$$x_3 = \frac{\beta}{R_0^2} + \frac{2N}{R_0^3C_d}$$

Let  $z = e^{i\omega}$ ,  $z = \cos\omega + i\sin\omega$ ,  $Re(z) = \cos\omega$ ,  $Im(z) = \sin\omega$ , then

$$\label{eq:Heisenberg} \begin{split} \text{H}(e^{\mathrm{i}\omega}) = \begin{bmatrix} 2\mathrm{x}_1 & -\mathrm{x}_2\sin\omega \\ -\mathrm{x}_2\sin\omega & 2\mathrm{x}_1(\mathrm{x}_3 + \frac{\mathrm{x}_2}{2}\cos\omega) \end{bmatrix} \end{split}$$

## C. Stability Conditions

The time-delayed control system (2) to (4) is asymptotically stable in terms of stable variables  $\delta w(t)$  and  $\delta q(t)$ , *iff* the following two conditions are satisfied.

Condition1: The Hermit matrix  $H(1) = H(e^{i0})$  is positive.

$$H(1) = \begin{bmatrix} 2x_1 & 0 \\ 0 & 2x_1(x_3 + \frac{x_2}{2}) \end{bmatrix}$$

From the determinant,  $4x_1^2\left(x_3 + \frac{x_2}{2}\right) > 0$ , after simplification,

$$L = p_{\text{max}} > -(\frac{2\beta NB}{R_0^2 C_d^2} + \frac{4N^2B}{R_0^3 C_d^3})$$
$$\beta > -(\frac{p_{\text{max}} C_d^2 R_0^2}{2NB} + \frac{2N}{R_0 C_d})$$

Condition 2: For all  $\omega \in [0,2\pi]$ , det  $H(e^{i\omega}) > 0$ , leads to the following inequality.

$$(2x_1)\left(2x_1\left(x_3 + \frac{x_2}{2}\right)\right)\cos\omega - x_2^2\sin^2\omega > 0$$
 
$$H(e^{i\omega}) = x_2^2\cos^2\omega + 2x_1^2x_2\cos\omega + 4x_1^2x_3 - x_2^2 > 0 \tag{16}$$

The necessary condition for (16) to be true is the discriminate,  $\Delta > 0$ 

$$cos\omega = \frac{-x_1^2 \pm \sqrt{x_1^2 (x_1^2 - 4x_3) + x_2^2}}{x_2}$$

properties of cosine By the function, for  $\omega \in [0,2\pi]$ ,  $\cos \omega \in [-1,1]$ 

The conditions can be written as,

$$\frac{-x_1^2 - \sqrt{x_1^2(x_1^2 - 4x_3) + x_2^2}}{x_2} > 1 \tag{17}$$

$$\frac{-x_1^2 + \sqrt{x_1^2(x_1^2 - 4x_3) + x_2^2}}{x_2} < -1 \tag{18}$$

By direct manipulation, there is no solution for the inequality (17). From (18), we obtain

$$0 < p_{max} < \left(\frac{2\beta NB}{R_0^2 C_d^2} + \frac{4N^2 B}{R_0^3 C_d^3}\right)$$
 (19)

$$0 < \beta < \left(\frac{p_{\text{max}} C_d^2 R_0^2}{2NB} + \frac{2N}{R_0 C_d}\right)$$
 (20)

# Theorem 1

Given the wireless network parameters C<sub>d</sub> (down link capacity), Cu (up-link capacity), N (number of TCP sessions), R<sub>0</sub> round-trip time, and B RED control parameter, the wireless network system given by (2) to (4) is asymptotically stable in terms of the state variables  $\delta w(t)$  and  $\delta q(t)$  if and only if the control parameters  $P_{max}$ and B satisfies

$$0 < p_{max} < \left(\frac{2\beta NB}{R_0^2 C_d^2} + \frac{4N^2B}{R_0^3 C_d^3}\right)$$

$$0 < \beta < \left(\frac{p_{\text{max}} C_d^2 R_0^2}{2NB} + \frac{2N}{R_0 C_d}\right)$$

# V. CONVERGENCE ANALYSIS OF DYNAMIC QUEUE

In this section, we discuss the convergence of buffer queue in the router. From equation (12),

$$(s I - A - E e^{-R0s})^{-1} = \frac{1}{P(s,e^{-R_0s})} \begin{bmatrix} y_1 & y_2 \\ y_3 & y_4 \end{bmatrix}$$

Where, 
$$y_1 = s + \frac{1}{R_0}$$
,  $y_2 = -\frac{LR_0C_d^2}{2N^2B}e^{-R_0s}$ ,  $y_3 = \frac{N}{R_0}$ ,  $y_4 = s + \frac{\beta}{R_0} + \frac{2N}{R_0^2C_d}$  Equation (13) can be written as

$$x(s) = \frac{F}{s p(s, e^{-R0s})} \begin{bmatrix} y_1 & y_2 \\ y_3 & y_4 \end{bmatrix}$$

After simplification,  $x(s) = \frac{y_5}{s p(e^{-R_0 s})} \begin{bmatrix} y_1 \\ y_2 \end{bmatrix}$ ,

or 
$$\begin{bmatrix} \delta W(s) \\ \delta Q(s) \end{bmatrix} = y_5 \begin{bmatrix} y_1 \\ y_3 \end{bmatrix}$$
 (21)

Where,

$$y_5 = \frac{LR_0C_d^2 \frac{(t_{\min} - q_0)}{2N^2B} + \frac{R_0C_d^2p_0}{2N^2}}{s p(s, e^{-R_0s})}$$

From equation (21),

$$\delta Q(s) = \frac{\frac{N}{R_0} (\frac{LR_0C_d^2}{2N^2B} (t_{min} - q_0) + \frac{R_0C_d^2p_0}{2N^2})}{sP(se^{-R_0s})}$$

$$\delta Q(s) = \frac{\left(\frac{{C_d}^2}{2N}\right)(\frac{L}{B}(t_{min} - q_0) + p_0)}{sp(s, e^{-R}_0 s)}$$

$$\delta Q(s) = \frac{\frac{1C_d^2}{s \cdot 2N} (\frac{L}{B} (t_{\min} - q_0) + p_0)}{S^2 + (\frac{\beta}{R_0} + \frac{2N}{R_0^2} C_d + \frac{1}{R_0}) s + (\frac{\beta}{R_0^2} + \frac{2N}{R_0^3 C_d}) + (\frac{LC_d^2}{2NB}) e^{-R_0 s}}$$
(22)

$$\delta Q(s) = \frac{y_6}{s^2 + x_1} \frac{y_6}{s + x_2} \frac{y_6}{s^2 - R_0 s}$$
 (23)

Where.

$$y_6 = \frac{1}{s} \frac{C_d^2}{2N} \left( \frac{L}{B} (t_{min} - q_0) + p_0 \right)$$

## A. Theorem 2

Given the wireless network parameters C<sub>d</sub>, C<sub>u</sub>, N, R<sub>0</sub> and B, on the basis of wireless network system given in (2) to (4), an approximate solution of q(t) is

$$q(t) = q_0 + y_6 [\frac{\mathrm{e}^{xt}}{(x-y)x} - \frac{\mathrm{e}^{yt}}{(x-y)y} + \frac{1}{xy}]$$

If the RED control parameter  $P_{max}$  and jitter control parameter  $\beta$  satisfies

$$0 < p_{\text{max}} \le \frac{-\xi_2 + \sqrt{\xi_2^2 - 4\xi_1\xi_3}}{2\xi_1}$$
$$0 < \beta \le \frac{-A_2 + \sqrt{A_2^2 - 4A_1A_3}}{2A_1}$$

Where  $\xi_i$ 's and  $A_i$  's are given in (28).

Proof: Expanding e<sup>-R</sup><sub>0</sub>, using Taylor's theorem about the stability point discarding the terms of order three and higher,

$$e^{-R_0 s} = 1 - R_0 s + \frac{{R_0}^2 s^2}{2}$$

From (23),  $s^2 + x_1 s + x_3 + \frac{x_2}{2} e^{-R_0 s}$ . This simplifies to

$$\begin{split} s^2 + \left(\frac{\beta}{R_0} + \frac{2N}{{R_0}^2 C_d} + \frac{1}{R_0}\right) s + \\ \left(\frac{\beta}{{R_0}^2} + \frac{2N}{{R_0}^3 C_d} + \frac{L{C_d}^2}{2NB} (1 - R_0 + \frac{{R_0}^2 s^2}{2})\right) \\ \left(1 + \frac{L{R_0}^2 {C_d}^2}{4NB}\right) s^2 + \left(\frac{\beta}{R_0} + \frac{2N}{{R_0}^2 C_d} + \frac{1}{R_0} - \frac{L{R_0}{C_d}^2}{2NB}\right) s \\ + \left(\frac{\beta}{{R_0}^2} + \frac{2N}{{R_0}^3 C_d} + \frac{L{C_d}^2}{2NB}\right) \end{split}$$

Put

$$\begin{split} \eta_1 &= \left(1 + \frac{\text{LR}_0^2 \text{C}_d^2}{4\text{NB}}\right), \eta_2 = \frac{\beta}{\text{R}_0} + \frac{2\text{N}}{\text{R}_0^2 \text{C}_d} + \frac{1}{\text{R}_0} - \frac{\text{LR}_0 \text{C}_d^2}{2\text{NB}}, \\ \eta_3 &= \frac{\beta}{\text{R}_0^2} + \frac{2\text{N}}{\text{R}_0^3 \text{C}_d} + \frac{\text{LC}_d^2}{2\text{NB}} \\ \eta_1 \text{ s}^2 + \eta_2 \text{ s} + \eta_3 \end{split} \tag{24}$$

If  $\Delta > 0$ , equation (24) has distinct roots given by

$$x, \ y = \frac{-\eta_2 \pm \sqrt{\eta_2^2 - 4\eta_1 \,\eta_3}}{2\eta_1}$$
 (25)

where, x takes + and y takes - of  $\pm$ 

The discriminate of (25) is positive. After simplification for the discriminant, and expressing in terms of L and  $\beta$ , we get,

$$\xi_1 L^2 + \xi_2 L + \xi_3 > 0$$
 (26)

$$A_1 \beta^2 + A_2 \beta + A_3 > 0 \tag{27}$$

where,

$$\xi_{1} = \left(\frac{c_{d}^{2} R_{0}}{2NB}\right)^{2}$$

$$\xi_{2} = \frac{2\beta c_{d}^{2}}{NB} + \frac{4c_{d}}{R_{0}B} + \frac{c_{d}^{2}}{NB}$$

$$\xi_{3} = \frac{4\beta}{R_{0}^{2}} - \left(\frac{\beta}{R_{0}} + \frac{1}{R_{0}} - \frac{2N}{R_{0}^{2} c_{d}}\right)^{2}$$
(28)

$$\begin{split} A_1 &= \frac{1}{R_0^2} \\ A_2 &= \frac{4N}{R_0^3 \, c_d} - \frac{2}{R_0^2} - \frac{2L{C_d}^2}{NB} \\ A_3 &= \frac{1}{R_0} + \frac{4N^2}{R_0^4 \, c_d^2} - \frac{4N}{R_0^3 c_d} - \\ & \left(\frac{LC_d^2 R_0}{2NB}\right) 2 - \frac{LC_d^2}{NB} - \frac{4LC_d}{R_0B} \end{split}$$

Solving (26) for L= $P_{max}$  and (27) for  $\beta$ , we get

$$0 < p_{\text{max}} \le \frac{-\xi_2 + \sqrt{\xi_2^2 - 4\xi_1 \xi_3}}{2\xi_1}$$
 (29)

$$0 < \beta \le \frac{-A_2 + \sqrt{A_2^2 - 4A_1A_3}}{2A_1} \tag{30}$$

From Equation (23)

$$\delta Q(s) = \frac{y_6}{s(\eta_1 s^2 + \eta_2 s + \eta_3)}$$
$$\delta Q(s) = \frac{y_6}{s(s-x)(s-y)}$$

Using partial fraction,

$$\delta Q(s) = y_6 \left[ \frac{1}{x(x-y)} \frac{1}{(s-x)} - \frac{1}{y(x-y)} \frac{1}{s-y} + \frac{1}{xy} \frac{1}{s} \right]$$

Taking Laplace transform,

$$\delta q(t) = y_6 \left[ \frac{e^{xt}}{x(x-y)} - \frac{e^{yt}}{y(x-y)} + \frac{1}{xy} \right]$$

$$q(t) = q_0 + y_6 \left[ \frac{e^{xt}}{x(x-y)} - \frac{e^{yt}}{y(x-y)} + \frac{1}{xy} \right]$$
(31)

# B. Theorem 3

Given the wireless network parameters  $C_d$ ,  $C_u$ , N,  $R_0$  and B, the instantaneous queue length converges to the target,  $T = \frac{(t_{min} + w_{max})}{2}$  if and only if RED control parameter,  $P_{max}$  and jitter control parameter  $\beta$  satisfies

$$P_{\text{max}} = K_1 K_2 + K_3$$
$$\beta = K_4 K_5$$

where Ki's are given by (35).

*Proof*: From equation (23),

$$\begin{split} \lim_{t \to \infty} \delta q(t) &= \lim_{s \to 0} sQ(s) = \\ \lim_{s \to 0} \frac{y_6}{s^2 + x_1 s + x_3 + \frac{x_2}{2} e^{-R_0 s}} \\ \lim_{t \to \infty} \delta q(t) &= \lim_{s \to 0} sQ(s) = \frac{y_6}{x_3 + x_2/2} + q_0 \\ \lim_{t \to \infty} q(t) &= q_0 + \lim_{t \to \infty} \delta q(t) \end{split}$$

$$\lim_{t \to \infty} q(t) = q_0 + \frac{y_6}{x_3 + \frac{x_2}{2}}$$
 (32)

Let 
$$\lim_{t\to\infty} q(t) = \frac{t_{min} + w_{max}}{2}$$

Then

$$P_{\text{max}} = K_1 K_2 + K_3 \tag{33}$$

$$\beta = K_4 K_5 \tag{34}$$

Where

$$K_{1} = \frac{{}^{4N^{2}}}{{}^{R_{0}}{}^{3}{}^{C}{}_{d}{}^{3}} + \frac{{}^{2\beta N}}{{}^{R_{0}}{}^{2}{}^{C}{}_{d}{}^{2}}$$

$$K_{2} = 2q_{0} - t_{min} - w_{max}$$

$$K_{3} = \frac{{}^{4\beta N}}{{}^{R_{0}}{}^{C}{}_{d}} + \frac{{}^{4N^{2}}}{{}^{R_{0}}{}^{2}{}^{C}{}_{d}{}^{2}}$$

$$K_{4} = \frac{{}^{P_{max}}{{}^{R_{0}}{}^{2}{}^{C}{}_{d}{}^{2} - 4N^{2}}}{{}^{2N+4NR_{0}}{}^{C}{}_{d}}$$

$$K_{5} = 1 + \frac{1}{{}^{R_{0}}{}^{C}{}_{d}} (2q_{0} - t_{min} - w_{max})$$
(35)

Theorem 3 gives a relationship between  $P_{max}$ ,  $\beta$  and  $q_0$ . The relations given in (33), (34) and (35) not only leads to the stability of the system but also brings the instantaneous queue length to converge to the given target value.

# C. Theorem 4

The wireless network system (2) to (4) is asymptotically stable in terms of the state variable  $\delta w(t)$ ,  $\delta q(t)$ , if the equilibrium value of the queue level  $q_0$  satisfies

$$\begin{split} & \frac{t_{min} + w_{max}}{2} - \frac{R_0 C_d}{2} < q_0 \leq \\ & \frac{t_{min} + w_{max}}{2} - \frac{R_0 C_d}{2} - \frac{\xi_2}{\xi_7} + \frac{\xi_8}{\xi_7} \sqrt{\xi_6} \end{split}$$

Proof: Using (33) in (29)

$$0 < \kappa_1 \, \kappa_2 + \kappa_3 \le \frac{^{-\xi_2 + \sqrt{\xi_2}^2 - 4\xi_1 \xi_3}}{^{2\xi_1}}$$

Substituting for K1, K2 and K3 from (35), and simplifying for  $q_0$ , we get

$$\frac{t_{\min} + w_{\max}}{2} - \frac{R_0 C_d}{2} < q_0 \le 
\frac{t_{\min} + w_{\max}}{2} - \frac{R_0 C_d}{2} - \frac{\xi_2}{\xi_7} + \frac{\xi_8}{\xi_7} \sqrt{\xi_6}$$

$$\xi_6 = \frac{C_d^4}{N^2 B^2} \left[ \left( 2\beta + 1 + \frac{4N}{R_0 C_d} \right)^2 + (\beta - 1)^2 + \frac{4N}{R_0 C_d} \left( \frac{N}{R_0 C_d} - \beta - 1 \right) \right]$$

$$\xi_7 = \frac{{}^{2}C_d^{\ 3}}{NB^2} \left(\beta + \frac{2N}{R_0^{\ }C_d^{\ }}\right)$$

$$\xi_8 = \frac{{}^{2}C_d^{\ 2}}{NB}$$
(37)

Theorem 4 gives a stable value for  $q_0$ . With help of this value one can tune the network system parameters to achieve queue convergence and hence obtain good throughput.

#### VI. SIMULATION AND PERFORMANCE ANALYSIS

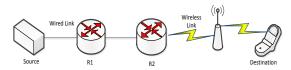


Fig.3. Network Model

A number of simulation experiments are conducted using Matlab R2009b to evaluate the performance of TCP. Fig.3 shows a typical network topology of a heterogeneous network.  $R_1$  and  $R_2$  are the routers and the TCP which has been modeled represents the last hop transmission between  $R_2$  and destination. The propagation time is assumed to be 50 ms. The bottleneck bandwidth ( $C_d$ ) is 10 Mbps, packet size is 1000 bytes and load factor is 10 TCP sessions, k=1,  $R_0=0.1$ s.

#### A. Experiment1: Un-stable network system

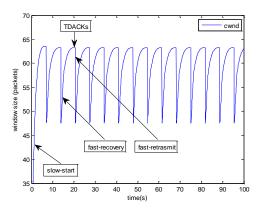


Fig.4. Slow-Start, Congestion Control and Recovery

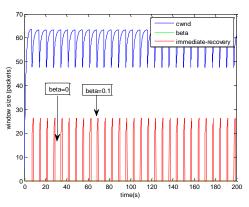


Fig.5. Cwnd Recovery due to Jitter-Loss

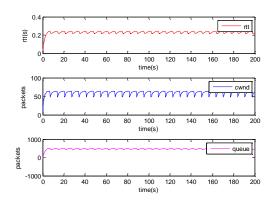


Fig.6. Performance of rtt, cwnd and Queue w.r.t Time

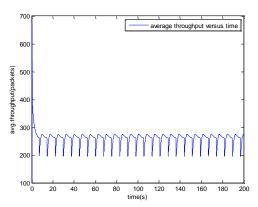


Fig.7. Performance of Throughput w.r.t Time

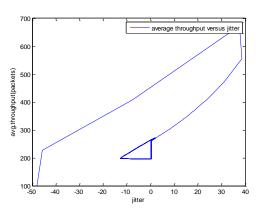


Fig.8. Variation of Throughput w.r.t Jitter

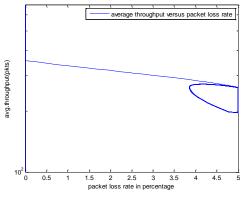


Fig.9. Performance of Throughput w.r.t pkt. Loss

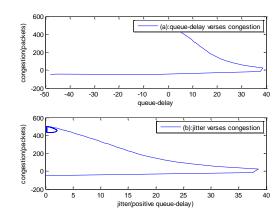


Fig. 10. (a) Congestion due to Queue-Delay (b) Congestion due to Jitter

The trace of the graph of fig.4 represents the typical behaviour of cwnd. The slow-start phase initiate data flow over the connection and increases continuously for every rtt until loss occurs. When the sender cwnd reaches a maximum size of 64 packets, buffer in the bottleneck router starts overflowing. The source receives TDAKs, the cwnd is reduced to half of its current value. For a timeout loss the window size reduces to 1 packet. In addition to timeout loss, the sender does an exponential backoff for some time. The effect of backoff is that the window size does not grow for a small period, after which it starts growing in the normal rate.

To add intelligence to TCP that packet loss is due to transmission and not due to congestion, and mitigate backoff loss, we introduce the term  $L_t(t)$  in equation (2). The traces in fig.5 represent immediate-recovery of sender window due to jittering. The timeout loss experienced by the source and reduction made in its sending rate is unnecessary. To recover the loss TCP initiates immediate-recovery algorithm. The amount of recovery is proportional to sending rate in the previous RTT. The jitter value is compared with k/w value. If it is congestion loss then  $\beta = 0$ , congestion control algorithm is invoked. If it is jitter loss then  $\beta$ =0.1. The traces of fig. 6 represent that the queue length oscillates with the sender window and similarly RTT varies with queue length. As the sender window increases, the queue length also increase because the sending rate by the source is higher than the service rate by the bottleneck router. The bottleneck bandwidth considered is 10 Mb/s. When the cwnd reaches 44 packets then the queue length reaches a minimum threshold value of 200 packets. We observe that when the cwnd is between 45-64 packets, number of packets in the queue is higher than 200 and the congestion avoidance event starts. The bottleneck router stars dropping the packets randomly. Sender TCP on receiving TDACKs, halves its cwnd size.

Throughput depends on the source sending rate. The graph of fig.7 shows that throughput varies over the range of 200 to 280 packets corresponding to cwnd 47 and 64 packets respectively. The traces of fig. 8 show the behaviour of throughput with respect to jitter. In the beginning of the simulation, jitter value is negative resulting highest throughput. As the simulation time lapses jitter value becomes positive resulting in the

decrease of throughput. When the jitter value reaches a maximum of 40 ms throughput drops suddenly to a small value. Traces of fig. 9 represent that throughput decreases with the increase of percentage packet loss rate. When the loss rate is between 4% to 5%, throughput falls by 30% but recovers immediately. The occurrence of jitter can be noticed by measuring the variation in queuing-delay at the destination. fig. 10(a) represents the variation of congestion in the bottleneck router with respect to (w.r.t) queue-delay. The later packet reaches the destination taking more time than the previous packet, causing variation in the inter arrival time of packets. This is due to transmission and is more frequent in wireless networks. Thus, Jittering triggers into timeout loss. fig. 10(b) gives the traces of congestion with respect to jitter. From the graph, the congestion slowly builds up with respect to increase in jitter, when jitter decrease, congestion reaches a maximum value of 500 packets because of the fact that many TCPs sessions are pumping large number of packet into the network (load), resources are being shared optimally.

## B. Experiment 2: Stable network system

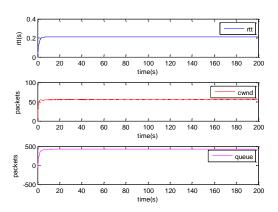


Fig.11. Asymptotic Stability of rtt, cwnd, Queue

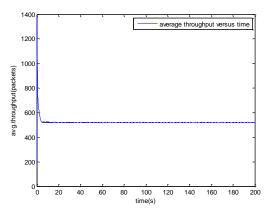


Fig.12. Stable Throughput

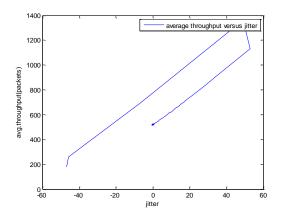


Fig.13. Stable Throughput w.r.t Jitter

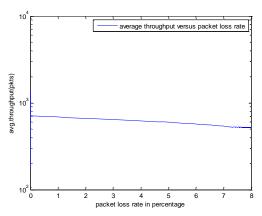


Fig.14. Stable Throughput w.r.t pkt-loss

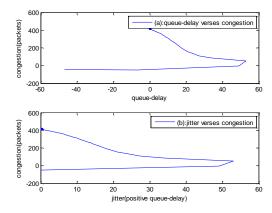


Fig.15. (a) Stable Congestion due to Queue-Delay (b) Stable Congestion due to Jitter

Fig. 11 to fig. 15 are the graphs of stable network system. The experiment was conducted by assuming the propagation delay as 50 ms. The bottleneck bandwidth is 10 Mbps, packet size is 1000 bytes and load factor is 10 TCP sessions. Minimum and maximum threshold values of the queue buffer are 200 and 500 packets respectively. The initial values of  $R_0 \!\!=\!\! 0.04s$  and  $\beta \!\!=\!\! 0$  and using relation (19), initial value of  $p_{max}$  was calculated. Using this initial  $p_{max}$  value and relation (20), next value of  $\beta$  was calculated. After small laps of simulation time,  $P_{max}$  and  $\beta$  converges to values 0.1067 and 0.3846 respectively. Traces of fig. 10 and fig. 11 shows that rtt, sender

window size, queue length and throughput values stabilise to 0.21s, 56 packets, 425 packets and 520 packets respectively. The graph of fig. 13, fig.14 and fig.15 gives the variation of throughput with respect to jitter, variation of throughput with respect to packet-loss rate and variation of congestion with respect to jitter respectively. The graphs are smooth and not oscillatory. The experimental results shows that for a given resources, stability boundary increases the throughput value by 30% by minimising the packet losses.

## C. Experiment 3: Queue convergence analysis

The simulation was conducted for different target values as summarised in table 1. For each of the simulations, the stability range of q<sub>0</sub> was calculated using relation (36), Using the  $q_0$  value,  $P_{\text{max}}$  value was calculated using relation (29) with an initial value of  $\beta$ =0.1, and finally using the value of  $p_{max}$ ,  $\beta$  was estimated using relation (30). In simulation 1, target queue length, T=500, the range of  $q_0$  is (459.8, 464.96), chose q0 = 462.38, Value of  $P_{max} = 0.544$ , and  $\beta = 0.0089$ . The graph of instantaneous queue length is as illustrated in fig. 4.16. Approximately, 93 % of the traces of the graph values fall around  $q_0$ . In simulation 2, target queue length, T=550, the range of  $q_0$  is (506.32, 512.69), chose  $q_0$  = 509.5, Value of  $P_{max}$  =0.0013, and  $\beta$ =0.0024.The graph of instantaneous queue length is as illustrated in fig. 17. About 96 % of the traces of the graph values fall around q<sub>0</sub>. In simulation 3, target queue length, T=600, the range of  $q_0$  is (555.16, 561.03), chose  $q_0 = 558.09$ , Value of  $P_{max}$  =0.112, and  $\beta$ =0.0018. The graph of instantaneous queue length is as illustrated in fig.18. Almost, 93 % of the traces of the graph values fall around  $q_0$ .

Table 1. Simulation results

1	2	3	4	5	6	7
1	(400, 600)	500	(459.8 ,464.96)	462.38	0.544	0.0089
2	(400, 700)	550	(506.32, 512.69)	509.5	0.0013	0.0024
3	(400, 800)	600	(555.16, 561.03)	558.09	0.112	0.0018

1: Simulation, 2: Minimum and Maximum threshold, 3: Target queue, 4: Stability range, 5: q<sub>0</sub>- value, 6: P<sub>max</sub> -value, 7: β-value.

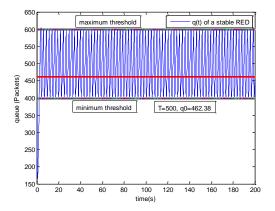


Fig.16. Queue Length when T= 500 Packets

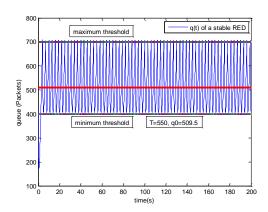


Fig.17. Queue Length when T= 550 Packets

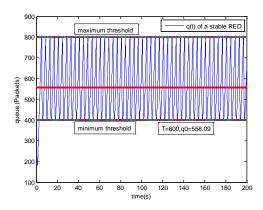


Fig.18. Queue Length when T=600 Packets

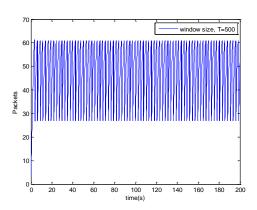


Fig.19. TCP Window when T= 500 Packets

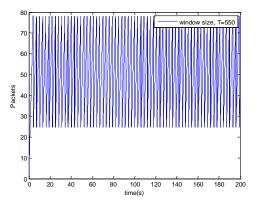


Fig.20. TCP Window when T= 550 Packets

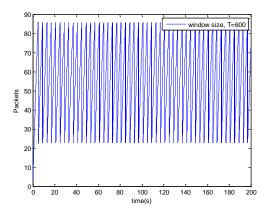


Fig.21. TCP Window when T= 600 Packets

Figs. 19, 20, and 21, illustrates the traces of TCP window dynamics for the threshold values 500, 550 and 600 respectively. Cwnd varies over the range (26, 60), (24, 77), and (22, 85) for T=500, 550, and 600 respectively. As the value of T increases, the lower bound of decreases whereas upper bound increases.

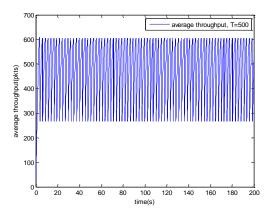


Fig.22. Average Throughput when T= 500 Packets

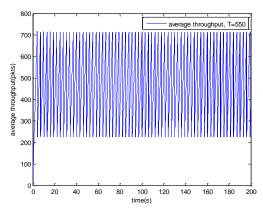


Fig.23. Average Throughput when T= 550 Packets

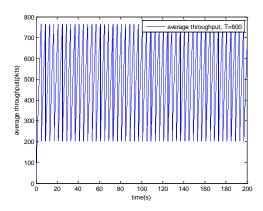


Fig.24. Average Throughput when T= 600 Packets

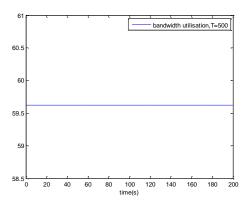


Fig.25. Bandwidth Utilisation when T= 500 Packets

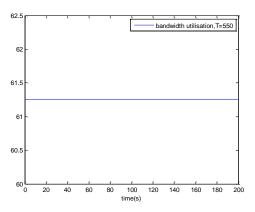


Fig.26. Bandwidth Utilisation when T= 550 Packets

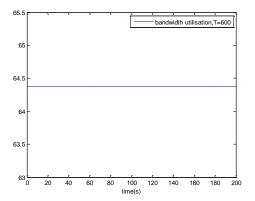


Fig.27. Bandwidth Utilisation when T= 600 Packets

Figs. 22, 23, and 24 illustrate the traces of average throughput and Figures 25, 26, and 27 illustrates the traces of bandwidth utilisation for different threshold values. The bandwidth utilisation increases with the increase of target values.

#### VII. CONCLUSION

In this paper, we enhance the performance of TCP in presence of jitter in wireless networks. Jitter is one transmission loss which occurs most frequently in wireless networks. Jitter leads to timeout loss resulting sudden drop in the throughput. The model has the capability of recognising the congestion loss from that of jitter loss. k/w loss-predictor technique is used to achieve this task. k/w loss-predictor function uses queuing-delay and average rtt-delay (Next-RTT) as an input for prediction. When the sender TCP identified that next packet loss is due to jitter, the loss incurred in the throughput is tried to recover using immediate-recovery algorithm considering  $\beta$ =0.1. The proposed model also provides an end-to-end congestion control. For further improvement in the performance of the model, we discuss stability analysis. A time-delay control theory is applied. The application of asymptotic stability helps in tuning the control parameters  $p_{\text{max}}$  and  $\beta$  so that the network system works in a stable condition. This also controls the oscillatory behaviour of the RED router. The implementation minimises the packet loss and increases the throughput approximately by 25%. In the last section of the paper, convergence analysis of queue length is discussed. An approximate solution for q(t) is derived. Convergence of q(t) for a given target value subject to that  $p_{max}$  and  $\beta$  satisfies certain condition is established. The stability region of q<sub>0</sub> is also presented there by our results provide global stability and convergence condition of the system. The described model works for networks which are associated with queuing servers with constant or variable service times. The model presented in the work is efficient, fair and adaptable to wireless networks.

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# **Authors' Profiles**



N.G.Goudru received his Ph.D degree in Mathematics from Gulbarga University, Karnataka in 1989, M.Sc (Applied Mathematics) degree from Karnataka University, Dharwar in 1981, M.S (Software Systems) degree from BITS, Pilani in 1994. He is working as a professor in the department of Mathematics, BMS

Institute of Technology, Bangalore, Karnataka. His major areas of research are in Computational fluid dynamics and wireless mobile networks.



**B.P.Vijaya Kumar** received his Ph. D degree in Electrical and Communication Engineering. department from Indian Institute of Science (IISc), Bangalore in 2003, M.Tech degree in Computer Science and Technology from the University of Roorkee (Presently Indian Institute of Technology, IITR), with honors in 1992

and Bacholers degree in Electronics and Communications from Mysore University with Distinction in the year 1987. He is currently working as a professor and Head of Information Science and Engineering department, MS Ramaiah Institute of Technology, Bangalore, Karnataka, India, where he is involved in research and teaching UG and PG students, and his major area of research are Computational Intelligence applications in Mobile, Adhoc and Sensor networks.

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